

# Determination of $\gamma$ from $B^\pm \rightarrow DK^\pm$ : LHCb and CLEOC

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# Outline

- Motivation for the precise determination of  $\gamma$
- LHCb
  - Overview
  - Status
- Measuring  $\gamma$  with  $B^\pm \rightarrow DK^\pm$  at LHCb
- Complementary measurements of  $D$  decay at CLEO-c

# Flavour physics

Flavour physics has been essential to formation of the Standard Model:

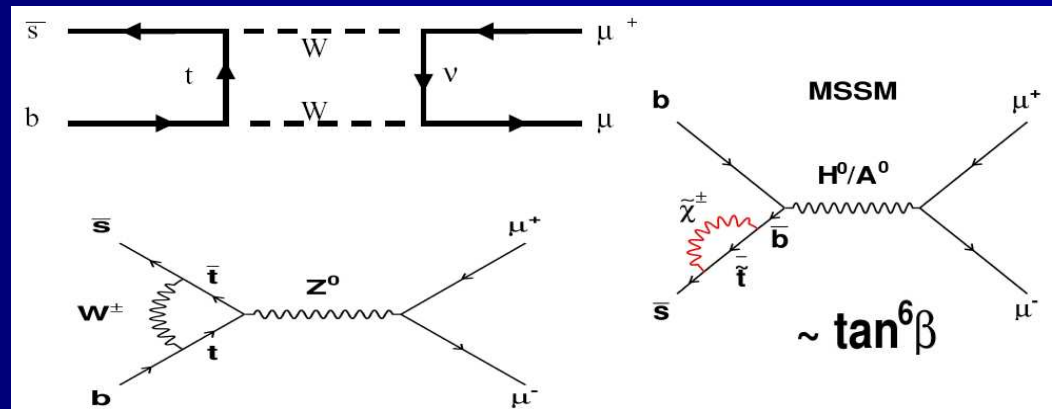
- **GIM mechanism** → charm
- **CP Violation** → 3 generations
- **B mixing** → heavy top

All surprises that predated  
'direct' discovery!

**We may assume same story will continue!**

Precise measurements ⇒ nature of new physics at multi-TeV scale

In B physics goal is to look for new sources of CP violation, or deviations from SM in very rare CP conserving processes, eg.  $BR(B_s \rightarrow \mu\mu)$



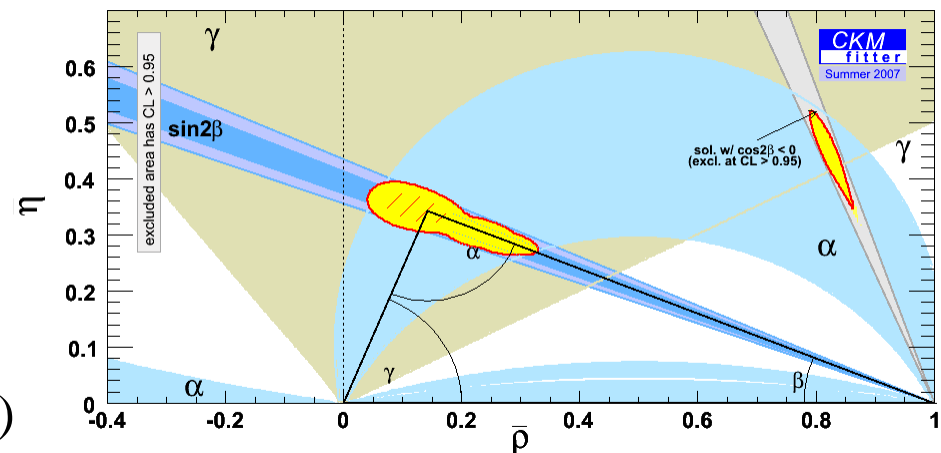
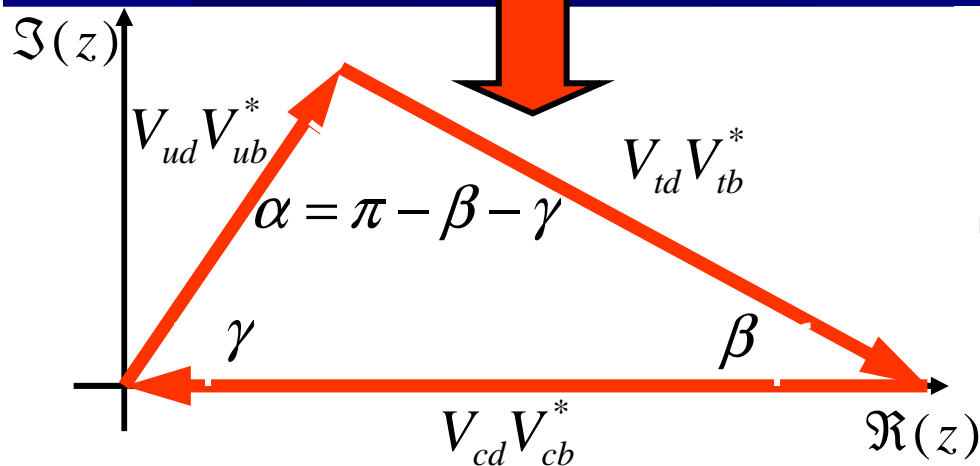
# CP violation in weak decays of quarks

- CP violation implies differences between **matter** and **antimatter**
- In the Standard Model the weak and flavour eigenstates of the three generations of quarks are related by a unitary matrix
- A complex phase introduces CP violating effects
- Represented in terms of the **Unitarity Triangle**

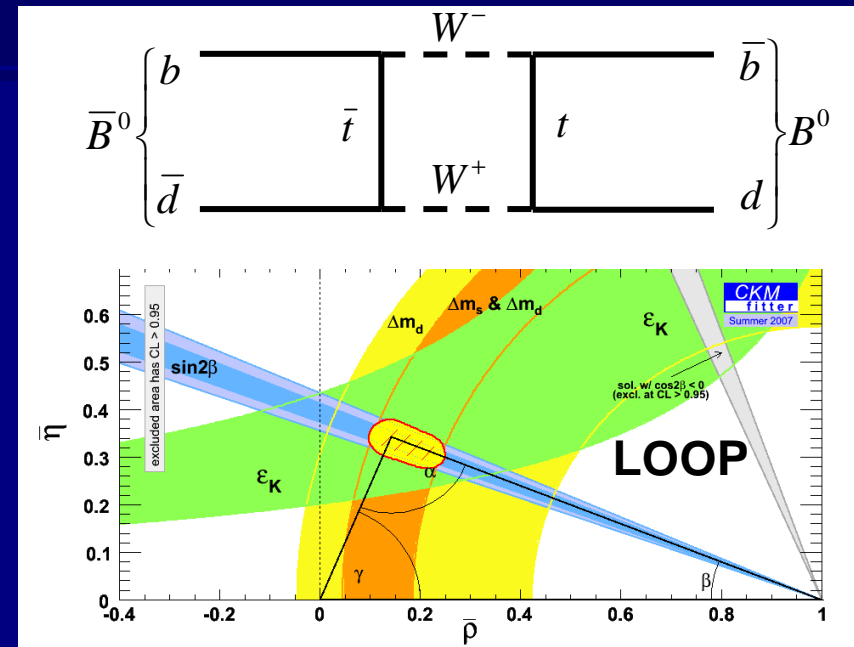
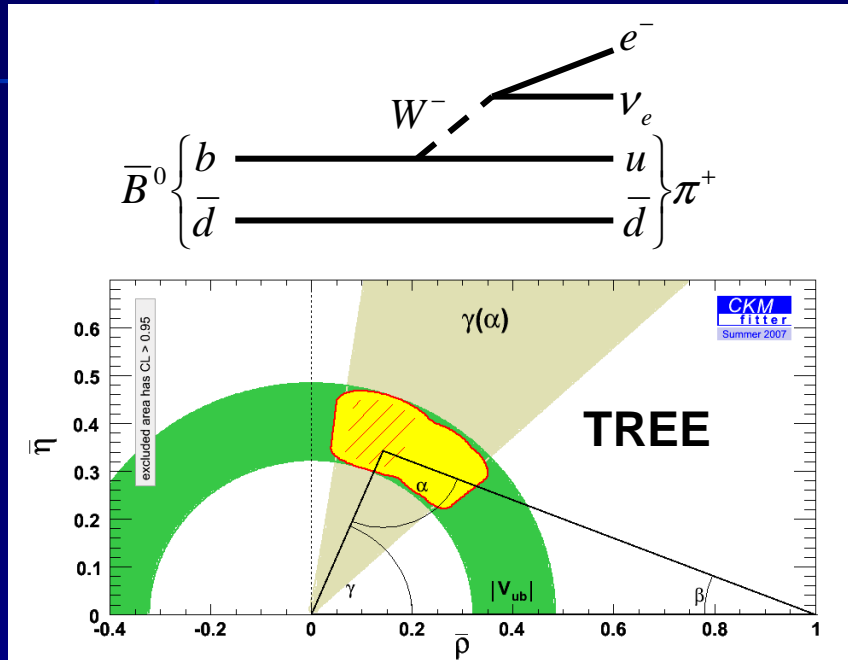
$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \propto e^{i\gamma} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} \propto e^{i\beta} & V_{ts} & V_{tb} \end{pmatrix}$$

All sides and angles can be measured in *b*-hadron decay

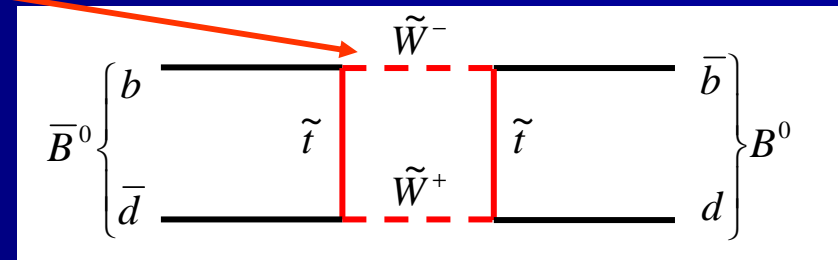
$$V_{\text{CKM}} V_{\text{CKM}}^\dagger = I \Rightarrow V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$



# Searching for new physics



- Non Standard Model particles contribute within the **virtual loops**
- Differences between tree-level and loop-level triangles
  - **Signature of new physics**
- **Complements direct searches**

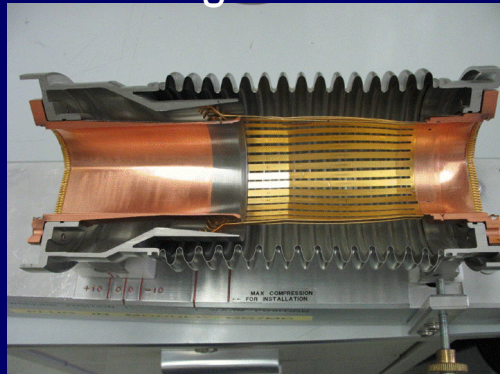
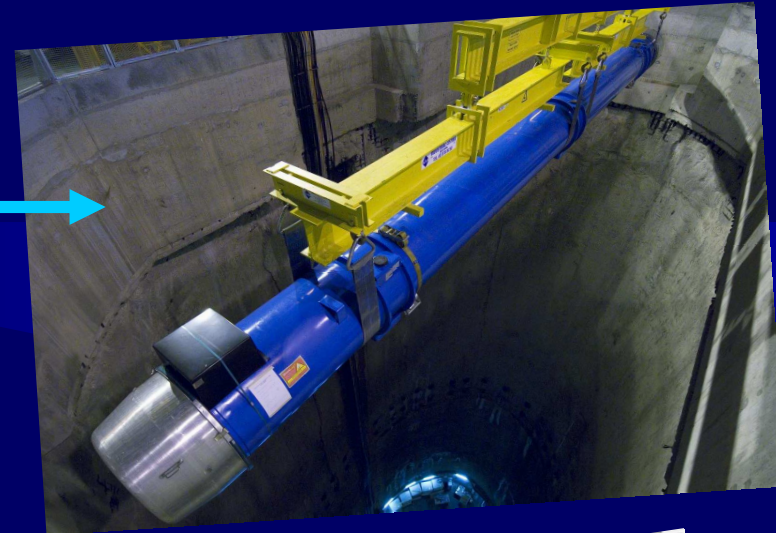


# LHC Status

- Last dipole lowered April 26<sup>th</sup> this year! (First was in March 2005)
- Last interconnect – Nov 2007
- Quad triplet remediation – Sep 2007

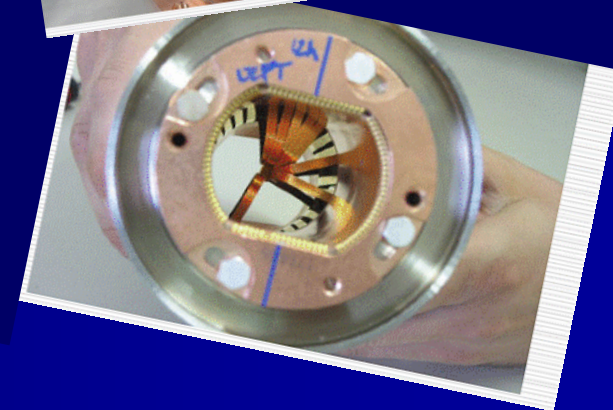
Latest official schedule had beam commissioning beginning in May '08, with then 2 months estimated before first 14 TeV collisions

Since then, there have been problems, eg. with shielding bellows in cold interconnects



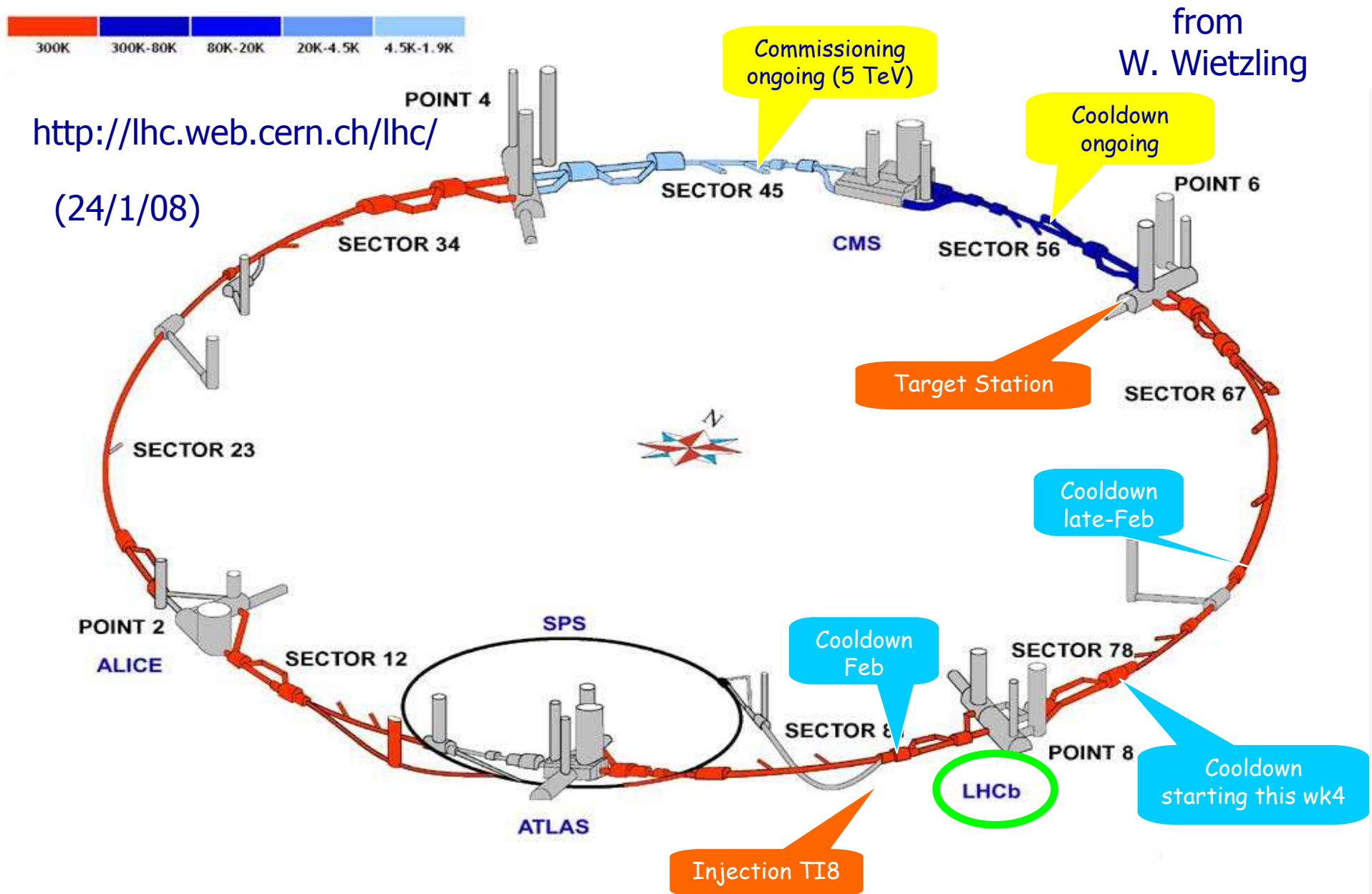
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Warm up of sector 7-8



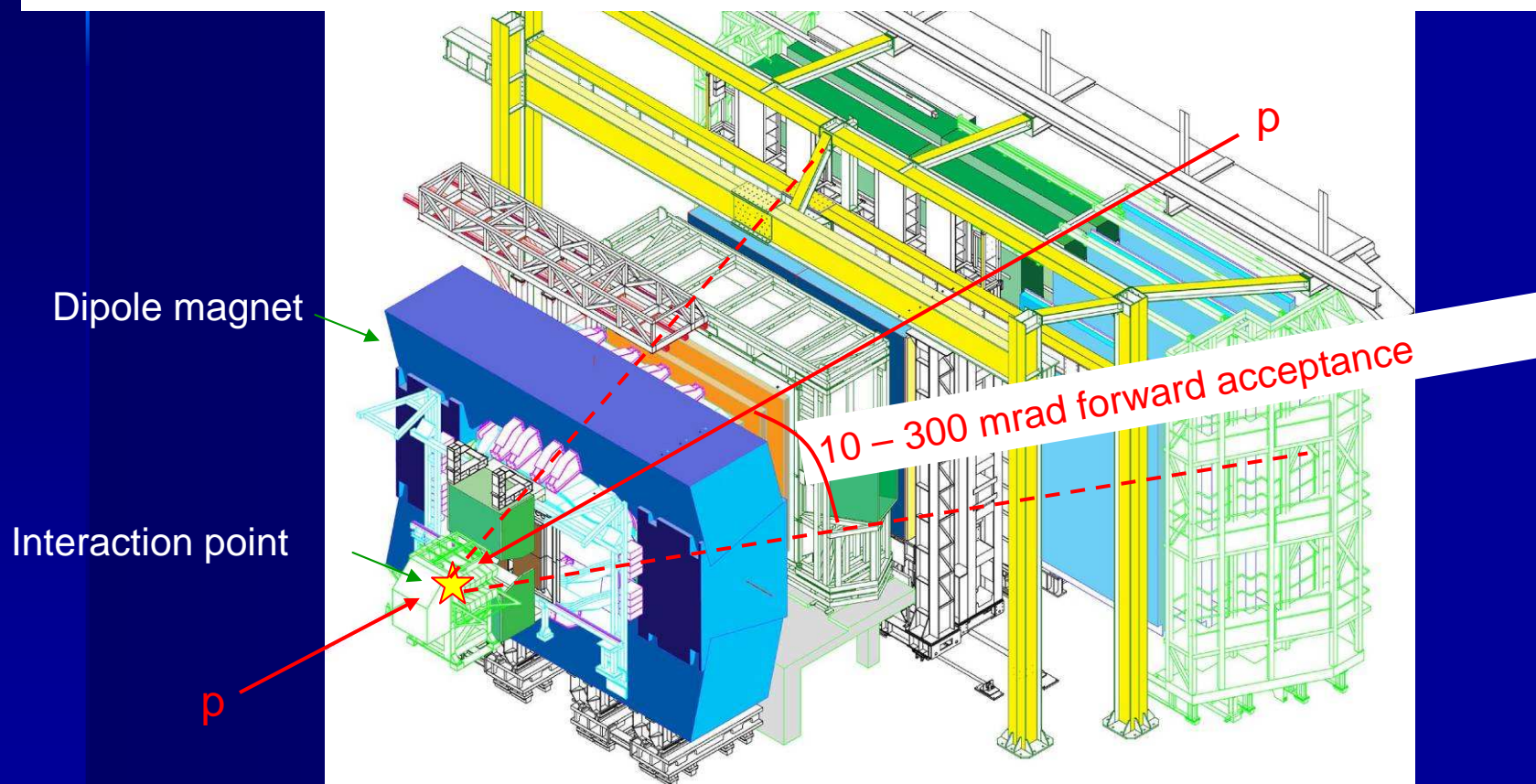
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# Status of the LHC Machine



# The LHCb Experiment

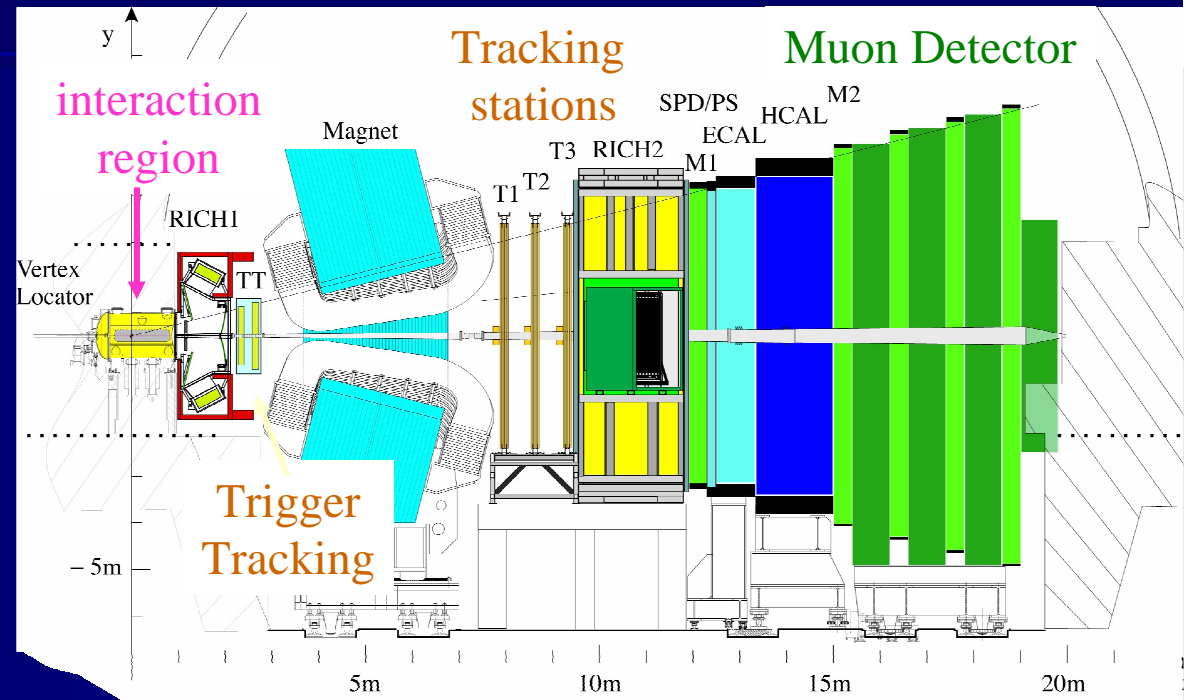
- ❑ Dedicated experiment for precision measurement of CP violation and rare decays of b-hadrons (and charm) at the LHC
- ❑ Collider-mode operation at same time as the general-purpose detectors, with less-focused beams → most events have a single pp interaction





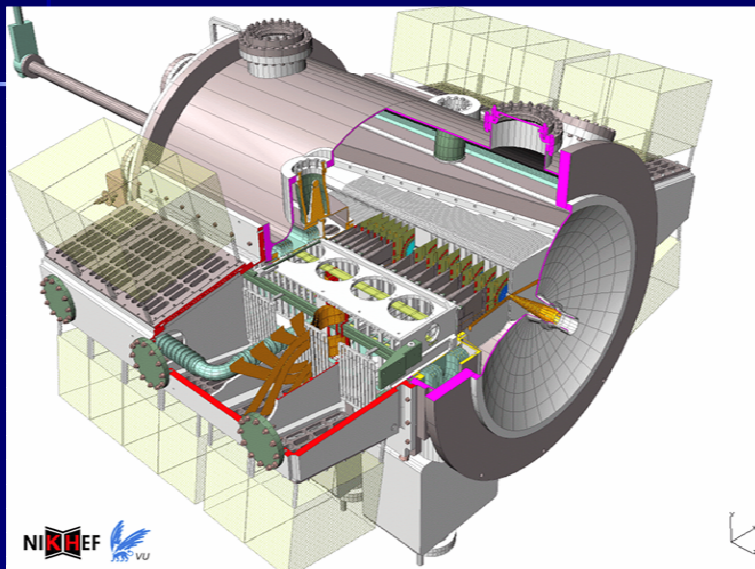
# LHCb in a slide

- $pp$  collisions at a centre of mass energy of 14 TeV
  - $10^{12} \text{ } b\bar{b}/\text{year}$
- Ring Imaging Cherenkov detectors
  - hadron ID for momentum from 2 to 100 GeV/c

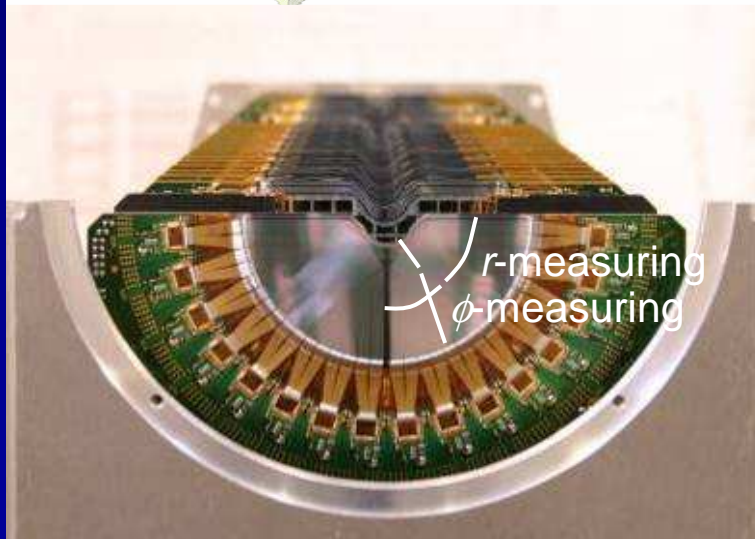


- First level hardware trigger rate from 10→1 MHz
  - 10 MHz the rate of bunch crossings with 1 or more interaction
  - Bunch crossing rate 30 MHz (offset interaction point)
- Software Higher Level Trigger (HLT):
  - inclusive and exclusive selections to reduce storage rate to 2 kHz

# Si Vertex Locator (VELO)



NIKHEF 



1st February 2008

- 21 stations of Si wafer pairs with  $r$  and  $\phi$  strip readout
- Split in two halves to allow retraction from beam line
  - When closed 8 mm from beam
- Both detector halves now installed in the pit



UCL S

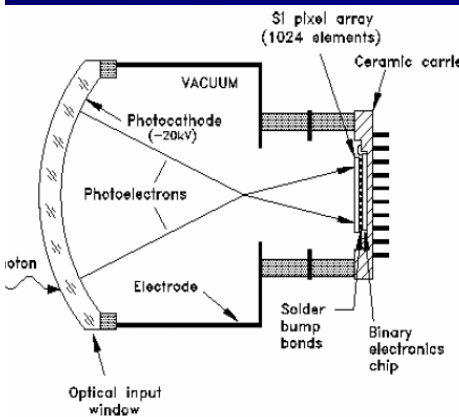
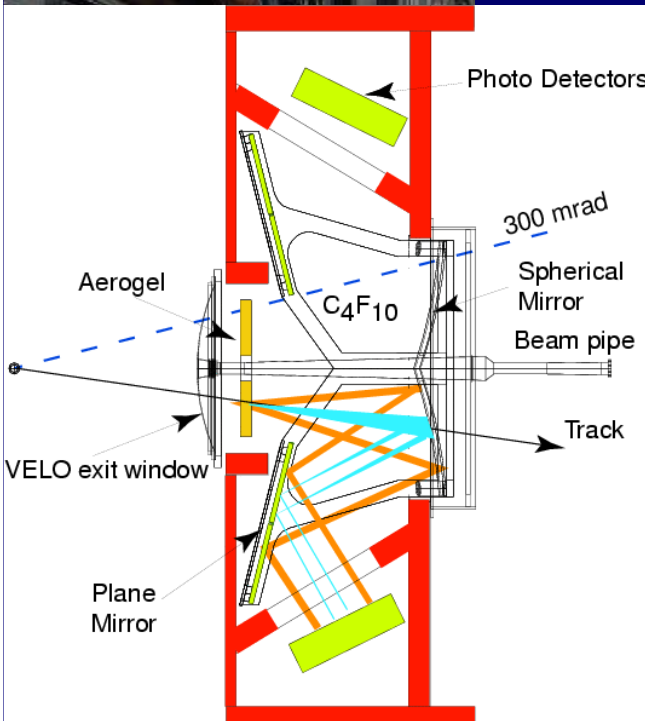
# RICH



RICH1



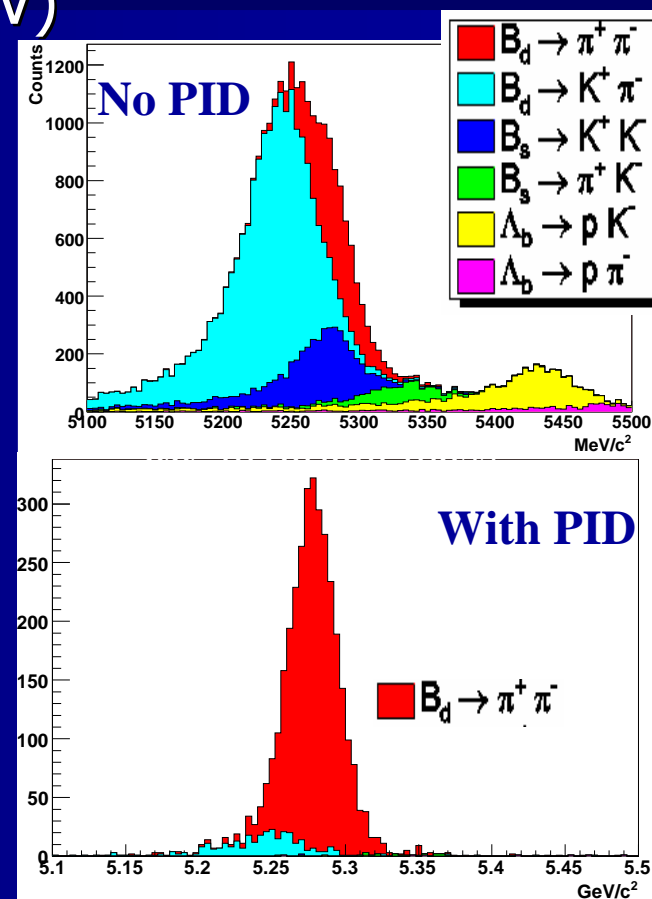
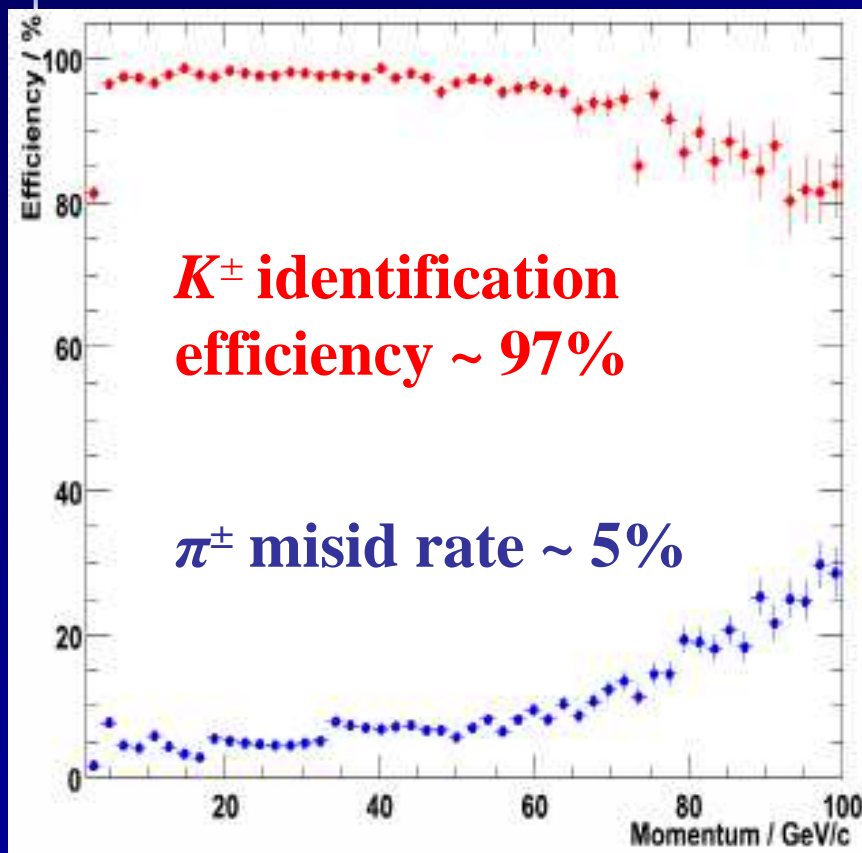
RICH2



Readout: Hybrid PhotoDiodes HPD  
 – 1024 pixels – LHCb development

# RICH Detectors

3 radiators: RICH1 Aerogel (2-10 GeV), C<sub>4</sub>F<sub>10</sub> (10-60 GeV)  
RICH2 CF<sub>4</sub> (16-100 GeV)



Status: RICH2 ready: full DAQ exercised  
RICH1: full commissioning early 2008

$\pi\pi$  invariant mass

# Trigger

## Full bandwidth for flavour unlike GPDs

### Hardware trigger (L0)

- Fully synchronized (40 MHz), 4  $\mu$ s fixed latency
- High  $p_T$  particles:  $\mu$ ,  $\mu\mu$ , e,  $\gamma$  and hadron
  - (typically  $p_T \sim 1-4$  GeV/c)

1 MHz (readout of all detector components)

### Software trigger (HLT)

- Full detector info available, only limit is CPU time
- Use more tracking info to re-confirm L0+high IP
- Full event reconstruction: exclusive and inclusive streams tuned for specific final states

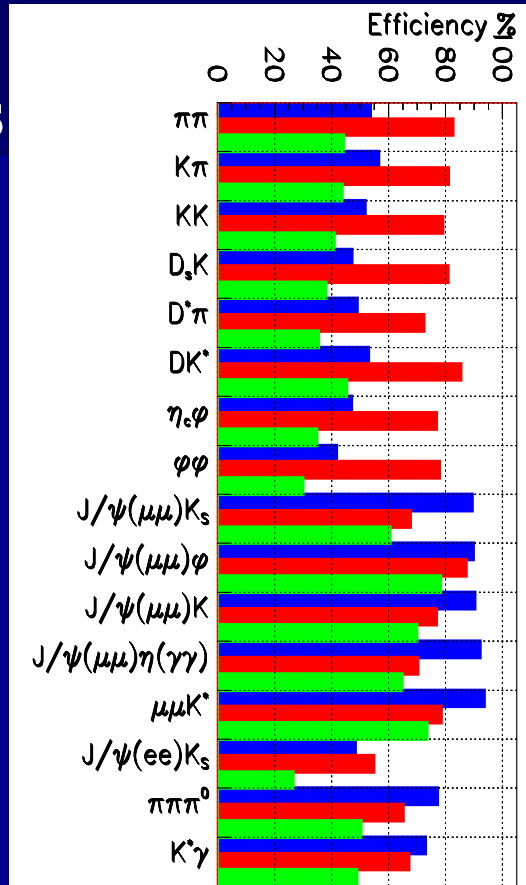
$\leq 2$  kHz (storage: event size  $\sim 35$  kB)

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PC farm of  $\sim 1000$  nodes

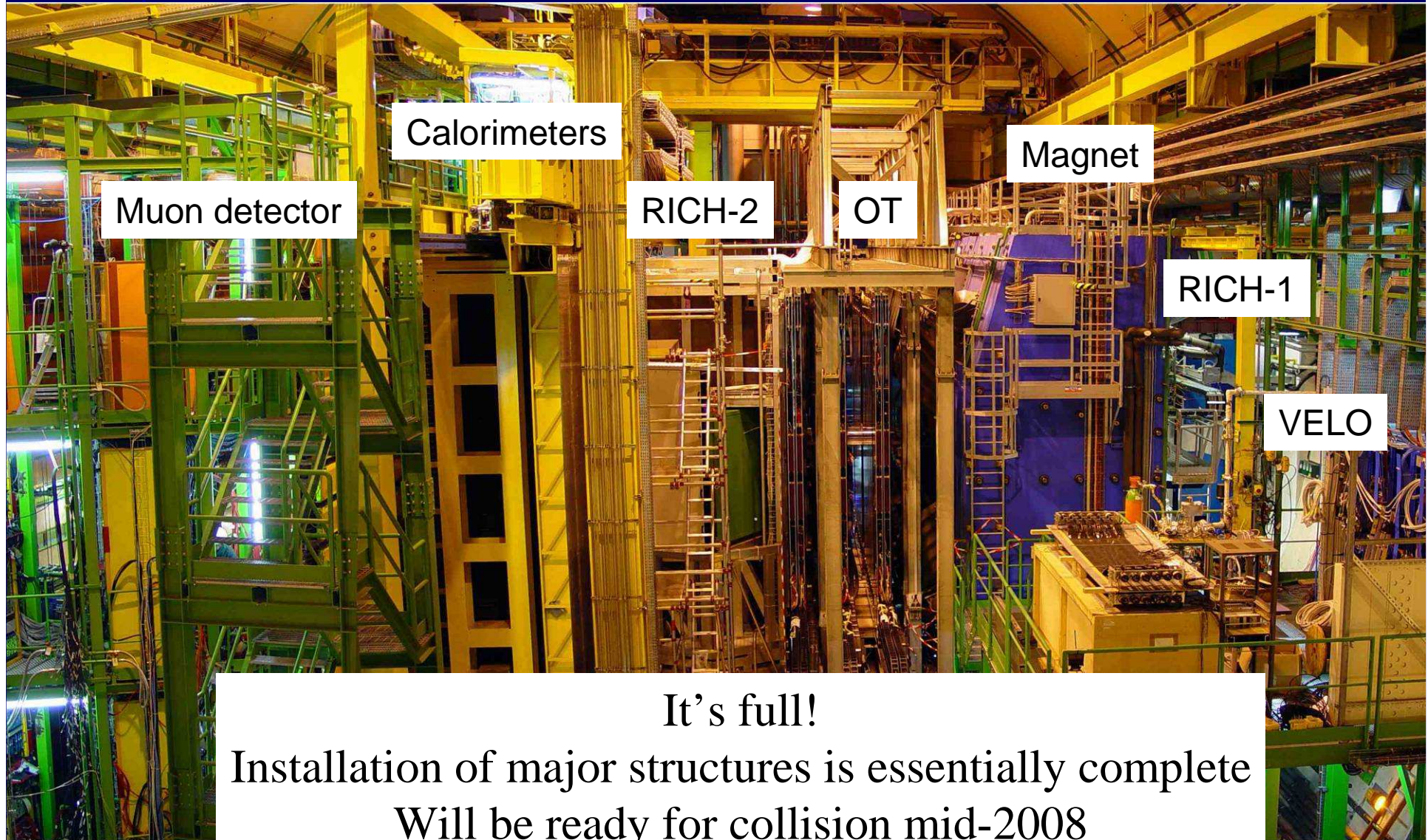
(multicore)

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L0 HLT and  
L0 x HLT efficiency

# View of the cavern



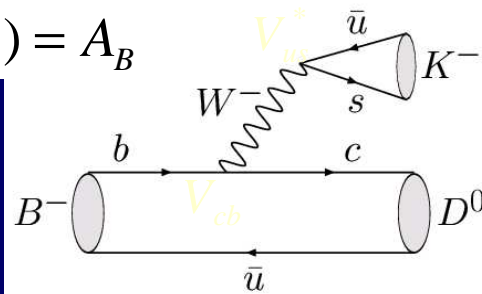
It's full!  
Installation of major structures is essentially complete  
Will be ready for collision mid-2008

# Introduction $B^{\pm} \rightarrow DK^{\pm}$

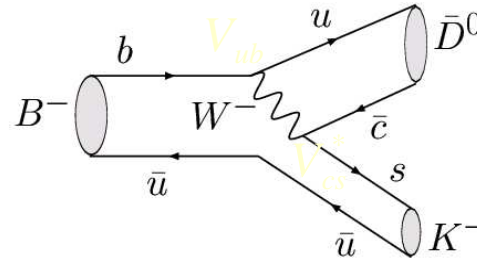
- $B \rightarrow DK$  decays involve  $b \rightarrow c$  and  $b \rightarrow u$  transitions

Strong phase difference

$$A(B^- \rightarrow D^0 K^-) = A_B$$



$$A(B^- \rightarrow \bar{D}^0 K^-) = A_B r_B e^{i(\delta-\gamma)}$$



Ratio of absolute amplitudes of colour/CKM suppressed to favoured ( $\sim 0.1$ )

- Access  $\gamma$  via interference if  $D^0$  and  $\bar{D}^0$  decay to the same final state
- These measurements are theoretically clean
  - No penguin  $\Rightarrow$  CKM standard candle
  - largest correction is sub-degree from D-mixing
- LHCb looking at a number of strategies to study such decays
  - $B^+$ : Atwood-Dunietz-Soni ('ADS'), 3 and 4 body Dalitz Plot Anal.

# $B^\pm \rightarrow D(K_S^0 \pi^+ \pi^-) K^\pm$

- For  $B^+ \rightarrow D(K_S^0 \pi^+ \pi^-) K^+$

$$A^- = f(m_+^2, m_-^2) + r_B e^{i(-\gamma+\delta)} f(m_-^2, m_+^2)$$

$$A^+ = f(m_+^2, m_-^2) + r_B e^{i(\gamma+\delta)} f(m_-^2, m_+^2)$$

$m_\pm = K_S^0 \pi^\pm$  invariant mass and  $f(m_\pm^2, m_\mp^2)$  Dalitz amplitudes

- Assume isobar model (sum of Breit-Wigners)

Number of resonances

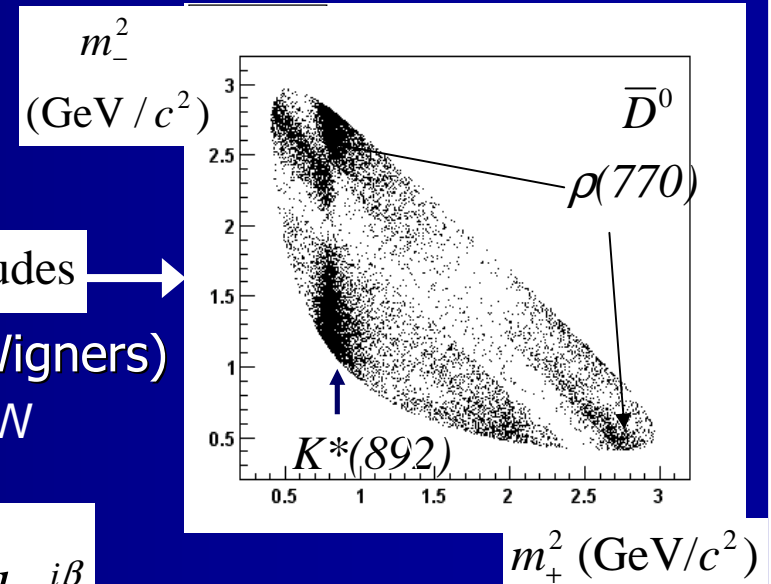
Rel. BW

$$f(m_+^2, m_-^2) = \left[ \sum_{j=1}^N a_j e^{i\alpha_j} A_j(m_+^2, m_-^2) \right] + b e^{i\beta}$$

Amplitude and phase extracted from  $D^{*+} \rightarrow D^0 \pi^+$  sample at B-factories

Non-resonant

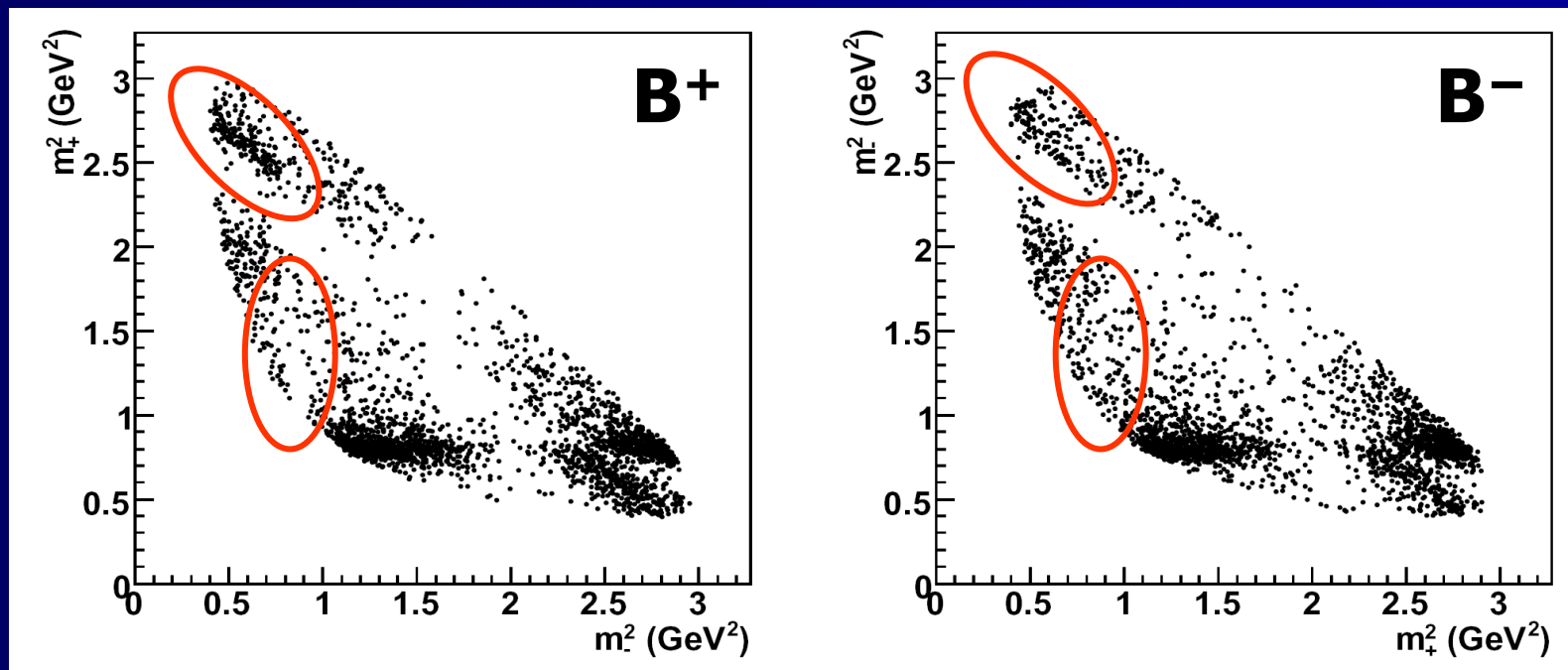
- Fit  $D$ -Dalitz plots from  $B$ -decay to extract  $\gamma$ ,  $r_B$  and  $\delta_B$





$$B^{\pm} \rightarrow D(K^0_S \pi^+ \pi^-) K^{\pm}$$

Absence of CP violation: distributions would be identical



Simulated LHCb data

# Current $e^+e^-$ results

PRD 73, 112009 (2006)  
hep-ex/0607104

- Current best direct constraints on  $\gamma$ :

$$\phi_3 = (53_{-18}^{+15}(\text{stat}) \pm 3(\text{syst}) \pm 9(\text{model}))^\circ \text{ [Belle]}$$

$$\gamma = (92 \pm 41(\text{stat}) \pm 11(\text{syst}) \pm 12(\text{model}))^\circ \text{ [BABAR]}$$

- Based on  $\sim 300$  events each ( $\sim 1/3$  of final data set)
- **However, large error from isobar model assumptions**
- BABAR and Belle use large samples of flavour tagged  $D^{*+} \rightarrow D^0\pi^+$  events to find parameters of the isobar model
  - Excellent knowledge of  $|f|^2$  but phases less well known
- Model uncertainties from assumptions about the resonance structures in the model

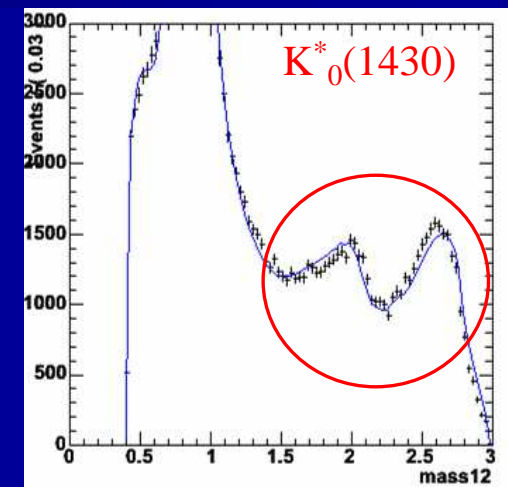
# Isobar model uncertainty

BABAR (PRL 95 121802,2005)

Resonance	Amplitude	Phase (deg)	Fit fraction
$K^*(892)^-$	$1.781 \pm 0.018$	$131.0 \pm 0.8$	0.586
$K_0^*(1430)^-$	$2.45 \pm 0.08$	$-8.3 \pm 2.5$	0.083
$K_2^*(1430)^-$	$1.05 \pm 0.06$	$-54.3 \pm 2.6$	0.027
$K^*(1410)^-$	$0.52 \pm 0.09$	$154 \pm 20$	0.004
$K^*(1680)^-$	$0.89 \pm 0.30$	$-139 \pm 14$	0.003
$K^*(892)^+$	$0.180 \pm 0.008$	$-44.1 \pm 2.5$	0.006
$K_0^*(1430)^+$	$0.37 \pm 0.07$	$18 \pm 9$	0.002
$K_2^*(1430)^+$	$0.075 \pm 0.038$	$-104 \pm 23$	0.000
$\rho(770)$	1 (fixed)	0 (fixed)	0.224
$\omega(782)$	$0.0391 \pm 0.0016$	$115.3 \pm 2.5$	0.006
$f_0(980)$	$0.482 \pm 0.012$	$-141.8 \pm 2.2$	0.061
$f_0(1370)$	$2.25 \pm 0.30$	$113.2 \pm 3.7$	0.032
$f_2(1270)$	$0.922 \pm 0.041$	$-21.3 \pm 3.1$	0.030
$\rho(1450)$	$0.52 \pm 0.09$	$38 \pm 13$	0.002
$\sigma$	$1.36 \pm 0.05$	$-177.9 \pm 2.7$	0.093
$\sigma'$	$0.340 \pm 0.026$	$153.0 \pm 3.8$	0.013
Non Resonant	$3.53 \pm 0.44$	$128 \pm 6$	0.073

- Most challenging aspects of the model uncertainty come from  $K\pi$  and  $\pi\pi$  S-wave

Fit to flavour tag sample



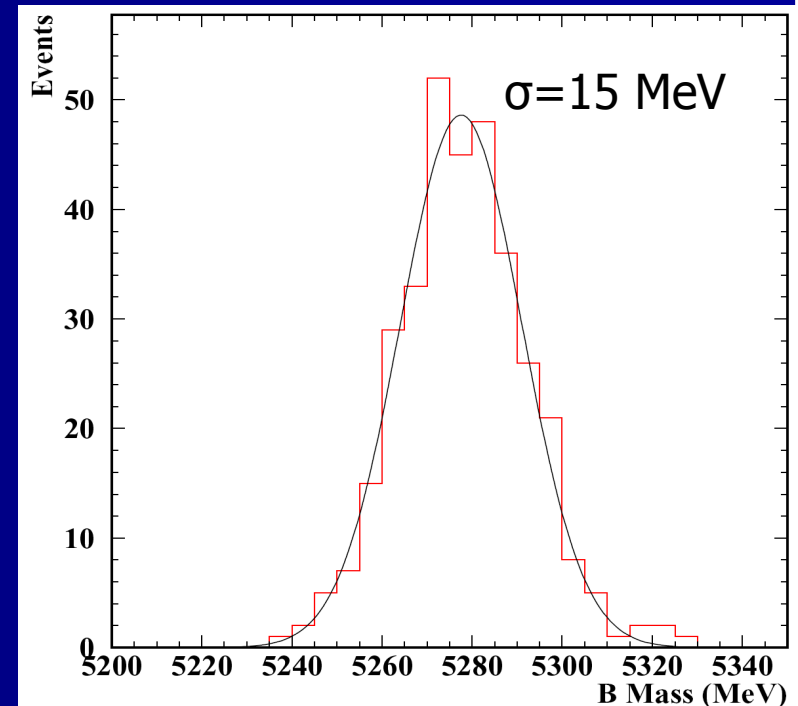
# $B^\pm \rightarrow D(K_S^0 \pi^+ \pi^-) K^\pm$ at LHCb

- Simulation studies performed to determine the expected yields and backgrounds at LHCb
  - One 'nominal' year of data-taking  $2 \text{ fb}^{-1}$
  - Total luminosity goal  $10 \text{ fb}^{-1}$
- Selection studies performed on PYTHIA/EVTGEN/GEANT4 simulated samples of signal and background events
- Limited statistics available for background estimates
  - 34 million  $b$ -inclusive events corresponds to  $\sim 15$  minutes of data taking at nominal luminosity
- Trigger simulation is applied for Level-0 and large impact parameter with  $p_t$  HLT

# $B^\pm \rightarrow D(K_S^0 \pi^+ \pi^-) K^\pm$ at LHCb

(LHCb-048-2007)

- Selection based on large impact parameter, RICH particle ID and good p resolution
- Efficiency =  $0.7 \times 10^{-3}$
- Backgrounds:
  - $B^\pm \rightarrow D(K_S^0 \pi^+ \pi^-) \pi^\pm$   
B/S=0.24
  - Combinatoric  
B/S < 0.7 at 90% c.l.



**5000 events/2fb<sup>-1</sup>**

# Model uncertainty impact on LHCb

- The model-dependent likelihood fit yields an uncertainty on  $\gamma$  between  $7-12^\circ$  for an  $r_B=0.1$ 
  - Range represents differing assumptions about the background
- However, the current model uncertainty is  $10-15^\circ$  with an  $r_B=0.1$ 
  - Uncertainties  $\propto 1/r_B$
- **Without improvements LHCb sensitivity will be dominated by model assumptions within 1 year of data taking**
- Motivates a model-independent method that relies on a binned analysis of the Dalitz plot
  - Disadvantage is that information is lost via binning

# Binned method

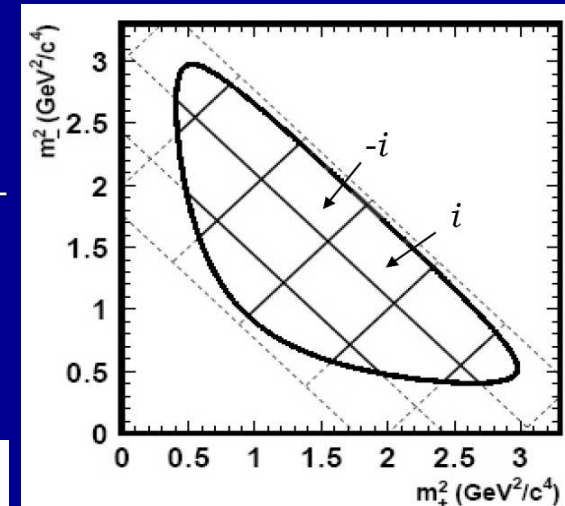
- Proposed in the original paper by Giri, Grossman, Soffer and Zupan and since been extended significantly by Bondar and Poluektov
  - GGSZ, PRD **68**, 054018 (2003)
  - BP, most recently arXiv:0711.1509v1 [hep-ph]
- Bin the Dalitz plot symmetrically about  $m_-^2 = m_+^2$  then number of entries in  $B^-$  decay given by:

$\propto$  # events in bin of flavour tagged  $D^0$  decays

$$N_i^- \propto \int_{D_i} |f(m_-^2, m_+^2)|^2 dD + r_B^2 \int_{D_i} |f(m_+^2, m_-^2)|^2 dD + 2\sqrt{\int_{D_i} |f(m_-^2, m_+^2)|^2 dD \int_{D_i} |f(m_+^2, m_-^2)|^2 dD} (x_- c_i + y_- s_i)$$

$$x_{\pm} = r_B \cos(\delta_B \pm \gamma) \quad y_{\pm} = r_B \sin(\delta_B \pm \gamma)$$

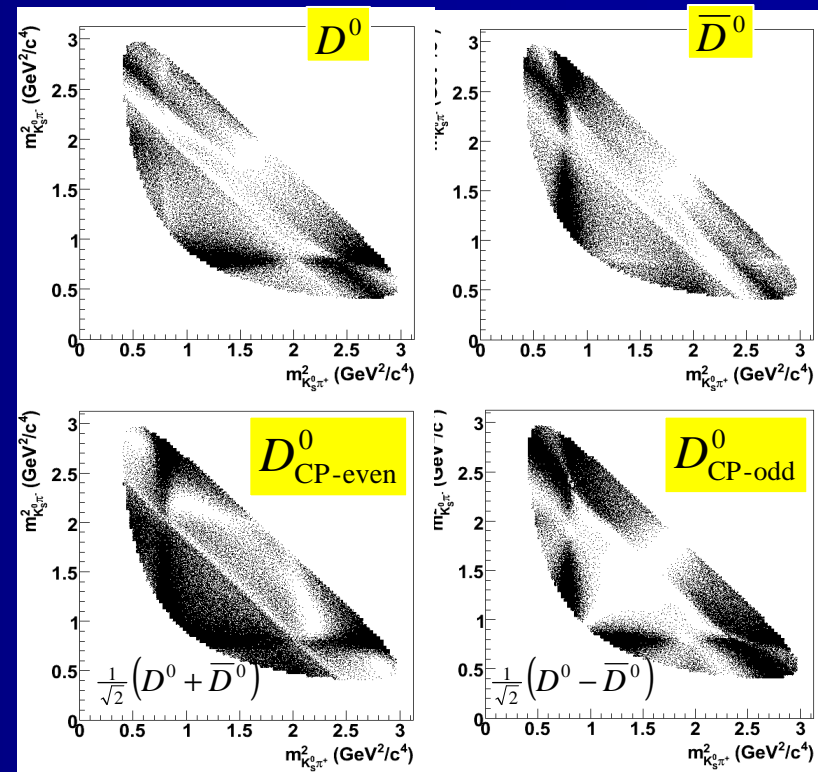
'Cartesian coordinates'



**Average cosine and sine of strong phase difference between  $D^0$  and  $\bar{D}^0$  decay amplitudes ( $\Delta\delta_D$ ) in this bin**

# Binned method continued

- Can determine  $s_i$  and  $c_i$  at the same time as extracting  $\gamma$ ,  $r_B$  and  $\delta_B$  from  $B$  data
  - $3 + N_{\text{bins}}$  free parameters ( $c_i = c_{-i}$  and  $s_i = -s_{-i}$ )
  - Huge loss in  $\gamma$  sensitivity not practical until you have  $O(10^6)$  events (2500/fb<sup>-1</sup> @ LHCb)
- However, **CP-correlated**  $e^+e^- \rightarrow \psi'' \rightarrow D^0 \bar{D}^0$  data where one decay is to  $K_S \pi \pi$  and the other decays to a CP eigenstate and  $K_S \pi \pi$  allows  $c_i$  and  $s_i$  to be determined, respectively





# Enter CLEO-c

CLEO is the grand-daddy of flavour physics, with history of achievement dating back over 25 years

Cornell University, Ithaca NY, USA

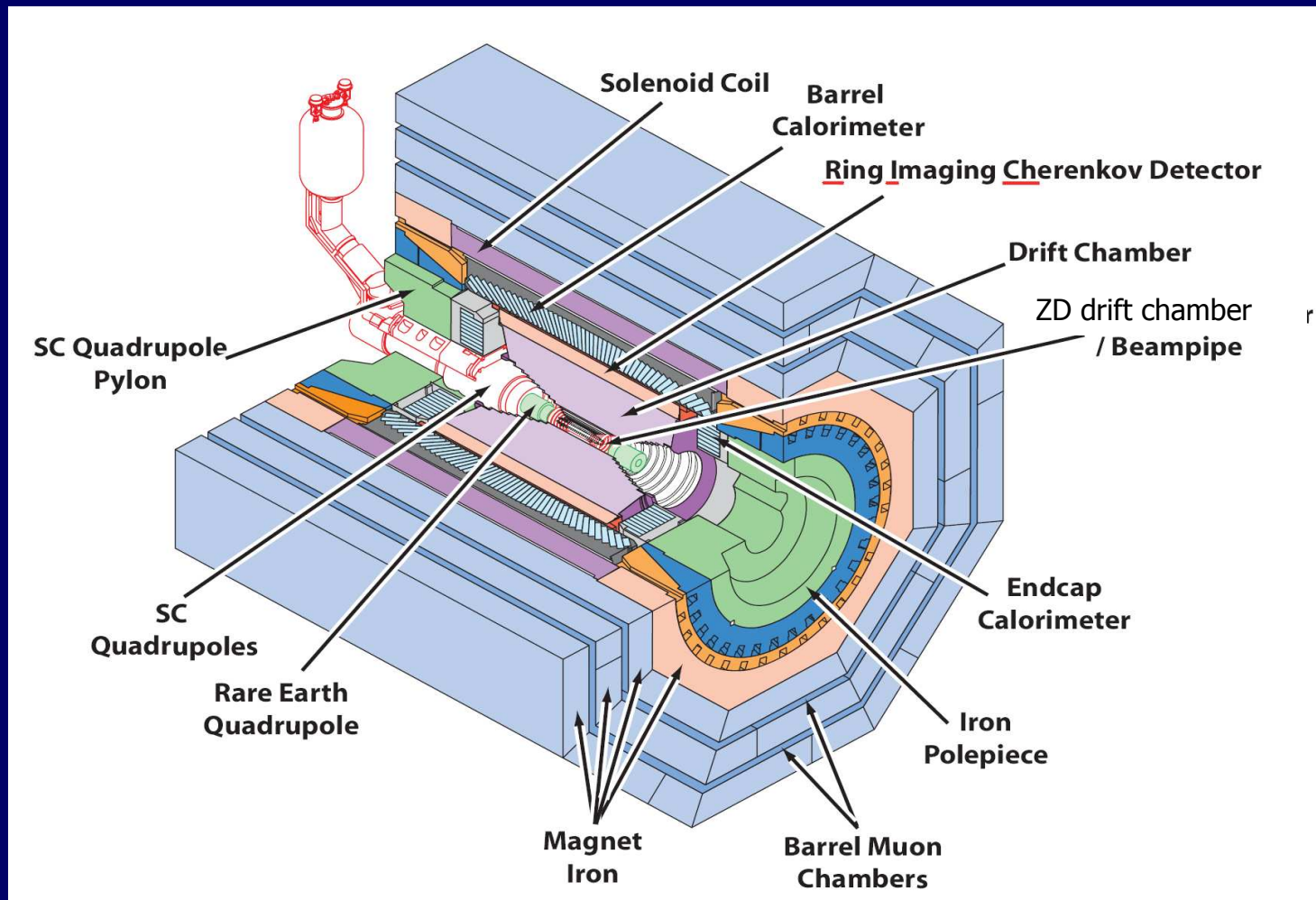
CLEO-c is latest incarnation.  
Dedicated programme of data-taking at and above the  $c\bar{c}$  threshold

**Important studies for LQCD and B physics**

**Oxford LHCb physicists (with Bristol) have joined CLEO-c in order to measure quantities essential for the  $\gamma$  studies**



# CLEO-c detector



# CLEO-c data samples

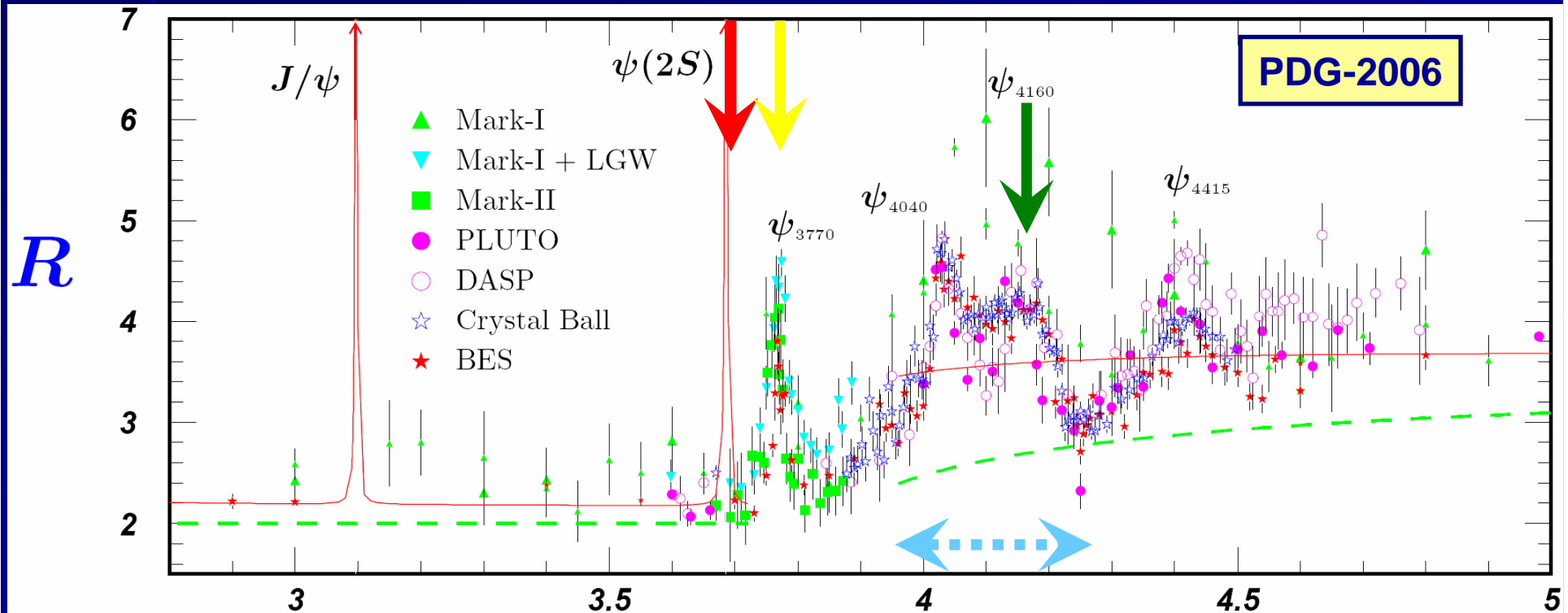
CLEO-c: Oct. 2003 – April Fool's Day 2008

**3686MeV**,  $54 \text{ pb}^{-1}$ ,  $N(\psi(2S)) \approx 27\text{M}$   $e^+e^- \rightarrow \psi(2S) \rightarrow \pi\pi J/\psi, \gamma\chi_c$  etc.

**3773MeV**,  $800 \text{ pb}^{-1}$  delivered,  $\sim 3$  million  $\psi(3770) \rightarrow D^0 \bar{D}^0$

**4170MeV**,  $195 \text{ pb}^{-1} \rightarrow \sim 300 \text{ pb}^{-1} \rightarrow \text{more} \rightarrow \sim 720 \text{ pb}^{-1}$ ,  $D_{(s)}^{(*)} \bar{D}_{(s)}^{(*)}$

**3970–4260MeV** energy scan,  $60 \text{ pb}^{-1}$  in 12 points

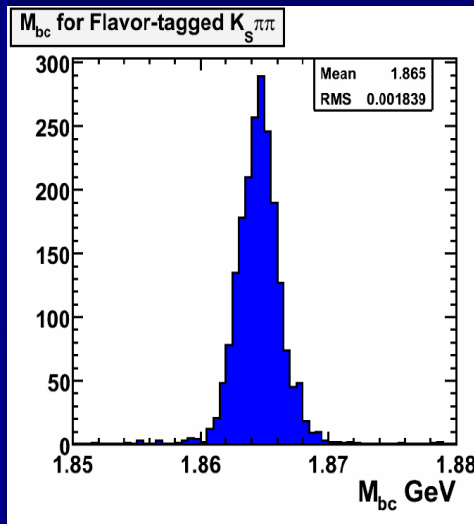
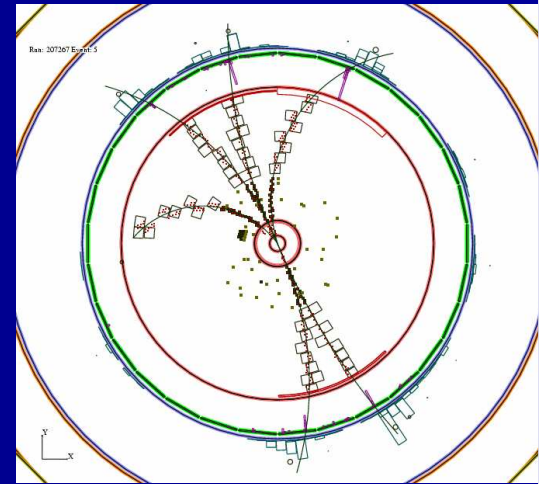


# CLEO-c: double tagged $\psi(3770)$ events

CLEO-c has collected  $\sim 800 \text{ fb}^{-1}$  at the  $\psi(3770)$   
 $D\bar{D}$  produced in quantum entangled state:

$$e^+e^- \rightarrow \psi'' \rightarrow \frac{1}{\sqrt{2}} [D^0\bar{D}^0 - \bar{D}^0D^0]$$

Reconstruct one D in decay of interest for  $\gamma$   
 analysis (eg.  $K\pi\pi$ ), & other in CP eigenstate  
 (eg.  $KK$ ,  $K_S\pi^0$  ...) then CP of other is fixed.

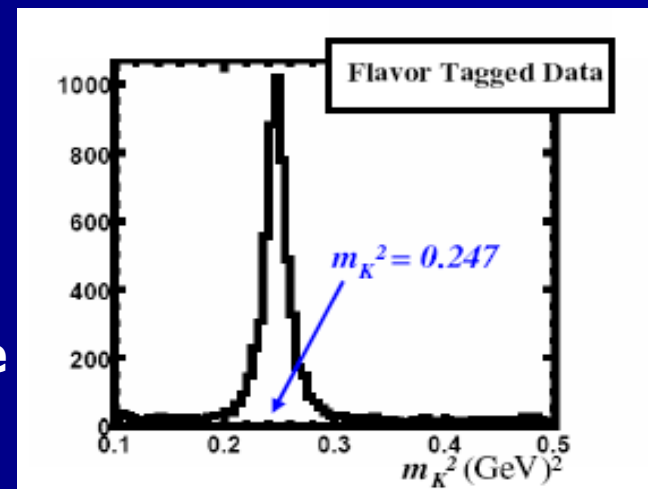


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← Almost  
 background free

Can use  $K_L \Rightarrow$

From talk by E. White  
 at Charm 07



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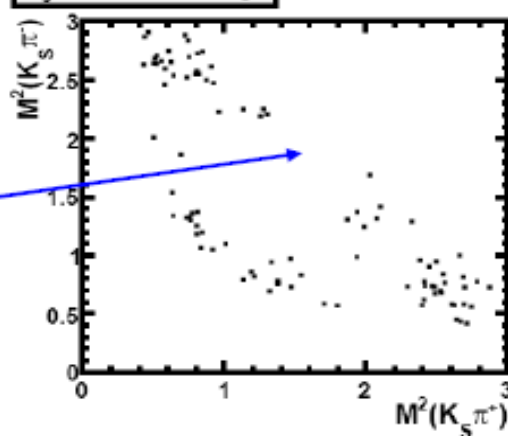
28

# CP-tagged $K_S\pi^+\pi^-$ - Dalitz Plots

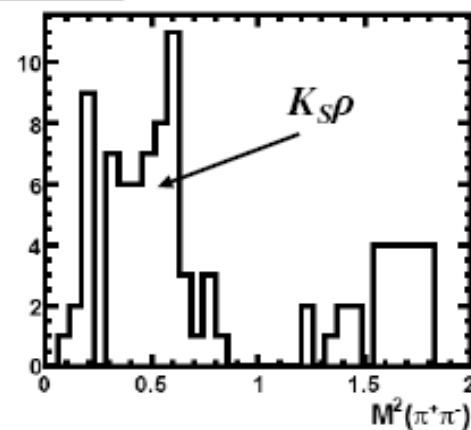
1/3 of total data  
( $<1/2$  the CP tags)

$K_S\rho^0$  resonance enhanced  
in CP-odd Dalitz plot

$K_S\pi\pi$  vs. CP-even Tags

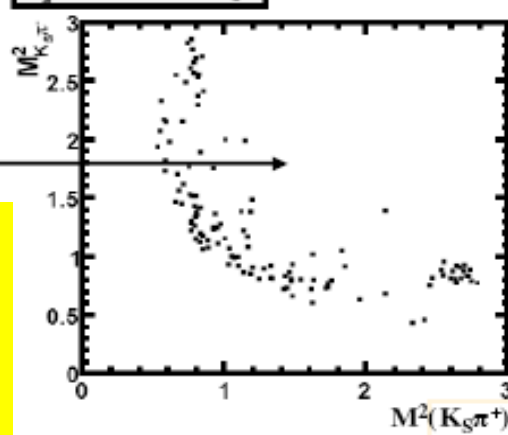


Z projection

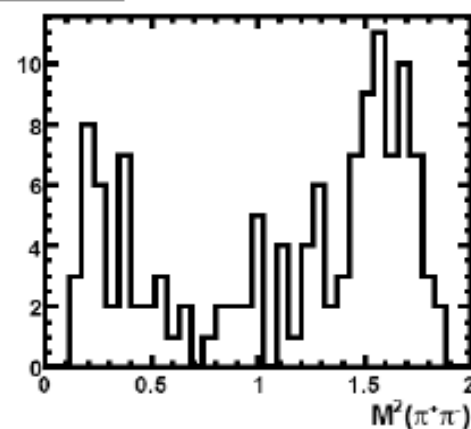


CP-odd  $K_S\rho^0$  resonance absent  
in CP-even Dalitz plot

$K_S\pi\pi$  vs. CP-odd Tags



Z projection

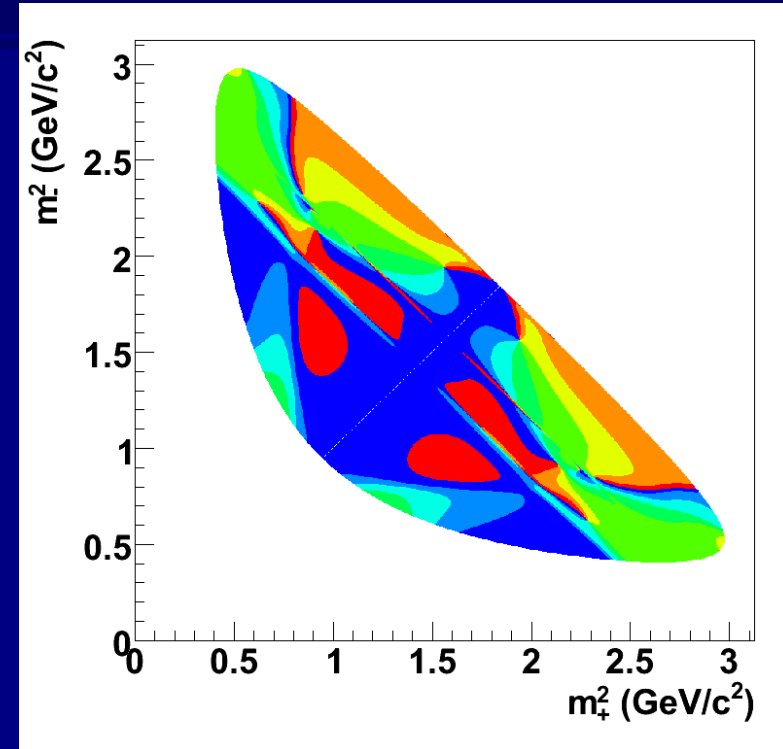


**Studies not complete  
but projected uncertainties  
on c and s will lead to  
3-5 degree uncertainty on  $\gamma$**

# Inkblot test

Absolute value of strong phase diff.  
(BABAR model used in LHCb-48-2007)

- Bondar and Poluektov show that the rectangular binning is far from optimal for both CLEOc and  $\gamma$  analyses
  - 16 uniform bins has only 60% of the B statistical sensitivity
  - c and s errors would be 3 times larger from the  $\psi''$
- Best B-data sensitivity **when  $\cos(\Delta\delta_D)$  and  $\sin(\Delta\delta_D)$  are as uniform as possible** within a bin



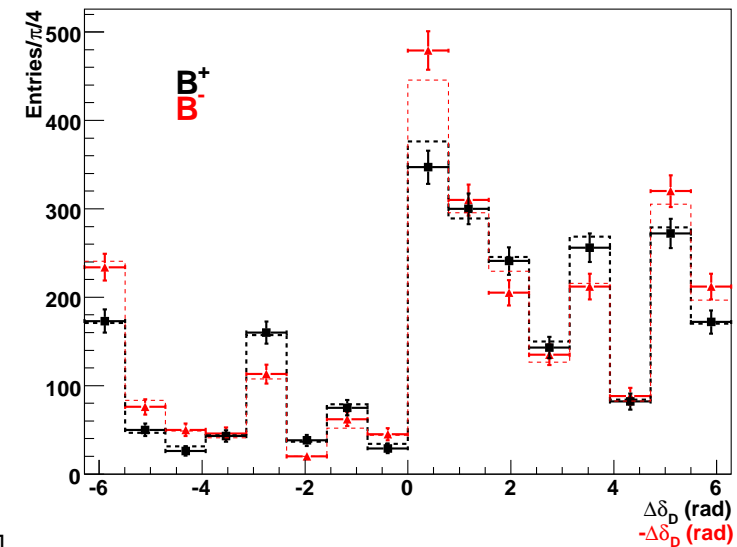
Good approximation and the binning that yields smallest s and c errors is equal  $\Delta\delta_D$  bins-80% of the unbinned precision

$$2\pi(i - \frac{1}{2}) / N < \Delta\delta_D(m_+^2, m_-^2) < 2\pi(i + \frac{1}{2}) / N$$

# Implementation at LHCb

( $\gamma=60^\circ$ ,  $r_B=0.1$  and  $\delta_B=130^\circ$ )

- Generate samples of  $B^\pm \rightarrow D(K_S^0 \pi^+ \pi^-) K^\pm$  with a mean of 5000 events split between the charges
- Bin according to strong phase difference,  $\Delta\delta_D \Rightarrow$
- Minimise  $\chi^2$



$$\chi^2 = \sum_{i=-8(i \neq 0)}^8 \left[ \frac{(n_i^+ - N_i^+(x_+, y_+, h))^2}{n_i^+} + \frac{(n_i^- - N_i^-(x_-, y_-, h))^2}{n_i^-} \right]$$

$n_i^\pm$  = number of  $B^\pm \rightarrow D(K_S^0 \pi^+ \pi^-) K^\pm$  events in  $i^{\text{th}}$  bin

$$N_i^\pm(x_\pm, y_\pm, h) = h \left[ K_{\pm i} + r_B^2 K_{\mp i} + 2\sqrt{K_i K_{-i}} (c_i x_\pm \pm s_i y_\pm) \right]$$

$h$  = normalization factor

$$K_{\pm i} = \int_{D_i} |f(m_+^2, m_-^2)|^2 dD \text{ [measured from flavour tag data]}$$

- $K_i$ ,  $c_i$  and  $s_i$  amplitudes calculated from model

- In reality from flavour tagged samples and CLEO-c

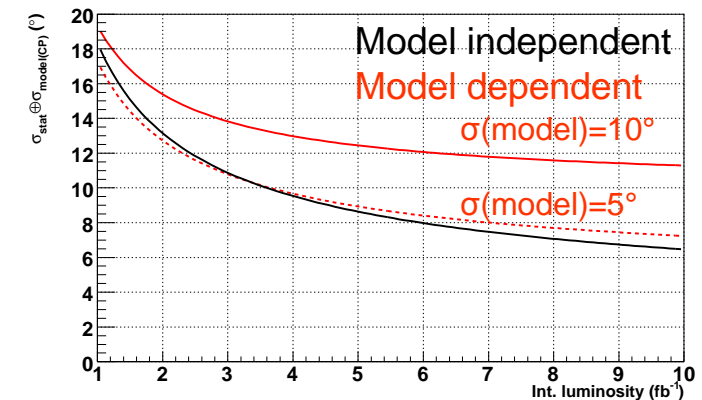
# $\gamma$ uncertainties with 5000 toy experiments

Scenario	2 fb <sup>-1</sup> Mod. Indep.	10 fb <sup>-1</sup> Mod. Indep.	2 fb <sup>-1</sup> Mod. Dep. (LHCb-048-2007)
No background	<b>7.9°</b>	<b>3.5°</b>	<b>5.9°</b>
Acceptance	<b>8.1°</b>	<b>3.5°</b>	<b>5.5°</b>
D $\pi$ (B/S = 0.24) (Best case scenario)	<b>8.8°</b>	<b>4.0°</b>	<b>7.3°</b>
DK <sub>comb</sub> (B/S=0.7) (Worst case scenario)	<b>12.8°</b>	<b>5.7°</b>	<b>11.7°</b>



# $B^\pm \rightarrow D(K^0_S \pi^+ \pi^-) K^\pm$ at LHCb

- Model independent fit with binning that yields smallest error from exploiting CLEO-c data
  - **Binning depends on model - only consequence of incorrect model is non-optimal binning and a loss of sensitivity**
- Measurement has no troublesome and hard-to-quantify systematic and outperforms model-dependent approach with full LHCb dataset with currently assigned model error
  - **$10 \text{ fb}^{-1}$  statistical uncertainty  $4\text{-}6^\circ$  depending on background**
- **CLEO-c measurements essential to validation of assumptions in model dependent measurement**
- LHCb-2007-141 – Available via CERN document server



# ADS

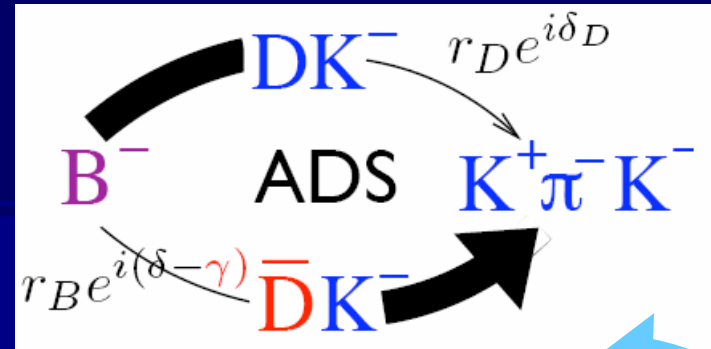
1st February 2008

UCL Seminar

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# ADS method

- Look at DCS and CF decays of D to rates that have enhanced



$$\Gamma(B^- \rightarrow (K^- \pi^+)_D K^-) \propto 1 + (r_B r_D^{K\pi})^2 + 2r_B r_D^{K\pi} \cos(\delta_B - \delta_D^{K\pi} - \gamma),$$

$$\Gamma(B^- \rightarrow (K^+ \pi^-)_D K^-) \propto r_B^2 + (r_D^{K\pi})^2 + 2r_B r_D^{K\pi} \cos(\delta_B + \delta_D^{K\pi} - \gamma),$$

$$\Gamma(B^+ \rightarrow (K^+ \pi^-)_D K^+) \propto 1 + (r_B r_D^{K\pi})^2 + 2r_B r_D^{K\pi} \cos(\delta_B - \delta_D^{K\pi} + \gamma),$$

$$\Gamma(B^+ \rightarrow (K^- \pi^+)_D K^+) \propto r_B^2 + (r_D^{K\pi})^2 + 2r_B r_D^{K\pi} \cos(\delta_B + \delta_D^{K\pi} + \gamma)$$

$$\Gamma(B^- \rightarrow (h^+ h^-)_D K^-) \propto 1 + r_B^2 + 2r_B \cos(\delta_B - \gamma)$$

$$\Gamma(B^+ \rightarrow (h^+ h^-)_D K^+) \propto 1 + r_B^2 + 2r_B \cos(\delta_B + \gamma)$$

h=π or K

- Unknowns :  $r_B \sim 0.1$ ,  $\delta_B$ ,  $\delta_D^{K\pi}$ ,  $\gamma$ ,  $N_{K\pi}$ ,  $N_{hh}$  ( $r_D = 0.06$  well measured)
- With knowledge of the relevant efficiencies and BRs, the normalisation constants ( $N_{K\pi}$ ,  $N_{hh}$ ) can be related to one another
- Important constraint from CLEOc  $\sigma(\cos \delta_D^{K\pi}) = 0.1 - 0.2$
- Overconstrained: 6 observables and 5 unknowns**

# Expected yields

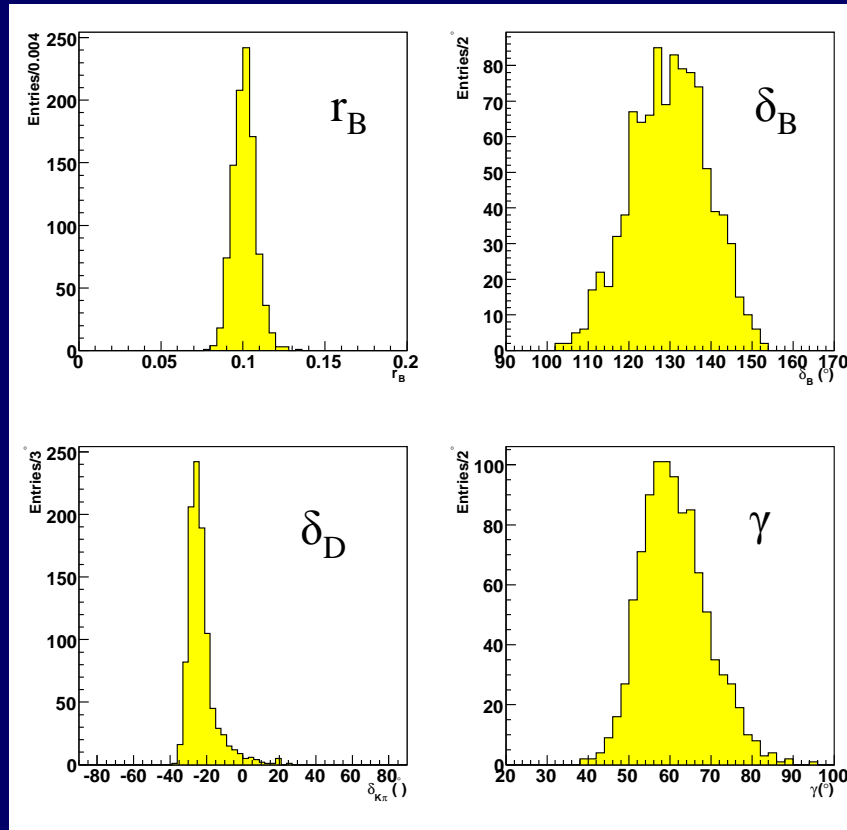
- ADS measurement is a counting experiment - but suppressed modes have  $\sim 10^{-7}$  BRs
  - Principal challenge background suppression
- Detailed selections studies as for Dalitz analysis
  - LHCb-2006-066

Channel	Signal yield/2 fb <sup>-1</sup>	B/S	B-factory yields ( $\sim 1/4$ final data set)
$B^{\pm} \rightarrow (K^{\pm} \pi^{\mp})_D K^{\pm}$	<b>56,000</b>	<b>0.6</b>	<b>4000</b>
$B^{\pm} \rightarrow (h^- h^+)_D K^{\pm}$	<b>8200</b>	<b>1.8</b>	<b>500</b>

- The suppressed modes have yields varying from 0 to 500 depending on the strong parameters
  - 780 background events predicted

# Sensitivity from 2-body

$\delta_D = -25^\circ$  – fit results from 1000 toy  $2 \text{ fb}^{-1}$  experiments :



$\delta_D$  constraint leads to  
a 0.5-1.0° reduction  
in  $\sigma_\gamma$

Also important for D  
mixing  
measurements

$\delta_D$ (°)	-25	-16.6	-8.3	0	8.3	16.6	25
$\sigma_\gamma$ (°)	9.5	8.6	7.5	8.6	8.6	9.3	9.4

# Four-body ADS

- $B \rightarrow D(K \pi \pi \pi) K$  can also be used for ADS style analysis
- Similar yields to 2-body – slightly worse B/S
  - LHCb-2007-004
- However, need to account for the resonant substructure in  $D \rightarrow K \pi \pi \pi$ 
  - made up of  $D \rightarrow K^* \rho, K^- a_1(1260)^+, \dots$
  - in principle each point in the phase space has a different strong phase associated with it - 3 and 4 body Dalitz plot analyses exploit this very fact to extract  $\gamma$  from amplitude fits
- Atwood and Soni (hep-ph/0304085) show how to modify the usual ADS equations for this case
  - Introduce **coherence parameter**  $R_{K3\pi}$  which dilutes interference term sensitive to  $\gamma$

$$\Gamma(B^- \rightarrow (K^+ \pi^- \pi^- \pi^+)_D K^-) \propto r_B^2 + (r_D^{K3\pi})^2 + 2r_B r_D^{K3\pi} R_{K3\pi} \cos(\delta_B + \delta_D^{K3\pi} - \gamma)$$

- $R_{K3\pi}$  ranges from
  - 1=coherent (dominated by a single mode) to
  - 0=incoherent (several significant components)
- Can slice and dice phase space to find most coherent regions

# Determining the coherence factor

- Measurements of the rate of  $K3\pi$  versus different tags at CLEO-c allows direct access to  $R_{K3\pi}$  and  $\delta_{K3\pi}$

1. Normalisation from CF  $K^-\pi^+\pi^+\pi^-$  vs.  $K^+\pi^-\pi^-\pi^+$  and  $K^-\pi^+\pi^+\pi^-$  vs.  $K^+\pi^-$

2. CP eigenstates:

$$\Gamma(K3\pi : CP\pm) = \Gamma_{K3\pi}^{CF} \Gamma_{CP} \left[ 1 + \left( r_D^{K3\pi} \right)^2 \mp 2 r_D^{K3\pi} R_{K3\pi} \cos \delta_D^{K3\pi} \right]$$

3.  $K^-\pi^+\pi^+\pi^-$  vs.  $K^-\pi^+\pi^+\pi^-$ :

$$\Gamma(K^-3\pi : K^-3\pi) = \Gamma_{K3\pi}^{CF} \Gamma_{K3\pi}^{DCS} \left[ 1 - R_{K3\pi}^2 \right]$$

4.  $K^-\pi^+\pi^+\pi^-$  vs.  $K^-\pi^+$ :

$$\Gamma(K^-3\pi : K^-\pi) \approx \Gamma_{K3\pi}^{CF} \Gamma_{K3\pi}^{DCS} \left[ 1 + \left( \frac{r_D^{K3\pi}}{r_D^{K\pi}} \right)^2 + 2 \frac{r_D^{K3\pi}}{r_D^{K\pi}} R_{K3\pi} \cos \delta_D^{K3\pi} \right]$$

K3π tag side	800 pb <sup>-1</sup> yield
K3π CF	4000
Kπ CF	5200
K3π/Kπ DCS	0-40 per mode
K <sup>0</sup> <sub>S</sub> π <sup>0</sup>	700
K <sup>+</sup> K <sup>-</sup>	500
π <sup>+</sup> π <sup>-</sup>	200

Assume  $\delta_D^{K\pi} \sim \pi$

$\sigma_{stat} \sim 0.1$  with 800 pb<sup>-1</sup>

# Conclusion-LHCb

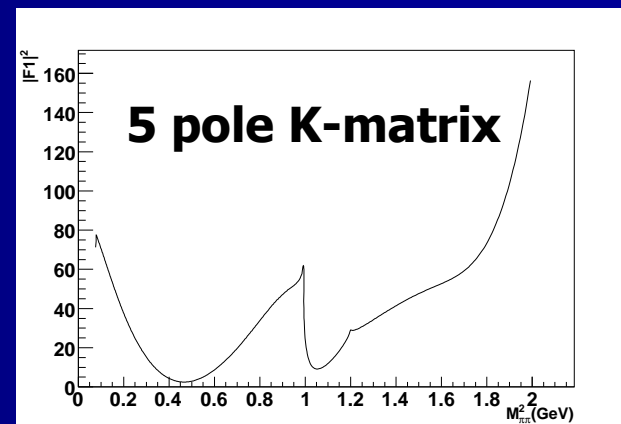
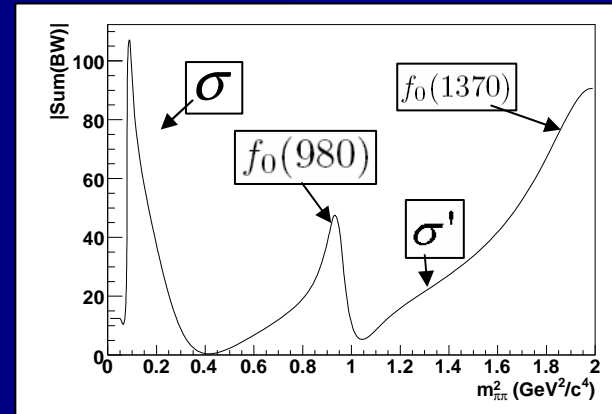
- LHCb has estimated  $2 \text{ fb}^{-1}$  sensitivity to  $\gamma$  in  $B^\pm \rightarrow DK^\pm$  with
  - $D \rightarrow K_S^0 \pi^+ \pi^-$  -  $\sigma_\gamma = 7-12^\circ$
  - $D \rightarrow K^- \pi^+$  and  $D \rightarrow h^+ h^-$  -  $\sigma_\gamma = 7.5-9.5^\circ$
  - $D \rightarrow K^- \pi^+ \pi^+ \pi^-$  will add additional information
- Not the whole story with theoretically clean measurements:
  - $B^0 \rightarrow DK^*$   $\sigma_\gamma \sim 9^\circ$  [LHCb-2007-050]
  - $B_s \rightarrow D_s K$   $\sigma_{\gamma+\phi_s} \sim 10^\circ$  [LHCb-2007-041]
- **CLEO-c measurements essential to fulfilling this goal**
- **Combined: a few degree precision on  $\gamma$  by the end of LHCb**
- Current world average:  $77 \pm 31^\circ$  (CKMfitter)



# Additional slides

# Aside: K-matrix

- Breit Wigner description of broad overlapping resonances violates unitarity and requires non-physical  $\sigma'$
- K-matrix description preserves unitarity
- First studies (Lauren Martin/JL) of LHCb  $\gamma$  fit with one K-matrix parameterisation of the  $\pi\pi$  S-wave
  - Difference between assuming K-matrix and BW model consistent with B-factory observations
  - Draft available from CPWG webpage
- Explore different physical K-matrix parameterisation to evaluate systematic rather than introduce  $\sigma'$   
**will reduce model uncertainty**

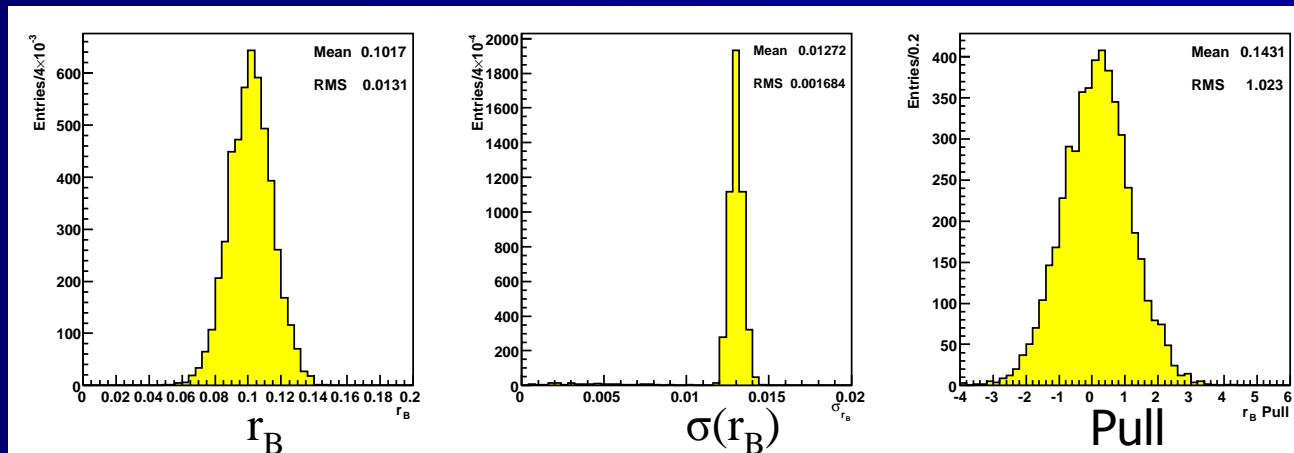
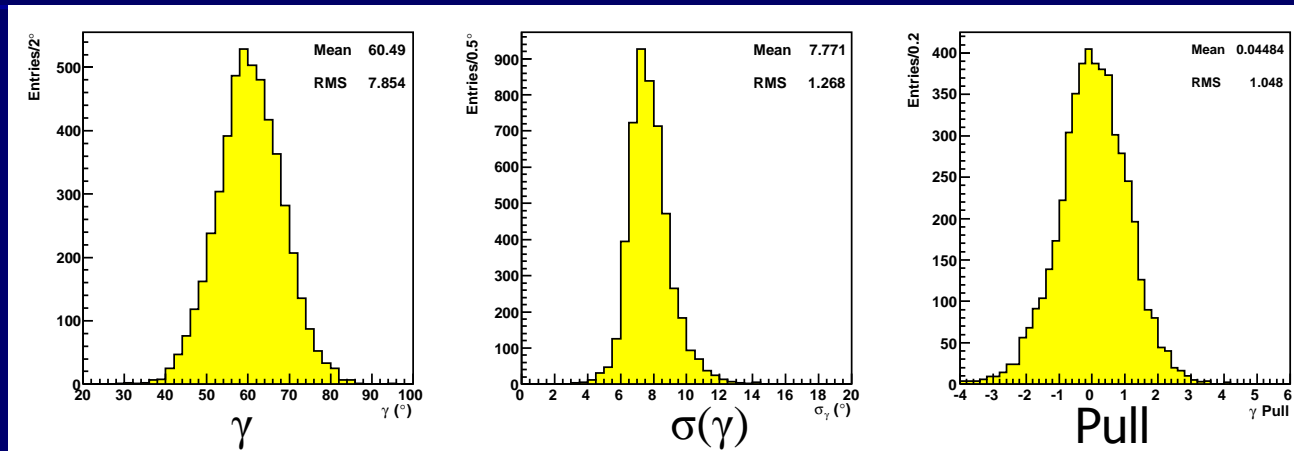


# No background with predicted $2 \text{ fb}^{-1}$ yield

5000 experiments

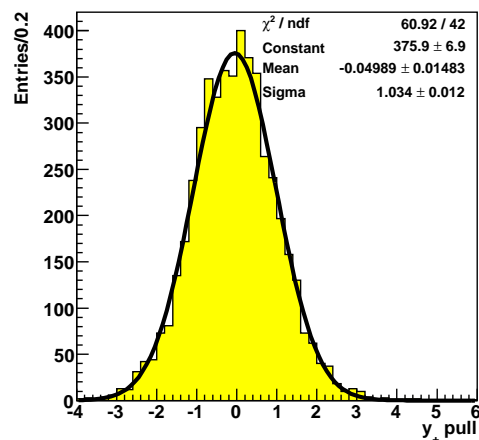
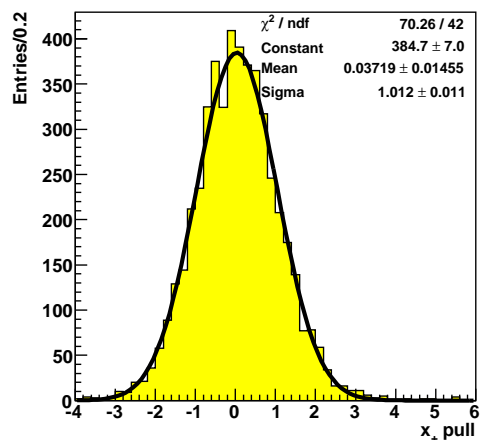
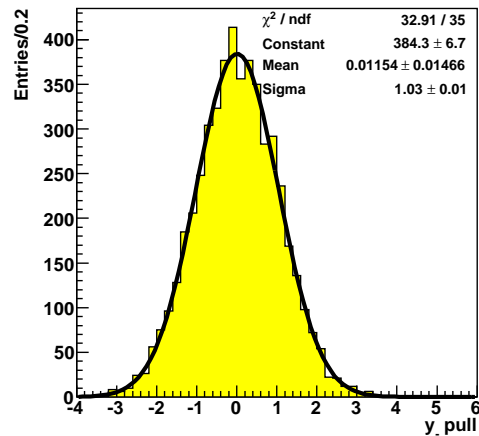
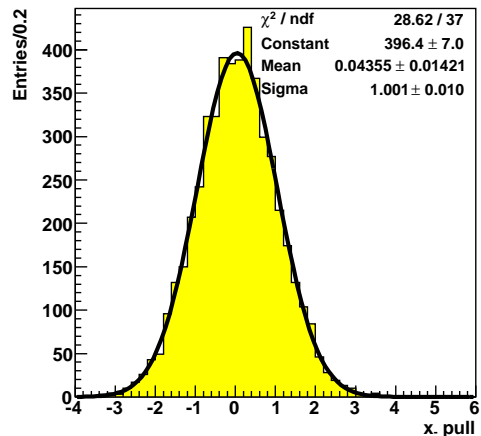
Input parameters

$\gamma=60^\circ$ ,  $r_B=0.1$  and  $\delta_B=130^\circ$



Model independent average uncertainty  $7.9^\circ$  (c.f. Model dependent  $5.9^\circ$ )

# No background with predicted $2 \text{ fb}^{-1}$ yield



5000 experiments

Input parameters

$\gamma=60^\circ$ ,  $r_B=0.1$  and  $\delta_B=130^\circ$

The four Cartesian coordinates and normalization are free parameters

All pulls are normal therefore calculate  $\gamma$ ,  $r_B$  and  $\delta_B$  with propagated Cartesian uncertainties

# Toy experiment results: $\gamma$ ( $2 \text{ fb}^{-1}$ )

Scenario	Mean	RMS	Mean $\sigma$	Mean pull	Pull RMS
No bck	$60.5 \pm 0.1$	7.9	7.8	$0.045 \pm 0.015$	1.05
Acc	$60.7 \pm 0.1$	8.1	7.8	$0.075 \pm 0.015$	1.07
D $\pi$	$60.7 \pm 0.1$	8.8	8.8	$0.088 \pm 0.015$	1.04
D $\pi$ + DK (B/S=0.7)	$60.7 \pm 0.2$	12.8	12.2	$0.049 \pm 0.016$	1.11
D $\pi$ + PS (B/S=0.7)	$60.8 \pm 0.2$	12.8	12.5	$0.064 \pm 0.015$	1.05
D $\pi$ + DK+ PS (50:50) (B/S=0.7)	$60.7 \pm 0.2$	12.7	12.6	$0.049 \pm 0.015$	1.04

# Toy experiment results: $\gamma$ ( $10 \text{ fb}^{-1}$ )

Scenario	Mean	RMS	Mean $\sigma$	Mean pull	Pull RMS
No bck	$60.17 \pm 0.05$	3.5	3.4	$0.050 \pm 0.015$	1.03
Acc	$60.13 \pm 0.05$	3.5	3.4	$0.036 \pm 0.015$	1.01
$D\pi$	$60.22 \pm 0.06$	4.0	3.9	$0.054 \pm 0.015$	1.03
$D\pi + DK$ (B/S=0.7)	$60.18 \pm 0.08$	5.7	5.7	$0.030 \pm 0.015$	1.01
$D\pi + PS$ (B/S=0.7)	$60.26 \pm 0.08$	5.5	5.5	$0.045 \pm 0.015$	1.00
$D\pi + DK + PS$ (50:50) (B/S=0.7)	$60.22 \pm 0.08$	5.4	5.6	$0.038 \pm 0.015$	0.97

# Toy experiment results: $r_B$ ( $2 \text{ fb}^{-1}$ )

Scenario	Mean	RMS	Mean $\sigma$	Mean pull	Pull RMS
No bck	$0.1017 \pm 0.0002$	0.013	0.013	$0.143 \pm 0.015$	1.02
Acc	$0.1017 \pm 0.0002$	0.014	0.013	$0.175 \pm 0.016$	1.13
$D\pi$	$0.1015 \pm 0.0002$	0.014	0.014	$0.123 \pm 0.015$	1.02
$D\pi + DK$ (B/S=0.7)	$0.1031 \pm 0.0003$	0.020	0.020	$0.215 \pm 0.016$	1.16
$D\pi + PS$ (B/S=0.7)	$0.1035 \pm 0.0003$	0.020	0.019	$0.175 \pm 0.015$	0.99
$D\pi + DK + PS$ (50:50) (B/S=0.7)	$0.1038 \pm 0.0003$	0.020	0.020	$0.186 \pm 0.015$	0.98

# Toy experiment results: $r_B$ ( $10 \text{ fb}^{-1}$ )

Scenario	Mean	RMS	Mean $\sigma$	Mean pull	Pull RMS
No bck	$0.1003 \pm 0.0001$	0.006	0.006	$0.056 \pm 0.015$	1.00
Acc	$0.1003 \pm 0.0001$	0.006	0.006	$0.051 \pm 0.015$	1.01
$D\pi$	$0.1003 \pm 0.0001$	0.006	0.006	$0.049 \pm 0.015$	0.98
$D\pi + DK$ (B/S=0.7)	$0.1009 \pm 0.0001$	0.009	0.009	$0.101 \pm 0.015$	0.97
$D\pi + PS$ (B/S=0.7)	$0.1008 \pm 0.0001$	0.009	0.009	$0.093 \pm 0.015$	0.99
$D\pi + DK + PS$ (50:50) (B/S=0.7)	$0.1007 \pm 0.0001$	0.009	0.009	$0.077 \pm 0.015$	0.98



# Acceptance

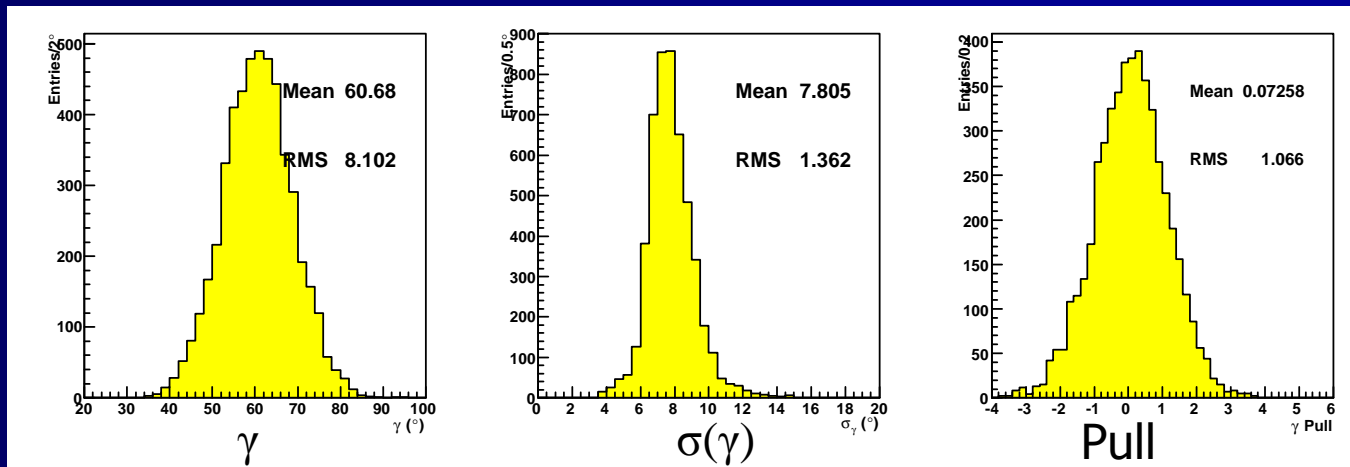
- Acceptance in each bin calculated as a weighted average of the acceptance function used for model dependent studies
  - 15% relative difference amongst bins
- Modifies the fit function:

Can be calculated from  $D\pi$

$$N_i^\pm(x_\pm, y_\pm, h) = h \varepsilon_{\pm i} \left[ K_{\pm i} + r_B^2 K_{\mp i} + 2\sqrt{K_i K_{-i}} (c_i x_\pm \pm s_i y_\pm) \right]$$

$$\varepsilon_i = \frac{\int_{D_i} |f(m_+^2, m_-^2)|^2 \varepsilon(m_+^2, m_-^2) dD}{K_i} \quad \text{where } \varepsilon(m_+^2, m_-^2) = 0.28 \times 10^{-3} (1 - 0.08(m_+^2 + m_-^2))$$

- Average  $\gamma$  uncertainty increases to  $8.1^\circ$



# Background

- 3 types of background to consider
  - $B \rightarrow D(K_S \pi \pi) \pi$  ( $B/S = 0.24$ )
    - $r_B(D\pi) \sim O(10^{-3})$  so Dalitz plots are like  $D^0$  and  $\bar{D}^0$  for  $B^-$  and  $B^+$ , respectively
  - Combinatoric ( $B/S < 0.7$ )-mixtures of two types considered
    1.  $DK_{\text{comb}}$ : real  $D \rightarrow D(K_S \pi \pi)$  combined with a bachelor  $K$ 
      - Dalitz plot an even sum of  $D^0$  and  $\bar{D}^0$  decays
    2.  $PS_{\text{comb}}$ : combinatoric  $D$  with a bachelor  $K$ 
      - Follows phase space
- Integrate background PDFs used in model-dependent analysis over each bin, then scaled to background level assumed:

$$N(D\pi)_i^\pm \propto \epsilon_{\pm i} K_{\pm i}$$

$$N(DK_{\text{comb}})_i^\pm \propto \frac{1}{2} (\epsilon_{\pm i} K_{\pm i} + \epsilon_{\mp i} K_{\mp i})$$

$$N(PS_{\text{comb}})_i^\pm \propto P_i$$

fractional area of Dalitz space covered by bin

# Systematic related to acceptance

- The acceptance varies over the Dalitz plane
- The relative acceptance in each bin can be measured using the  $B \rightarrow D\pi$  control sample with DK selection applied without bachelor K PID

$$\mathcal{E}_i = \frac{\int_{D_i} |f(m_+^2, m_-^2)|^2 \mathcal{E}(m_+^2, m_-^2) dD}{K_i} \propto \frac{N(B \rightarrow D(K_S^0 \pi \pi) \pi)_i}{K_i}$$

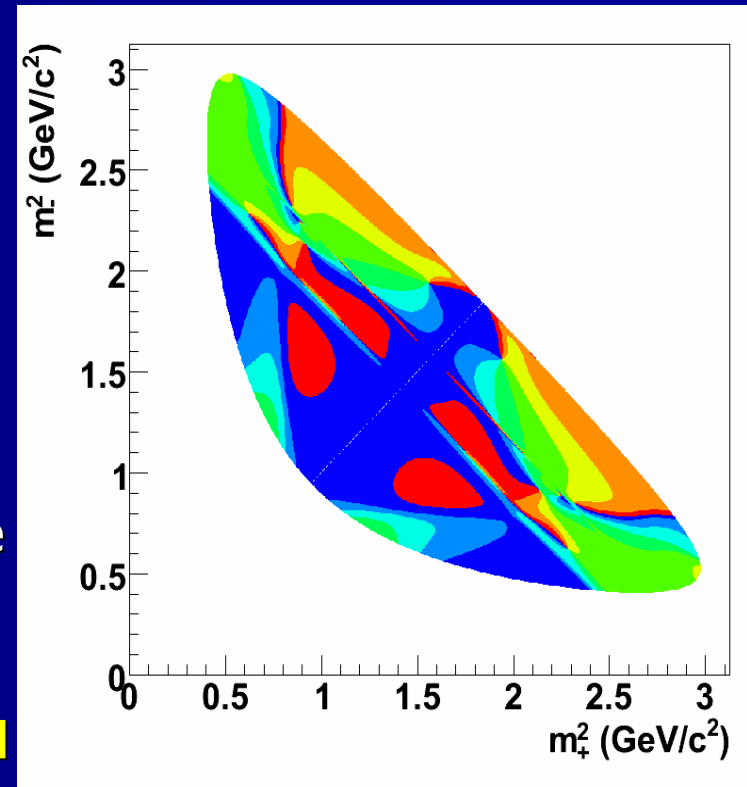
- With the DC04 selection expect 60k events/2 fb<sup>-1</sup>
  - Relative relative-efficiency uncertainty 1-4%/Δδ<sub>D</sub> bin with 2 fb<sup>-1</sup>
  - Increased statistics reduces error
- Toy MC study smearing bin efficiencies in event generation by this amount leads to an additional 1° uncertainty without background and **3.2° uncertainty** with DK<sub>comb</sub> B/S=0.7
  - **Small effect compared to statistical uncertainty**
- NB: the efficiency related to the PID of the bachelor π/K can be factored out and will be determined from the D\*<sup>\*</sup>→D(Kπ)π data to better than one percent-ignore at present

# Asymmetry in efficiency in Dalitz space

- Considered charge asymmetries in the efficiency across the Dalitz plane
  - $\varepsilon(m^2_+, m^2_-) \neq \varepsilon(m^2_-, m^2_+)$
- Generated with the efficiency biased relative to one another depending on whether the event had  $m^2_+ > m^2_-$  or  $m^2_+ < m^2_-$
- **Maximum bias on  $\gamma$  induced was  $<1^\circ$  for 10% relative effect and full background**
- 10% effects would be evident in the  $D\pi$  sample

# Resolution

- $\Delta\delta_D$  binning has some narrow regions in Dalitz space
- Investigation of how resolution on the Dalitz variables might affected the extraction of  $\gamma$
- 10  $\text{MeV}^2/c^4$  resolution (DC04) on Dalitz variables and generated toy experiments with this smearing
- Found that this led to a few bins with largest (red) and smallest (dark blue) phase difference having a 2-3% relative changes in expected yields due to resolution induced migration
- **Fit results on toy experiments where resolution included in generation but ignored in fit found no significant bias ( $<0.5^\circ$ ) on  $\gamma$**



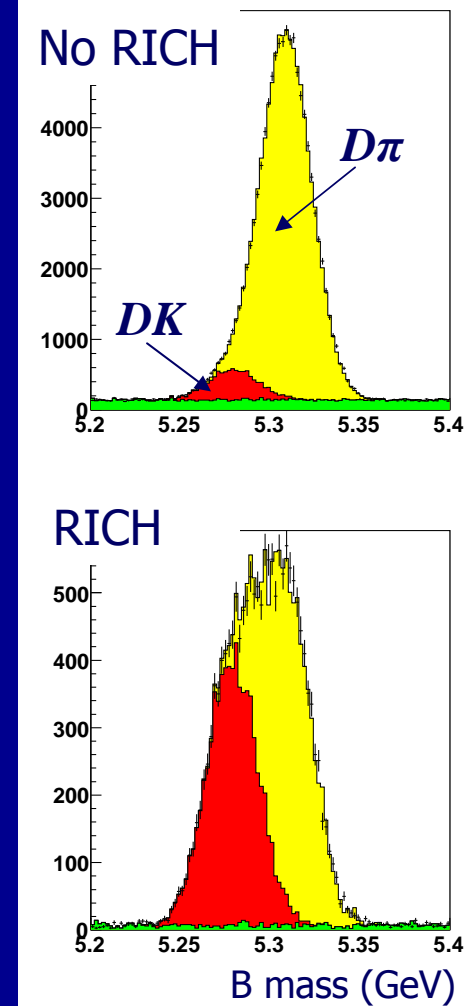
# Background fractions

- Combinatoric background rate will be determined from  $B$  and  $D$  mass sidebands which will cover at least 2-3 times the area of the signal region
  - Use 10 $\times$  in DC04 background studies but this will probably be unrealistic with data
- If background distributions relatively flat in masses one can estimate that this leads to B/S will be determined absolutely to around 0.01 or better
  - **Toy studies suggest that there is no impact on  $\gamma$  precision with this kind of uncertainty**
- Maybe complications depending on Dalitz space distribution of the PS background but can only speculate until we have the data in hand

# Background composition

0.5 fb<sup>-1</sup>

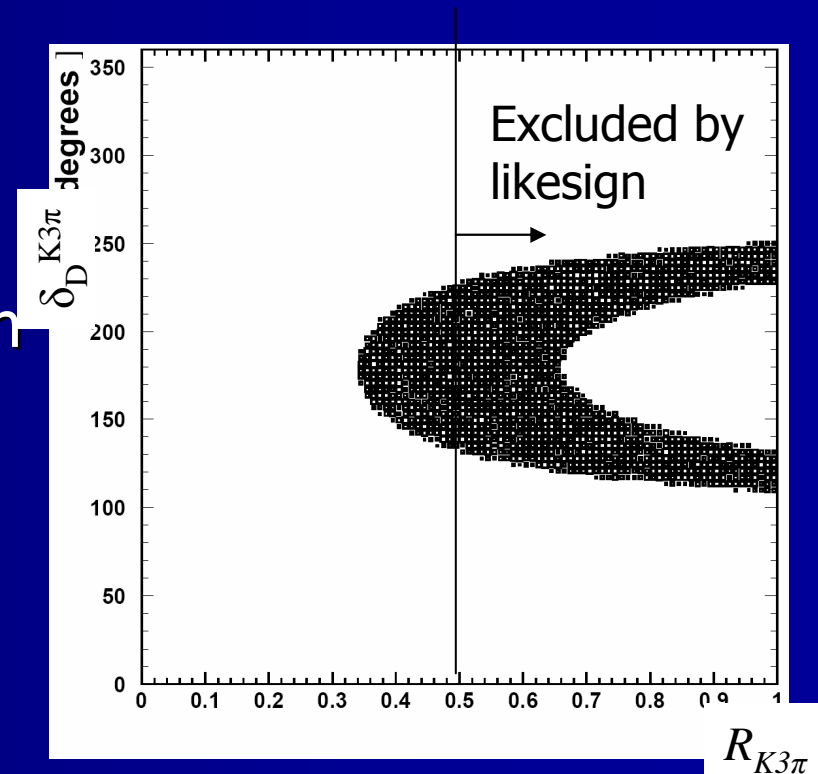
- For favoured mode background dominated by  $B \rightarrow D\pi$ 
  - 14 × larger BF
  - Power of the RICH
- For suppressed combinatoric dominates (green)
- For  $B \rightarrow D(hh)K$  more even mixture of comb. and  $D\pi$ 
  - $B \rightarrow D(KK)K$  has significant non-resonant  $B \rightarrow KKK$  component



# Determining the coherence factor

- Analysis underway 10% effects in CP modes so great care with
  - Background subtraction
  - Efficiency calculation
- Estimate of current sensitivity with the addition of  $K_L^0 \pi^0$  and further CP tags i.e.  $K_S^0 \eta$  to be added
- Further information in mixed CP SCS tags such as  $K_S^0 \pi^+ \pi^-$

$$\sigma_{stat} \sim 0.1 \text{ with } 800 \text{ pb}^{-1}$$





# Conclusion CLEOc

- **CLEO-c measurements essential to fulfilling this goal**
- **But there is much more that can be done**
- Full amplitude analysis of 4-body should yield ultimate precision
  - Need DCS model, which can be accessed via CP tags at CLEOc
  - Also will guide division of phase space for binned coherence factor analysis
- Other modes that can be used:
  - $D \rightarrow K^- \pi^+ \pi^0$  (Coherence analysis underway)
  - $D \rightarrow K_S^0 K^+ K^-$  and  $D \rightarrow K_S^0 K^+ \pi^-$
  - $D \rightarrow K^- K^+ \pi^+ \pi^-$  and  $D \rightarrow K_S^0 \pi^- \pi^+ \pi^0$