

The Mass of the W Boson (and, maybe, a few other selected topics)

Dave Waters

on behalf of the UCL-CDF group :

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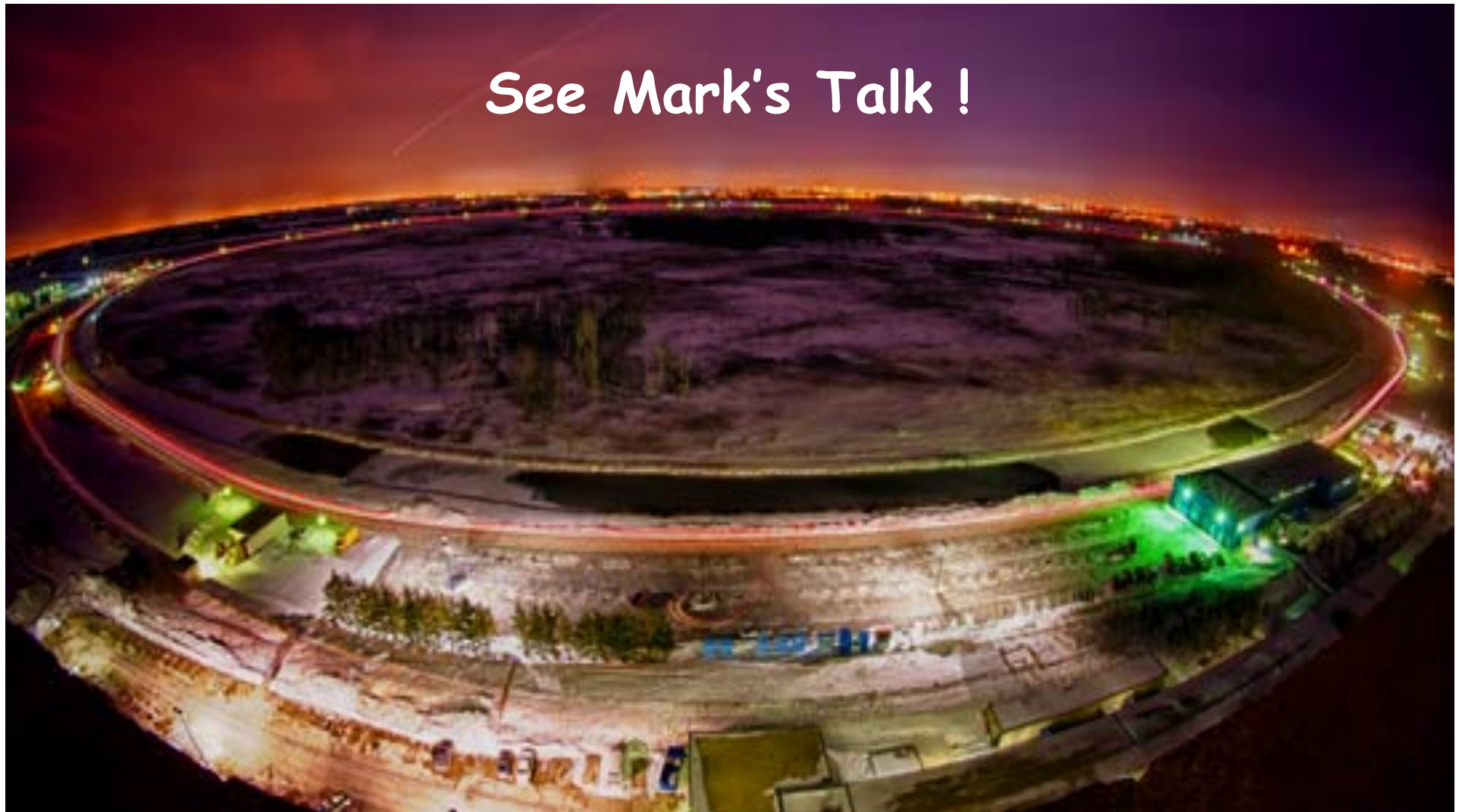


Tevatron Run II



1st March 2001 – 30th September 2011

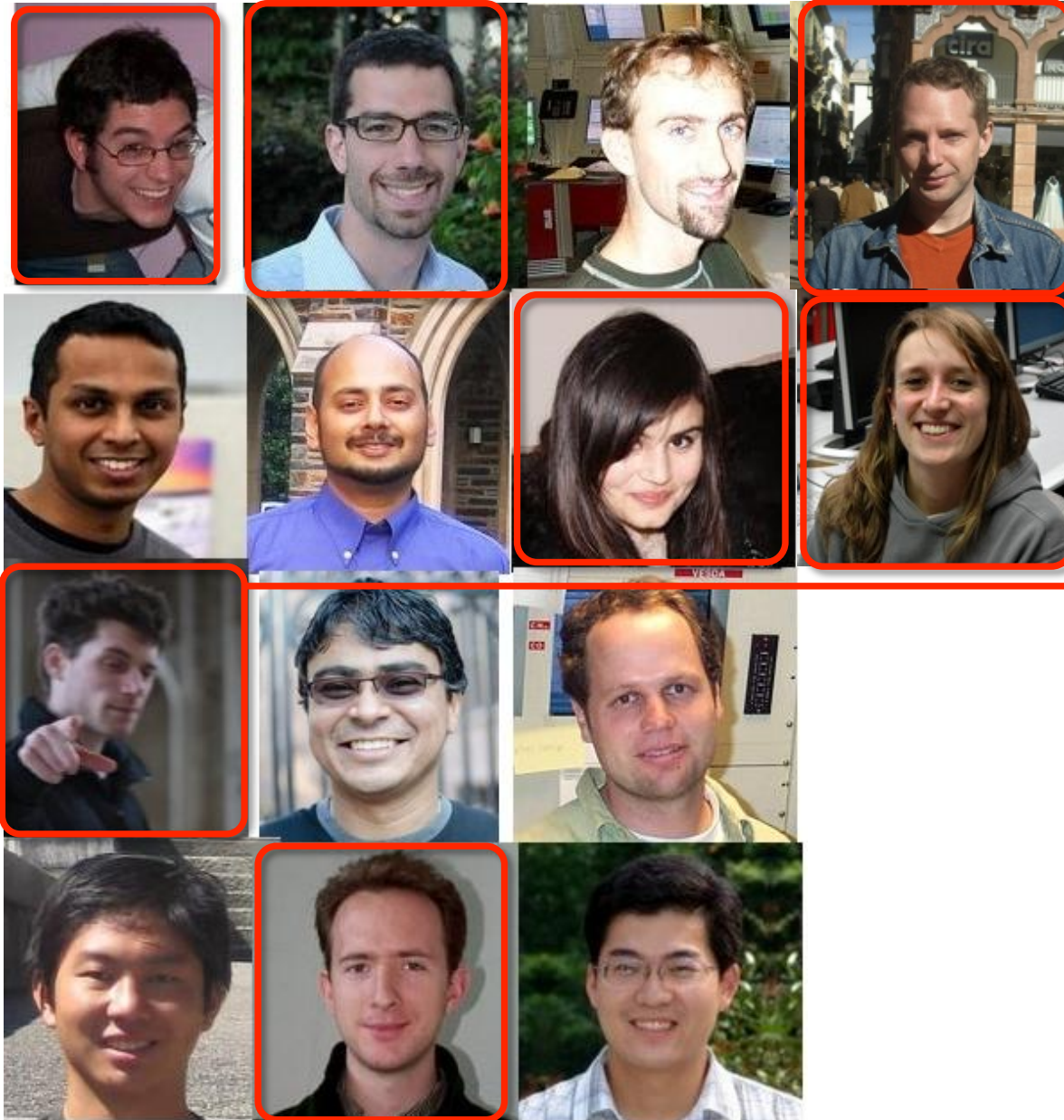
- ▶ 12 fb⁻¹ delivered to CDF and DØ → ~10 fb⁻¹ good data on tape.







W Mass





W Width





How Well do we Know our Forces ?



Force	Carrier	Mass	Lifetime
EM	Photon	$< 10^{-16}$ eV	stable
Strong	Gluon	$< \text{few MeV}$	stable
Weak NC	Z^0	91.1876 ± 0.0021 GeV	$1/\tau = 2.4952 \pm 0.0023$ GeV
Weak CC	W^\pm	80.399 ± 0.023 GeV	$1/\tau = 2.085 \pm 0.042$ GeV (directly measured : UCL CDF 2008)

2011

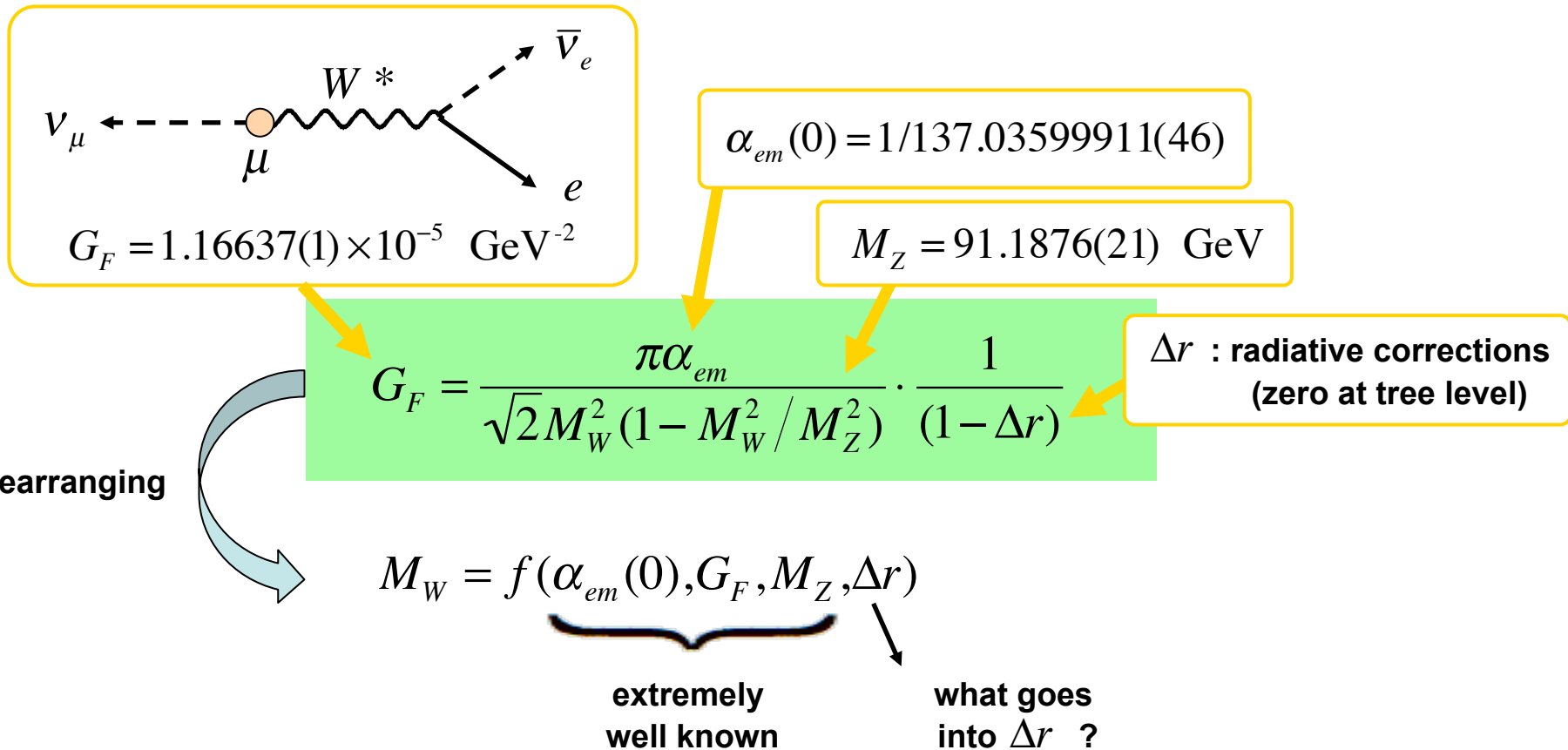
$$\frac{\Delta M_W}{M_W} / \frac{\Delta M_Z}{M_Z} \approx 12 \qquad \frac{\Delta \Gamma_W}{\Gamma_W} / \frac{\Delta \Gamma_Z}{\Gamma_Z} \approx 22$$



EWK Precision Measurements : Big Picture



- Electroweak standard model relates precisely known parameters and less well known parameters through radiative corrections :

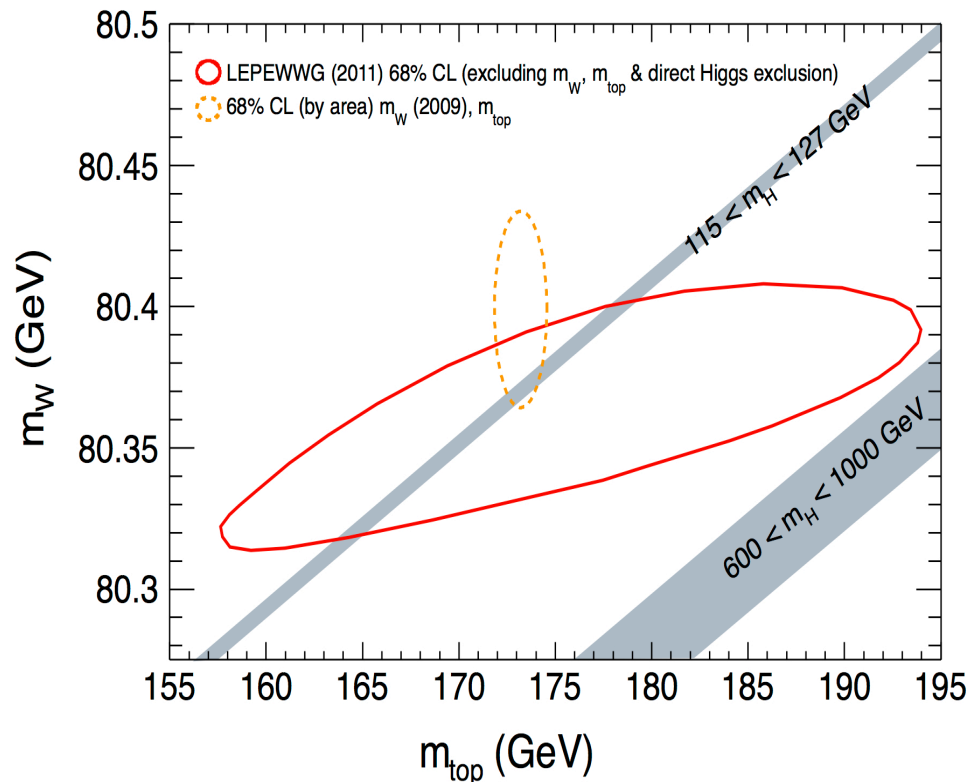


- Radiative corrections to M_W include those due to **top** and **Higgs** :

$$\Delta M_W \propto M_{top}^2$$

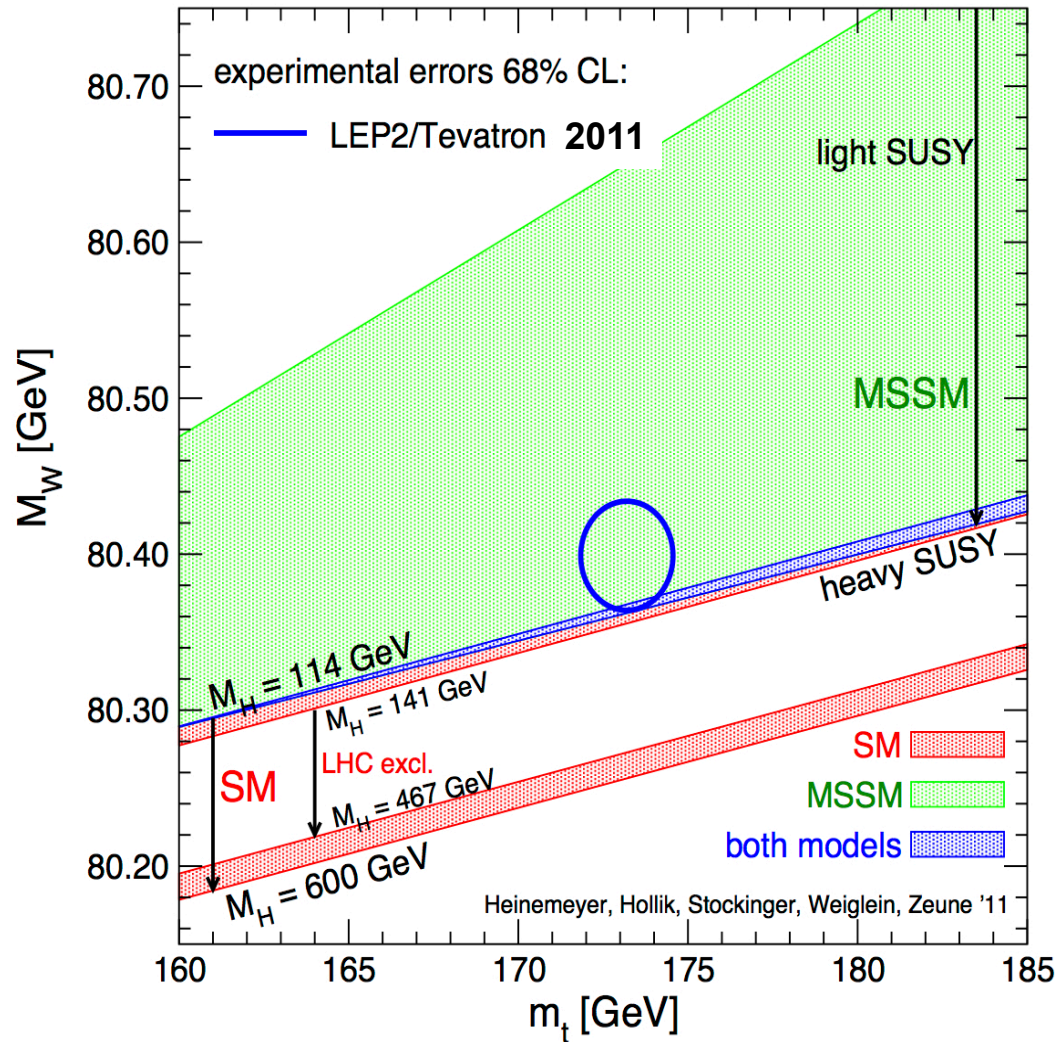
$$\Delta M_W \propto \ln M_H$$

- Equivalently, measuring M_W and M_{top} places constraints on the missing piece, M_H .



$$M_H = 92^{+34}_{-26} \text{ GeV} \quad (\text{LEP EWWG, 2011})$$

- How do M_W and M_{top} inputs compare ?
- Current top mass precision :
 $\Delta(M_{TOP}) = 0.9 \text{ GeV} \text{ (0.54\%)}$
- Equivalent constraint on M_H would come from:
 $\Delta(M_W) = 6 \text{ MeV} \text{ (0.001\%)}$
- The most important measurement for us to improve now is the W mass !

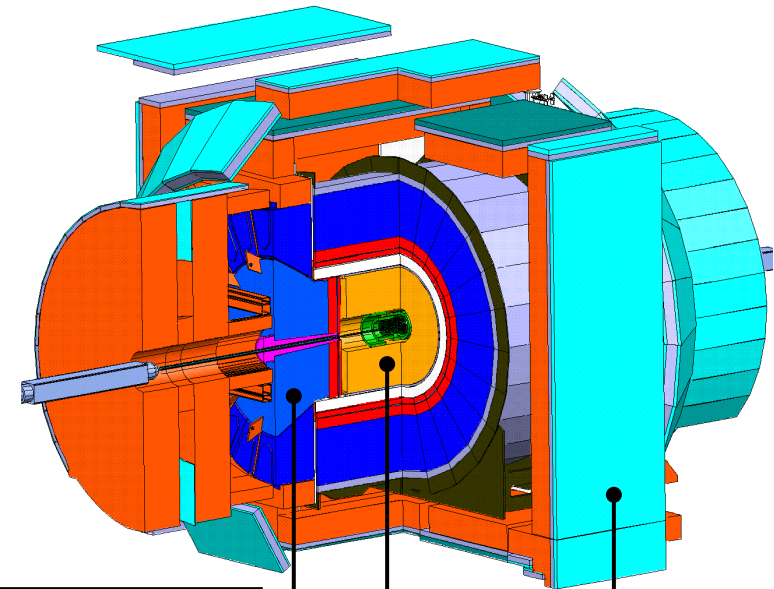
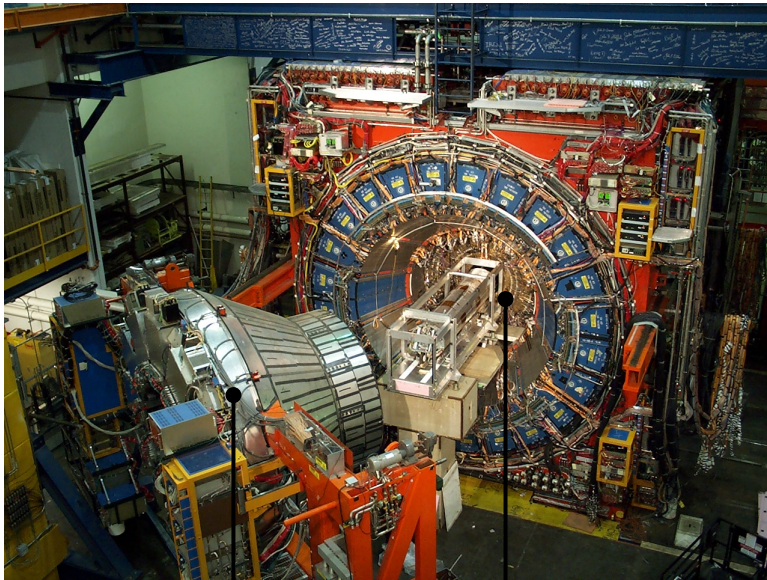


- Even after a Higgs discovery at the LHC, precision EWK measurements will enable powerful Standard Model consistency fits.
- May be possible to distinguish SM from MSSM and in general constrain the properties of new physics at higher mass scales.





CDF Detector



Drift chamber outer tracker :

$$\delta p_T / p_T \approx 0.0005 \times p_T \quad [\text{GeV}/c; \text{beam constrained}]; \quad |\eta| < 1$$

Silicon vertex detector :

tracking coverage out to $|\eta| < 2.8$

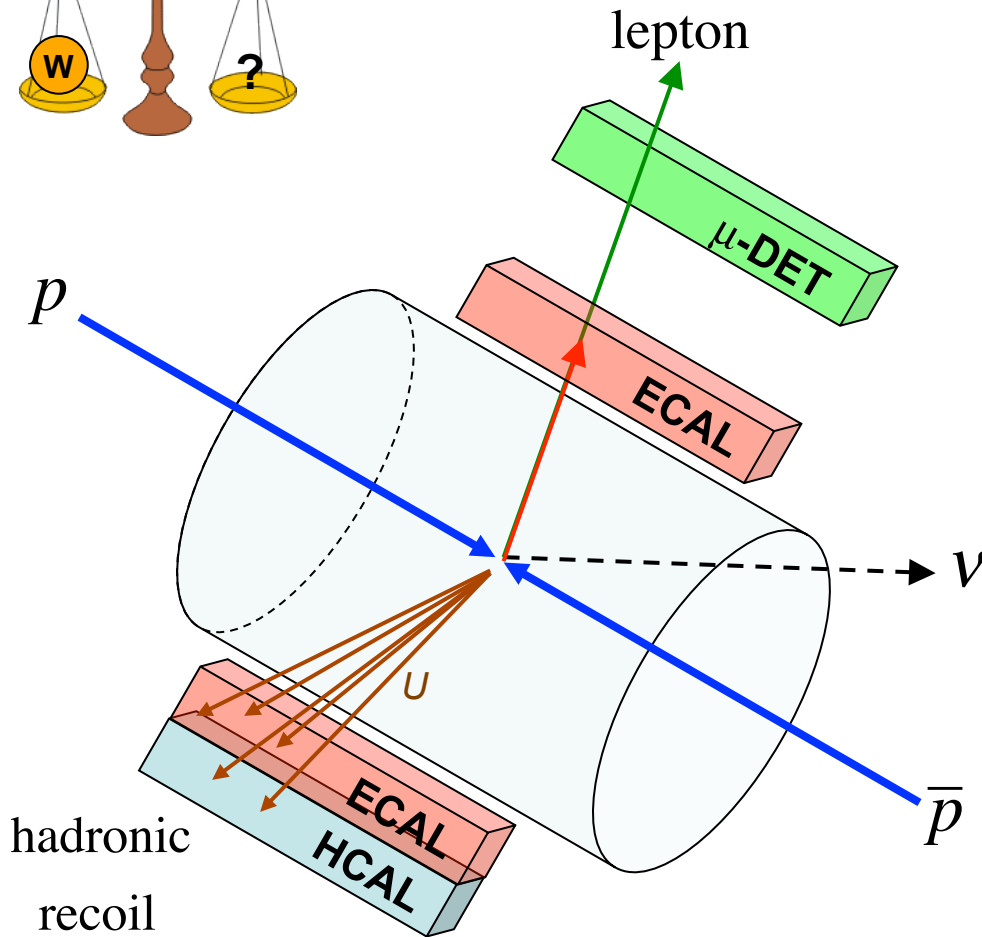
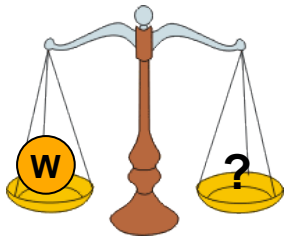
Central calorimeter : $\delta E_T / E_T \approx 13.5\% / \sqrt{E_T} \oplus 1.5\% \quad |\eta| < 1.1$

Plug calorimeter : coverage out to $|\eta| < 3.0$

Muon chambers : coverage out to $|\eta| < 1.0$



W Mass : Observables



$$p\bar{p} \rightarrow W (\rightarrow l\nu) + X$$

Lepton :

Measure 4-vector as precisely as possible.

Hadronic Recoil :

Measure in transverse plane only

$$\vec{u}_T = \{u_x, u_y\}$$

Neutrino :

Infer transverse momentum :

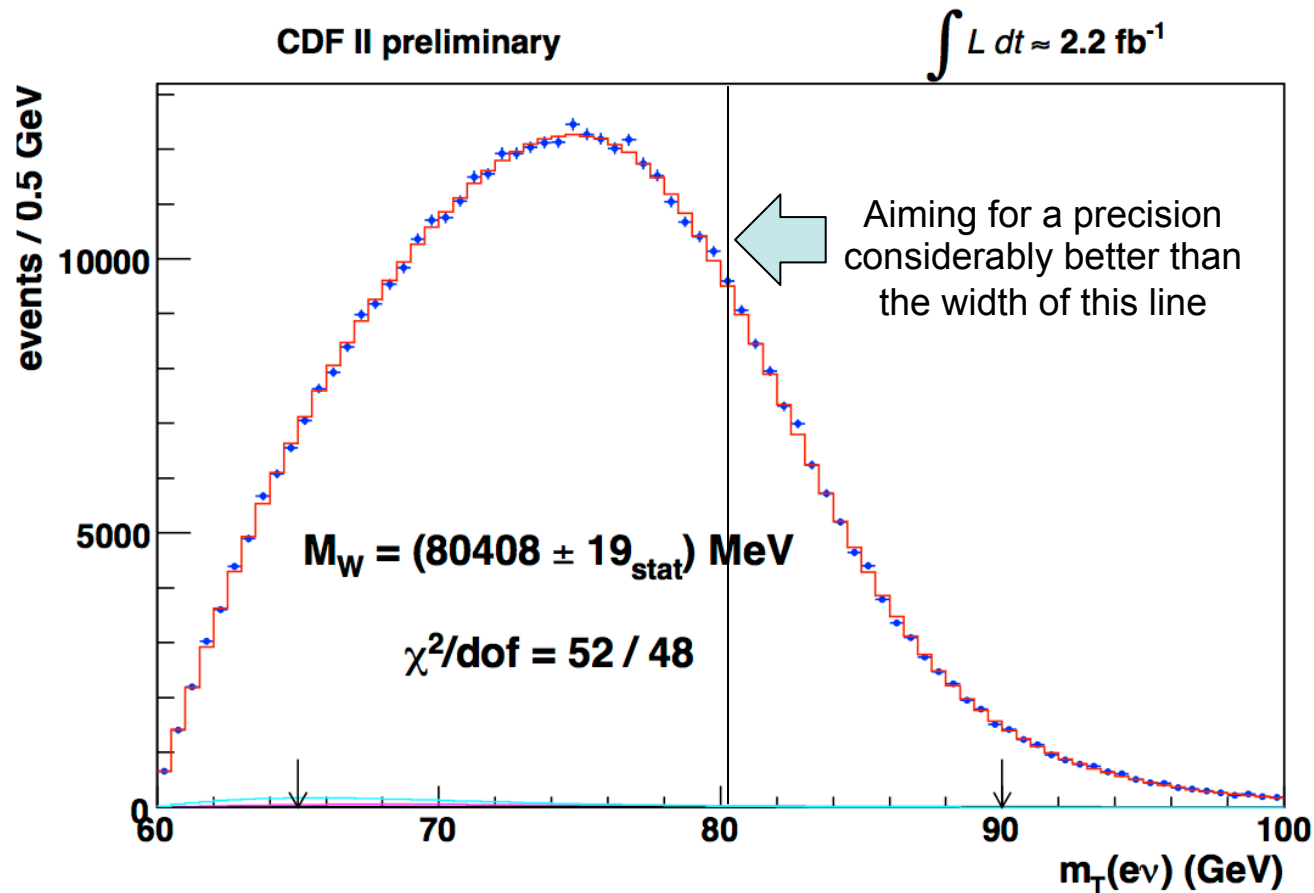
$$\vec{p}_T^{\nu} = -(\vec{p}_T^l + \vec{u}_T)$$

Transverse Mass :

$$M_T = \sqrt{2p_T^l p_T^{\nu} (1 - \cos(\Delta\phi^{l\nu}))}$$



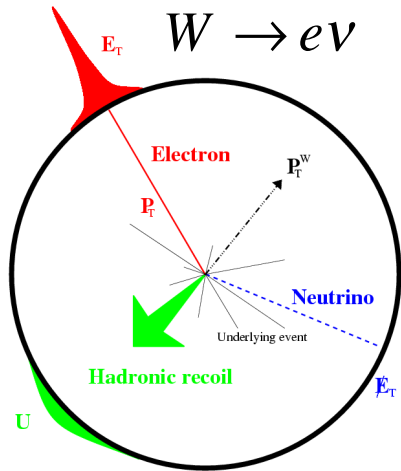
Measurement Strategy



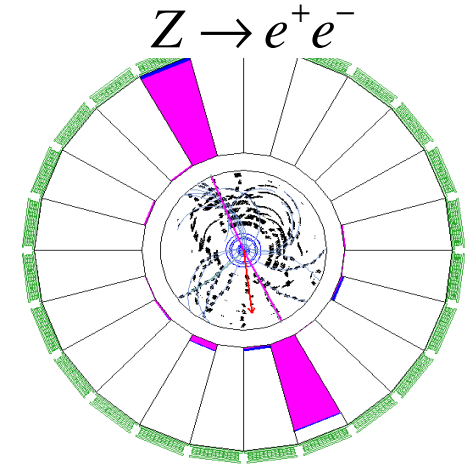
- ▶ Fit to M_T around the Jacobian peak.
- ▶ Extremely good control of signal modelling, backgrounds & instrumental effects.
- ▶ Also extract independent information from lepton and neutrino p_T distributions.



W Mass : Samples

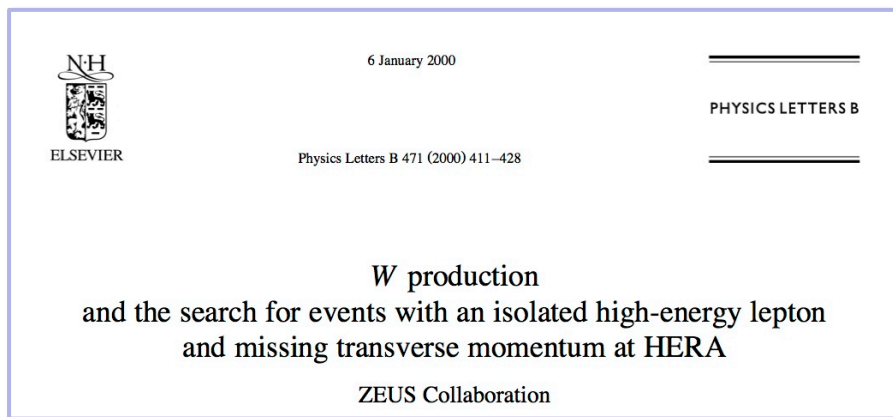


Channel (Exp.)	Luminosity	#Events
$W \rightarrow e\nu$	2.2 fb^{-1}	470, 126
$W \rightarrow \mu\nu$	2.2 fb^{-1}	624, 708
$Z \rightarrow ee$	2.2 fb^{-1}	16,134
$Z \rightarrow \mu\mu$	2.2 fb^{-1}	59,738

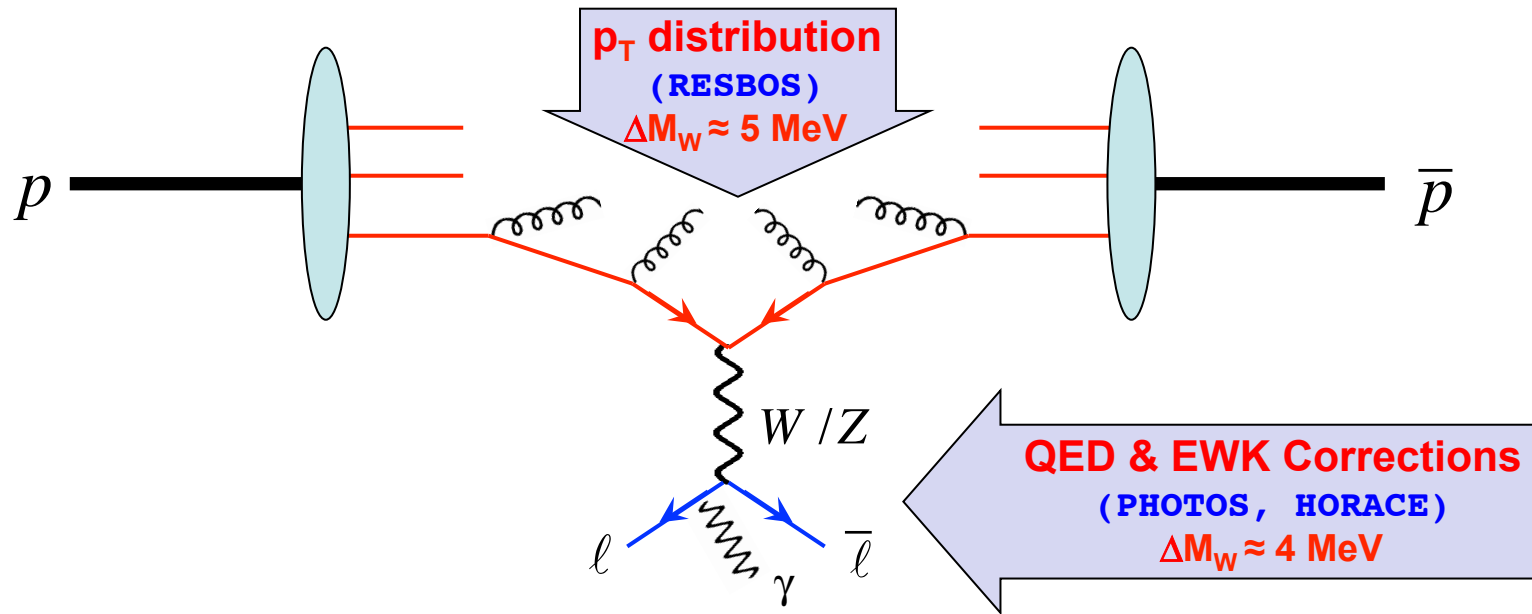


$W \rightarrow \ell\nu$ Kinematic Cuts \rightarrow $30 < p_T^\ell, p_T^\nu < 55 \text{ GeV}$
 $|\vec{u}| < 15 \text{ GeV}$

- Selection efficiencies are *small* compared to cross-section analyses : 3% (Z) - 12% (W).
- We are trading statistics for systematics - tight fiducial and ID cuts.



\leftarrow My Ph.D. Thesis
 3 $W \rightarrow e\nu$ events in 48 pb^{-1}
 $\sigma(e^+p \rightarrow e^+W^\pm X) = 0.9_{-0.7}^{+1.0} \pm 0.2 \text{ pb}$



$$d\sigma_{p\bar{p} \rightarrow W/Z \rightarrow \ell\bar{\ell}} = \int \sum_{i,j=u,d,s,(c,b)} [f_i^q(x_p) f_j^{\bar{q}}(x_{\bar{p}}) + f_i^{\bar{q}}(x_p) f_j^q(x_{\bar{p}})] \times d\sigma_{q\bar{q} \rightarrow W/Z \rightarrow \ell\bar{\ell}} dx_p dx_{\bar{p}}$$

y-distribution
(MSTW2008, CTEQ6.6)
 $\Delta M_W \approx 10 \text{ MeV}$

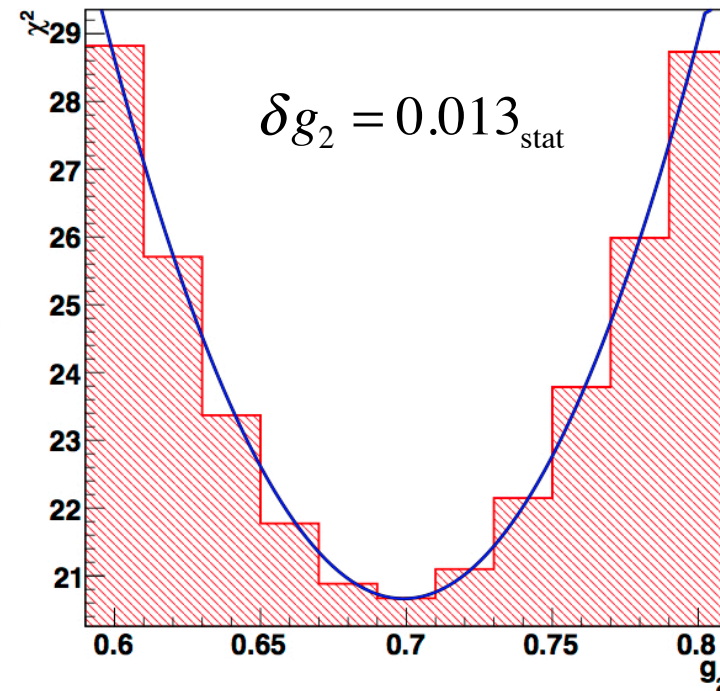
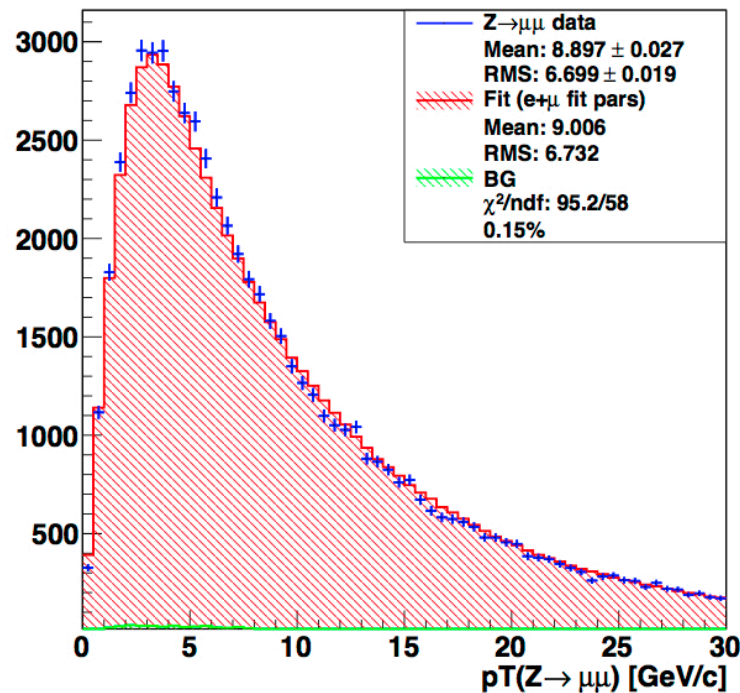
angular & mass distributions (RESBOS)

$$d\sigma_{q\bar{q} \rightarrow W/Z \rightarrow \ell\bar{\ell}}(\hat{s}, \theta_l, \phi_l) \propto \text{couplings} \times \left[\frac{1}{(\hat{s} - M_{W/Z}^2)^2 + (\Gamma_{W/Z} \hat{s} / M_{W/Z})^2} \right]$$

- Use the best model on the market : RESBOS [Landry et al. \(2003\)](#)

$$\frac{d\sigma}{dp_T^{W/Z}} \sim f^{\text{PETURBATIVE}}(\alpha_s) \times f^{\text{NON-PETURBATIVE}}(\alpha_s, g_1, g_2, g_3)$$

- Constrain parameters using *our own* Z data :



- Vary g_2 and α_s taking into account correlations $\rightarrow M_W \sim 3 \text{ MeV}$

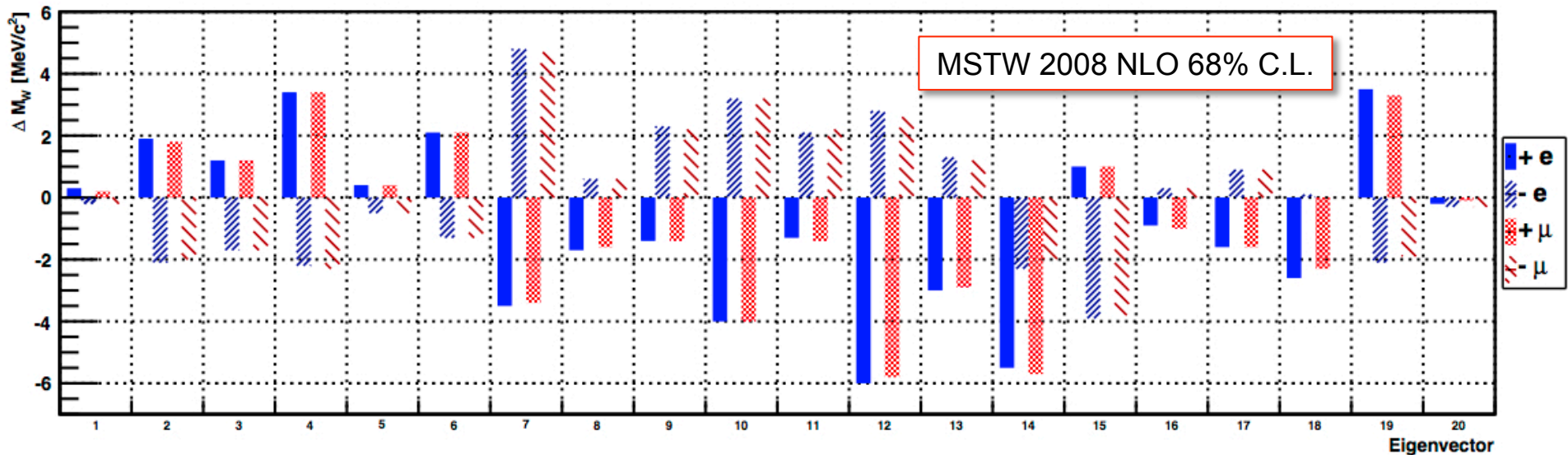
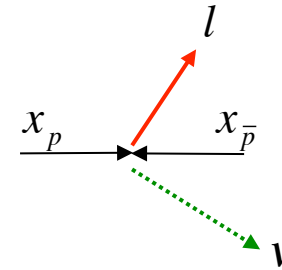
Dan Beecher Ph.D. Thesis



W Production Modelling : p_z



- PDF's sculpt kinematic distributions through the requirement that the charged lepton be central :
- Generate weighted event ensembles using PDF error sets :



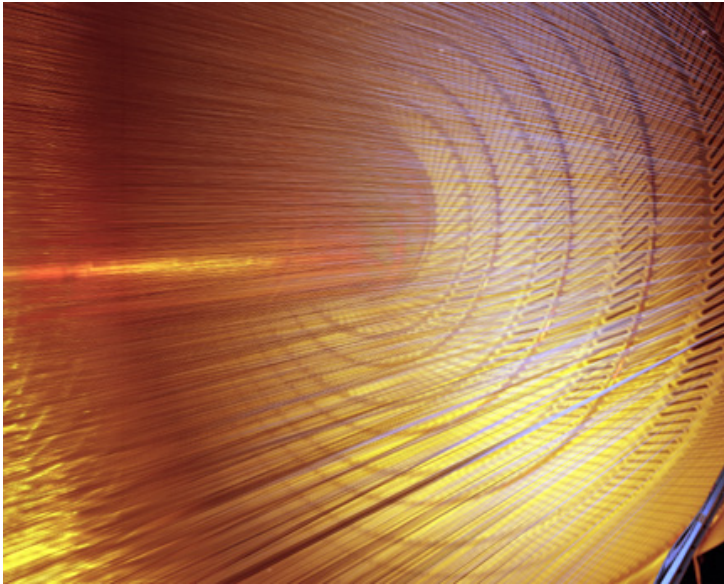
$$\Delta M_W = \frac{1}{2} \sqrt{\sum_i (\Delta M_W^{i,+} - \Delta M_W^{i,-})^2} \quad (\text{special treatment for shifts with the same sign})$$

→ $M_W \sim 10 \text{ MeV}$ (validated using CTEQ6, NNLO etc.)

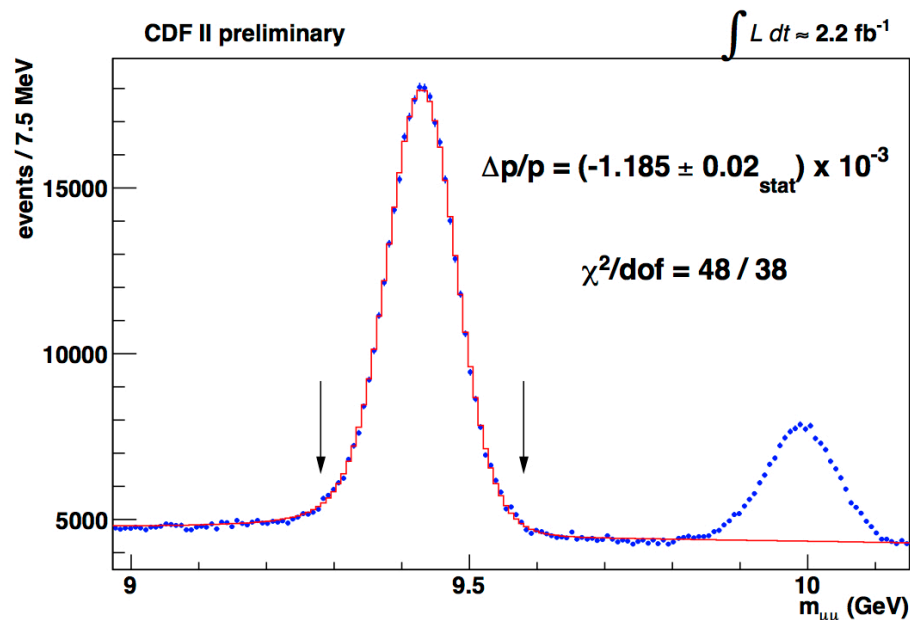
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Momentum Scale



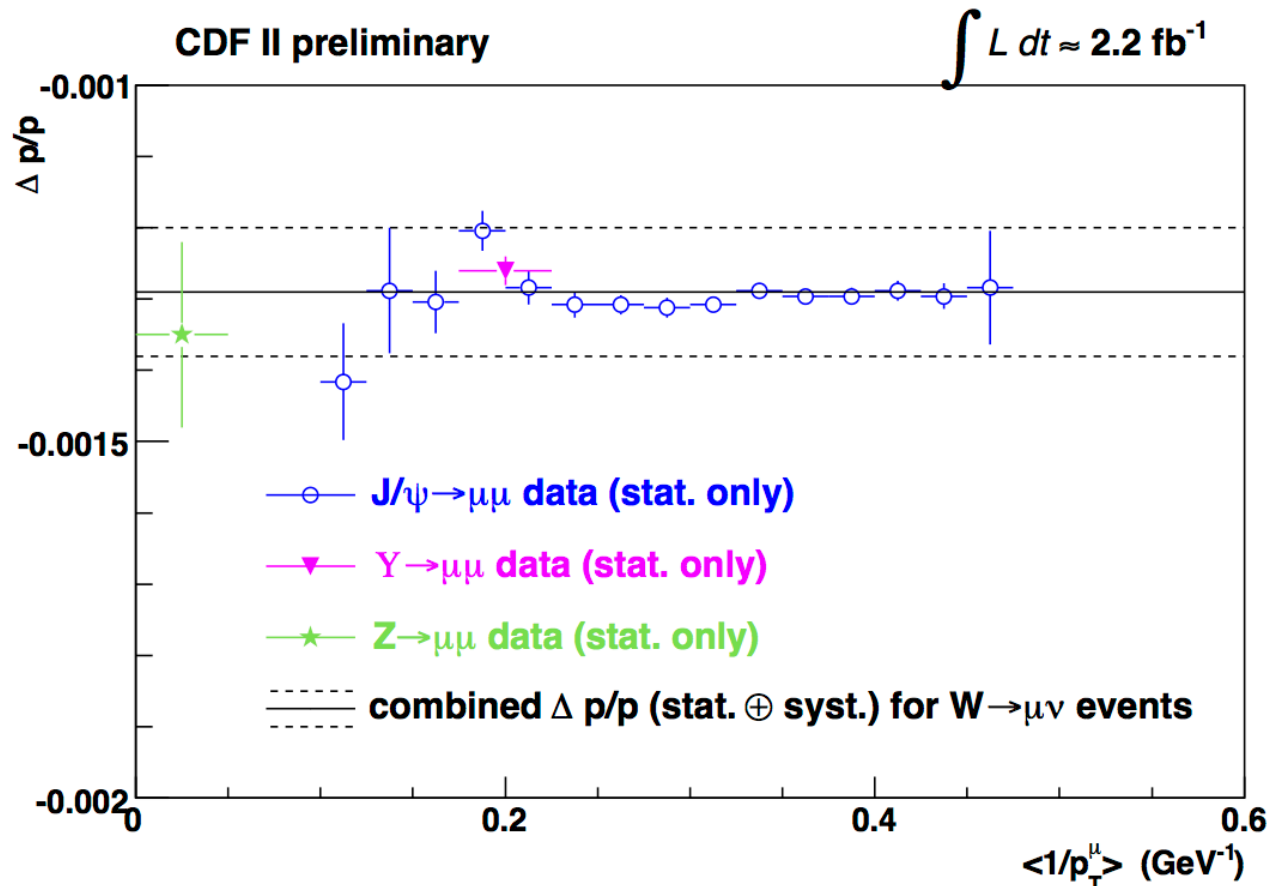
- The heart of the CDF analysis is the extremely good p_T measurement from the tracker.
- Start with a detailed cosmic ray internal alignment of the 30,240 sense wires of the COT to an accuracy of $\sim 5 \mu\text{m}$



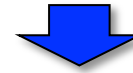
- Use fits to precisely known J/Ψ and Υ resonances spanning a large range of curvature.
- Fit the single hit resolution $\sim 150 \mu\text{m}$ and the effect of the beam constraint.



Momentum Scale



$$\Rightarrow \frac{\delta p}{p} = 0.00009$$



$$\Delta M_W(\mu) = 7 \text{ MeV}$$



Flatness over a large p_T range
is also a test of dE/dx modelling



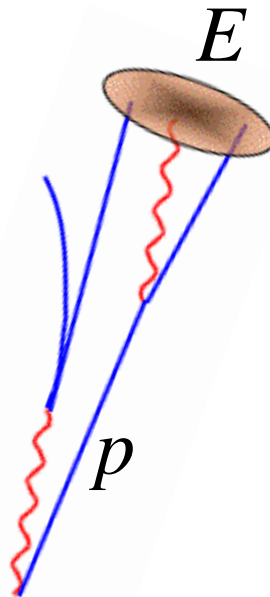
Electron Energy Scale



- How do we precisely determine the electromagnetic calorimeter energy scale ?

[1] Transfer the precise momentum scale to the calorimeter by fitting the ratio E/p for electrons.

- ▶ Statistically precise.
- ▶ Hard ! Need to understand reconstruction of E and p in minute detail.



[2] Extract directly by fitting to precisely known $Z \rightarrow ee$ resonance.

- ▶ Relatively easy. No tracking.
- ▶ Statistically poorer.

- Do the 2 methods agree ?
 - ▶ A very powerful cross-check .
 - ▶ Run 1 : 3.9σ discrepancy never resolved.

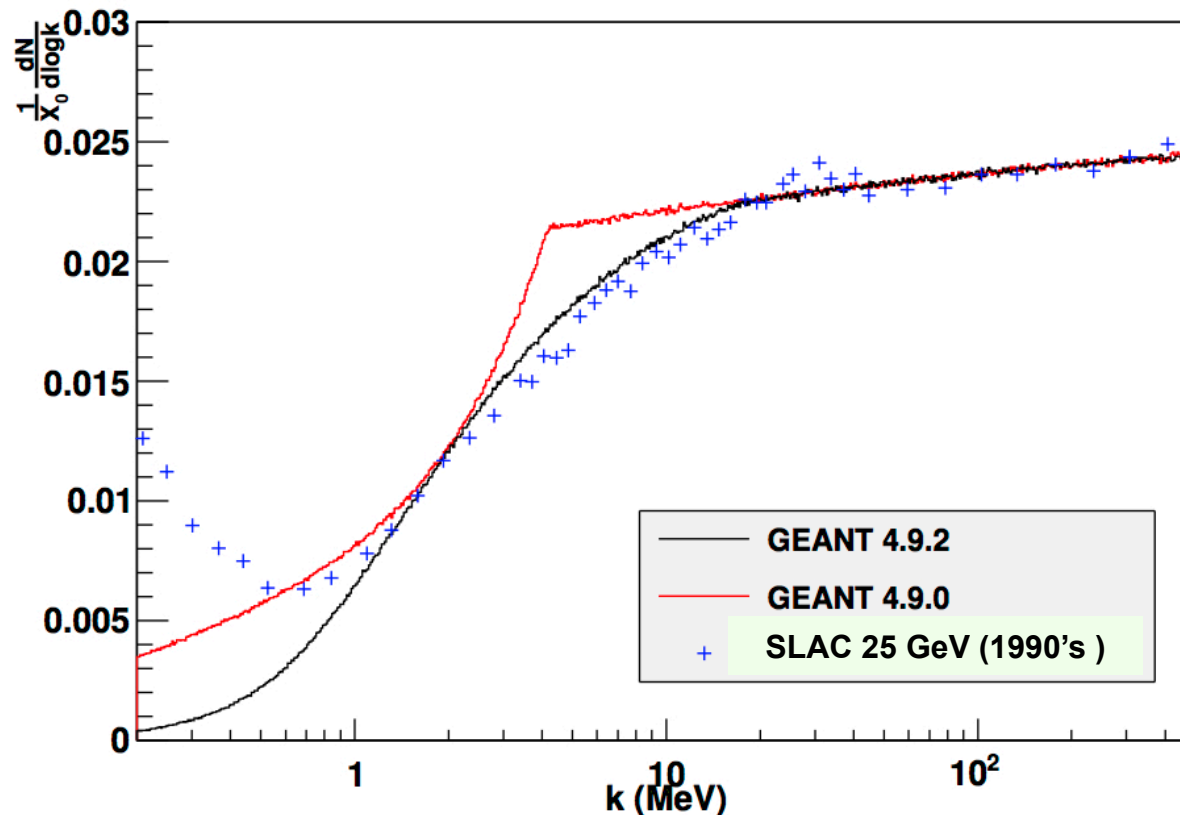


Electron Energy Loss Mechanisms



- Precise control over all possible energy loss mechanisms is required.
- For example Landau-Pomeranchuk-Migdal (LPM) suppression of Bremsstrahlung for low-energy photons :

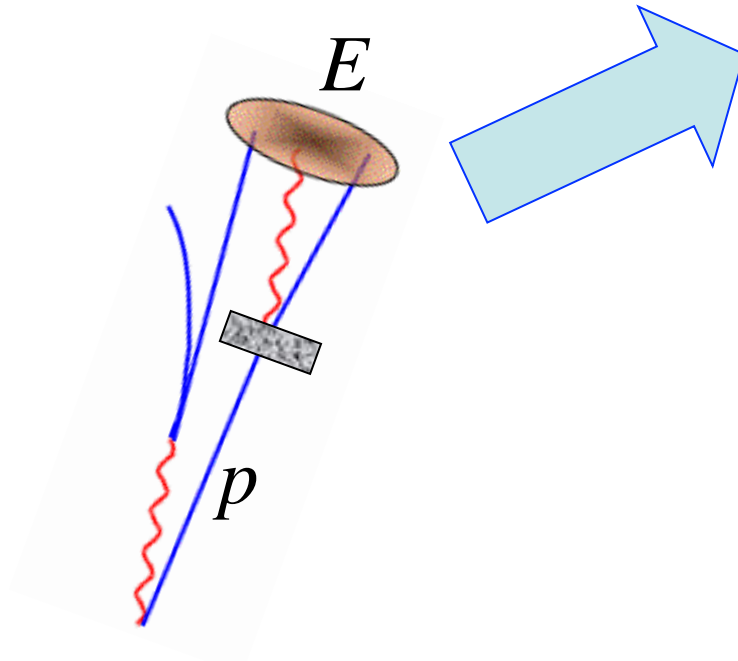
$$k(E_\gamma) < \frac{E^2}{E + E_{LPM}} \quad \text{where} \quad E_{LPM} \sim 72 \text{ TeV (Si)}$$



- Go back and systematically validate GEANT-4 against original test-beam data.
- Assess systematic uncertainty from all sources : **~ few MeV**

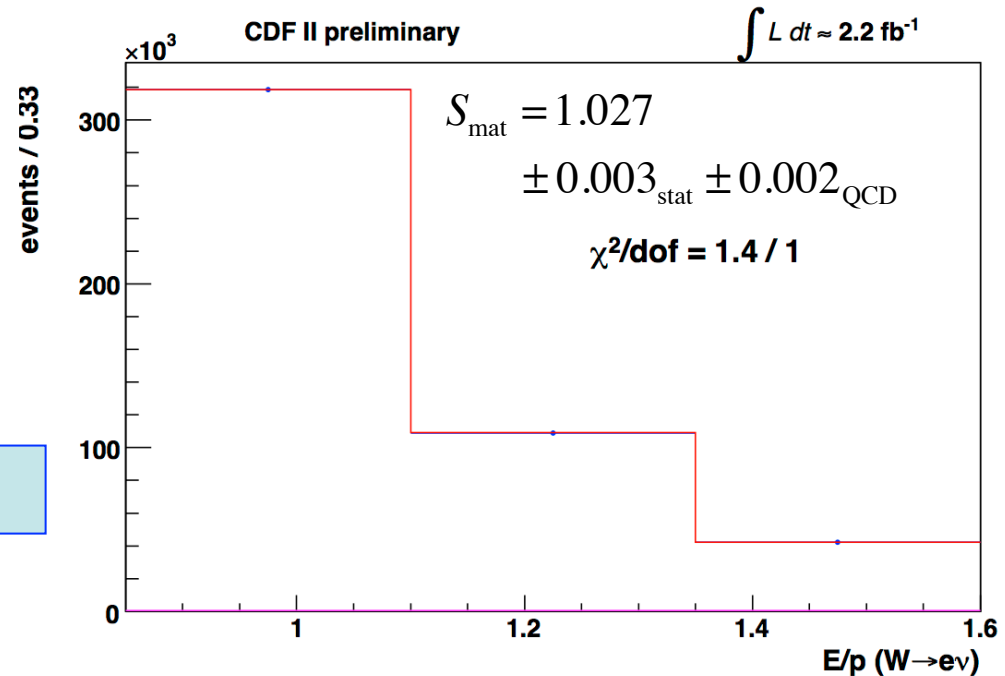
Tom Riddick Ph.D. Thesis

- Start from a detailed, tuned material map.
- Very detailed Brem. & energy loss treatment.
- Compare E/P tails in data and simulation :



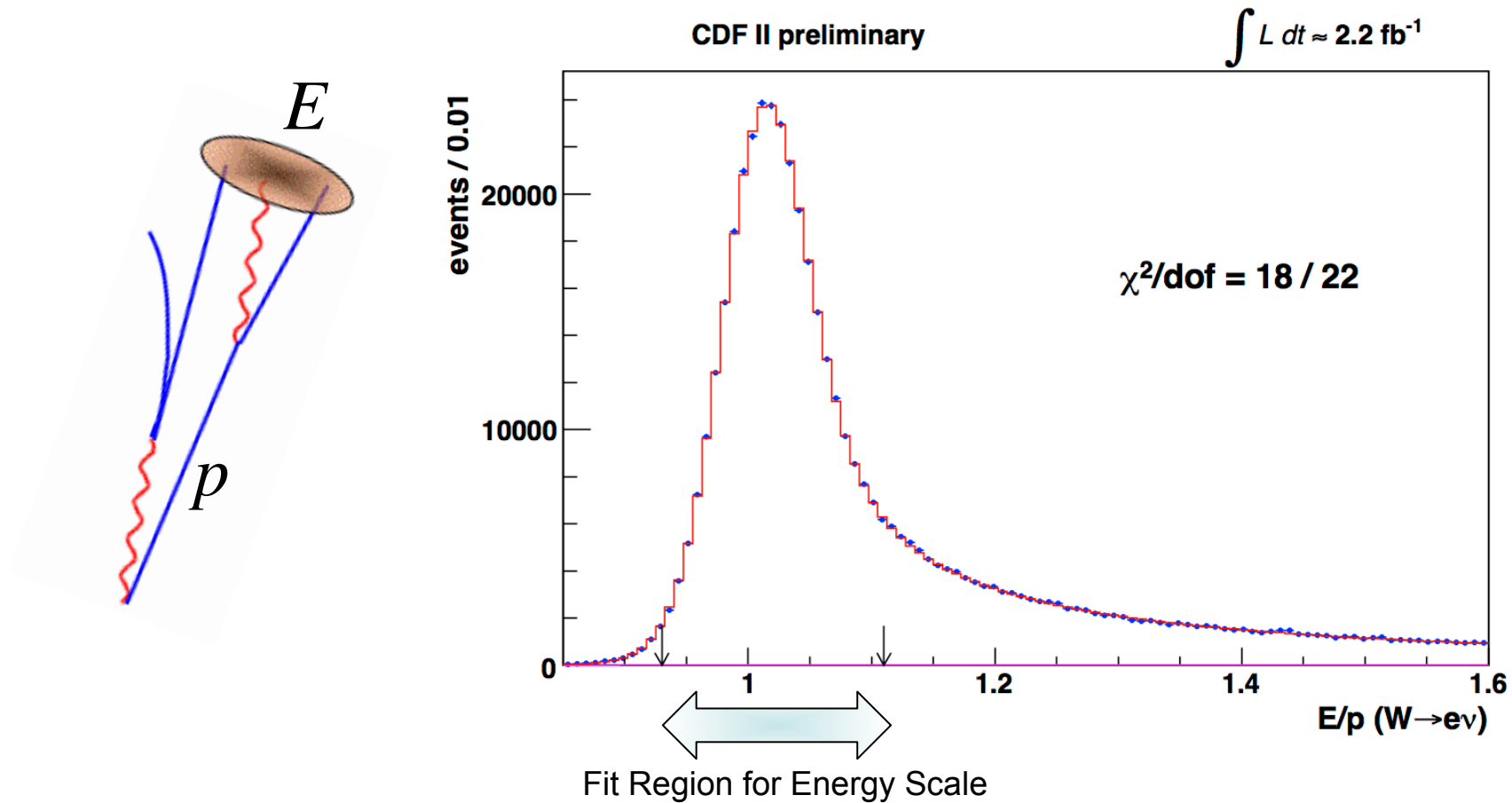
$E/p \sim 1$
No Brem.

$E/p \sim 1.5$
Hard Brem.



Determine amount of radiating material to better than 0.5%

- Transfer p-scale to E-scale using E/p :



- Need to worry about *non-linearity* when comparing scales determined from W's and Z's

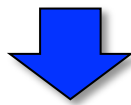
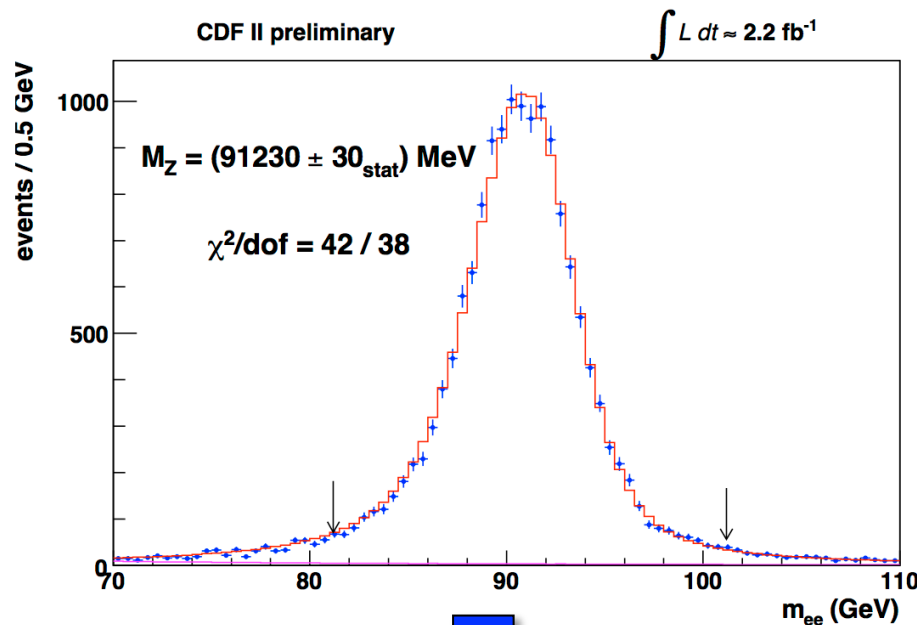
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M_Z Cross-Checks

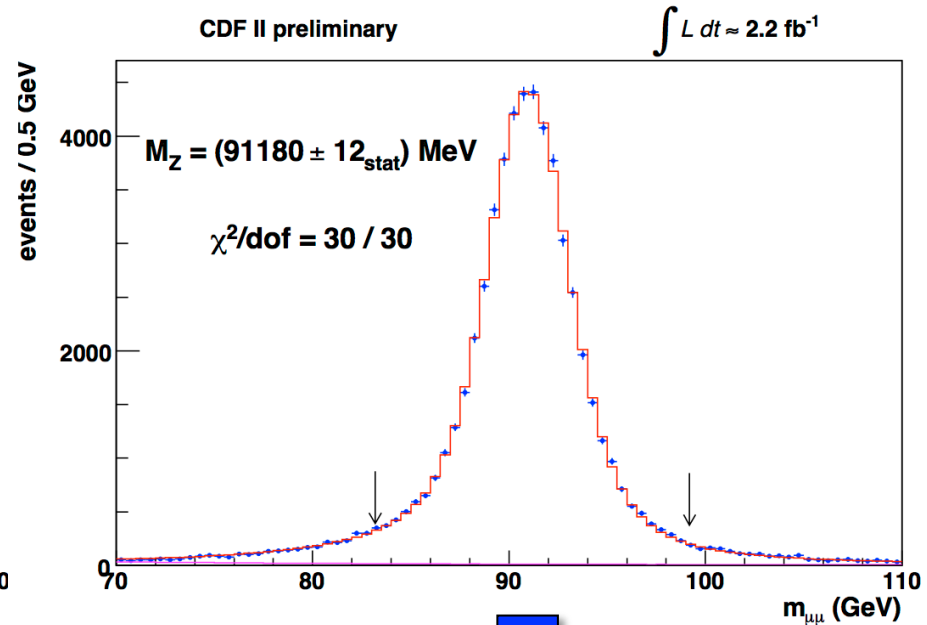


- Z mass fits blinded until the p-scale (from J/ψ and Υ) and E-scale (from E/p) were finalised.
- Compare Z mass fits with PDG .
- Subsequently Z constraints are included in p/E-scale determinations.



combined with E/p to give :

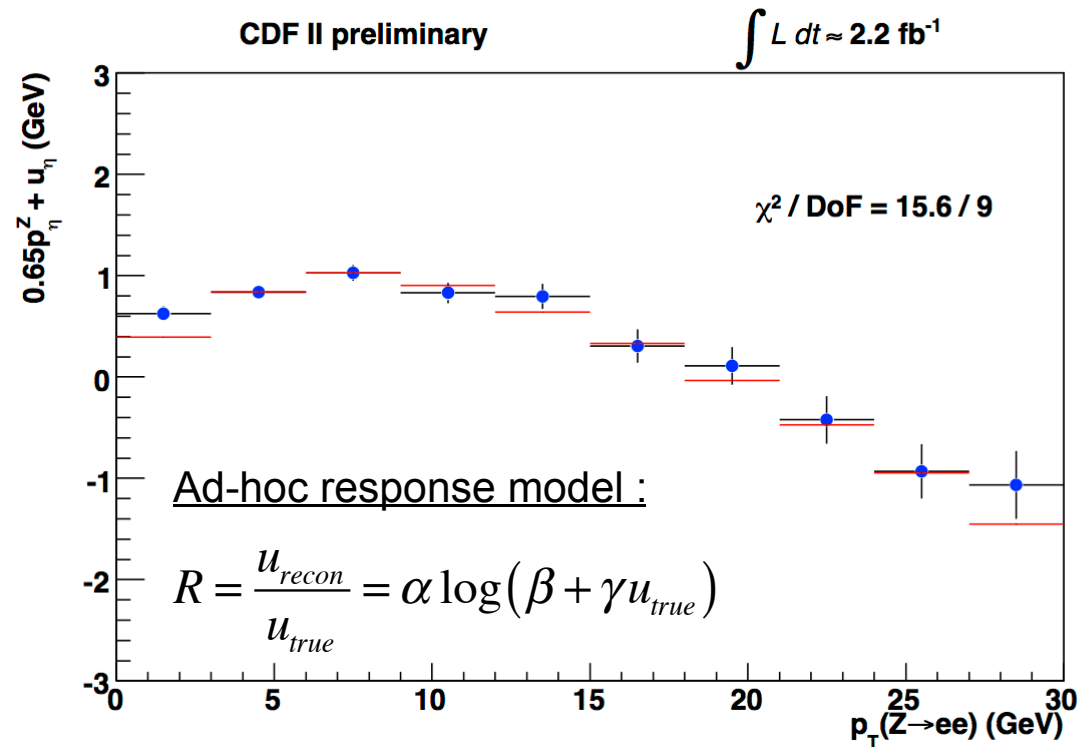
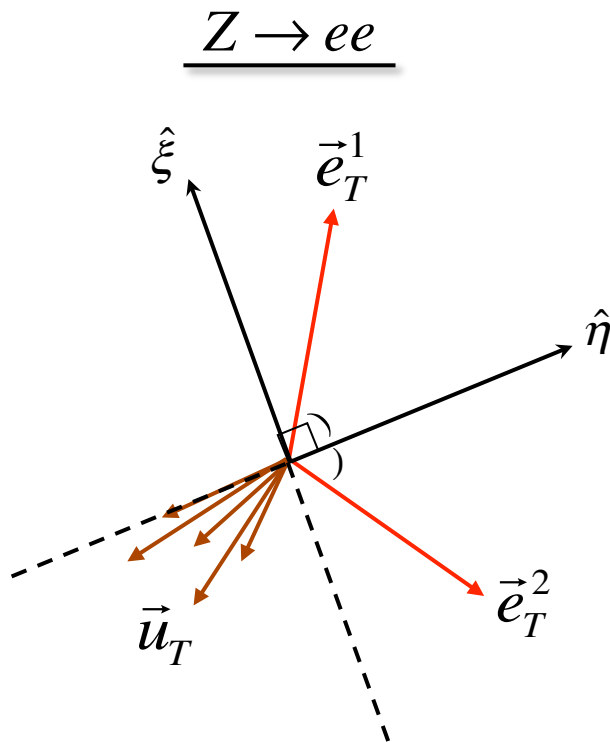
$$\Delta M_W (e) = 10 \text{ MeV}$$



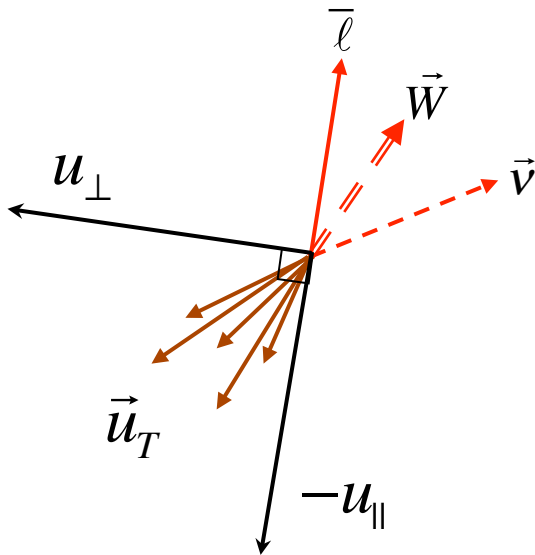
combined with J/ψ and Υ to give :

$$\Delta M_W (\mu) = 7 \text{ MeV}$$

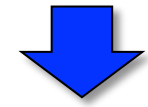
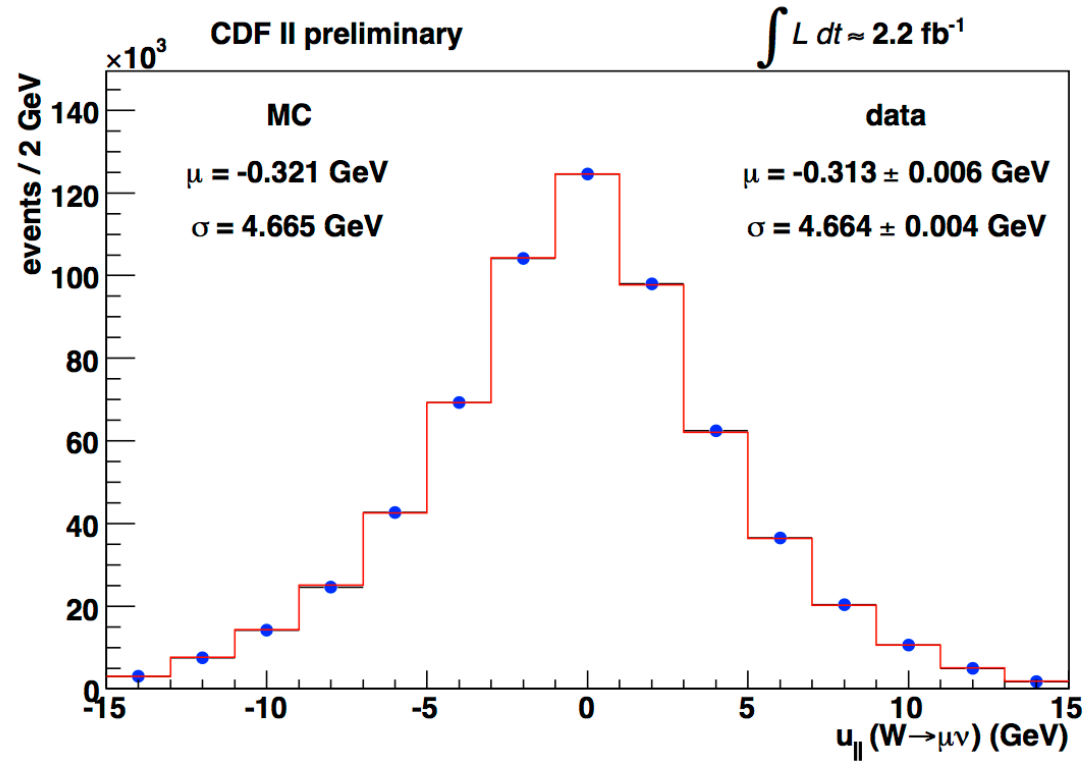
- “Recoil” from (1) W/Z p_T (2) UE (3) overlapping MB events (4) lepton energy leakage/FSR.
- Tune using Z data and minimum-bias data.



$$\underline{W \rightarrow e\nu}$$



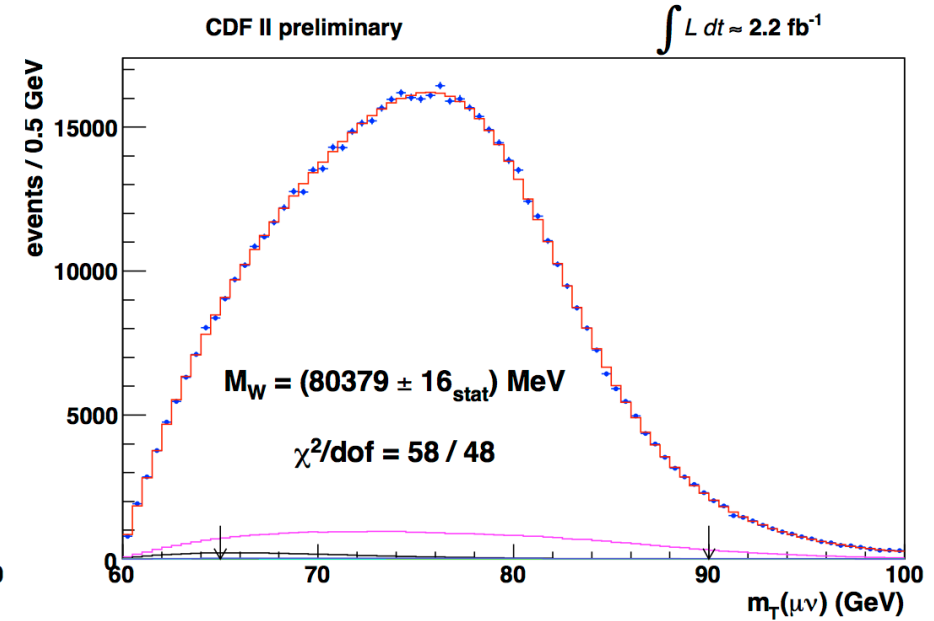
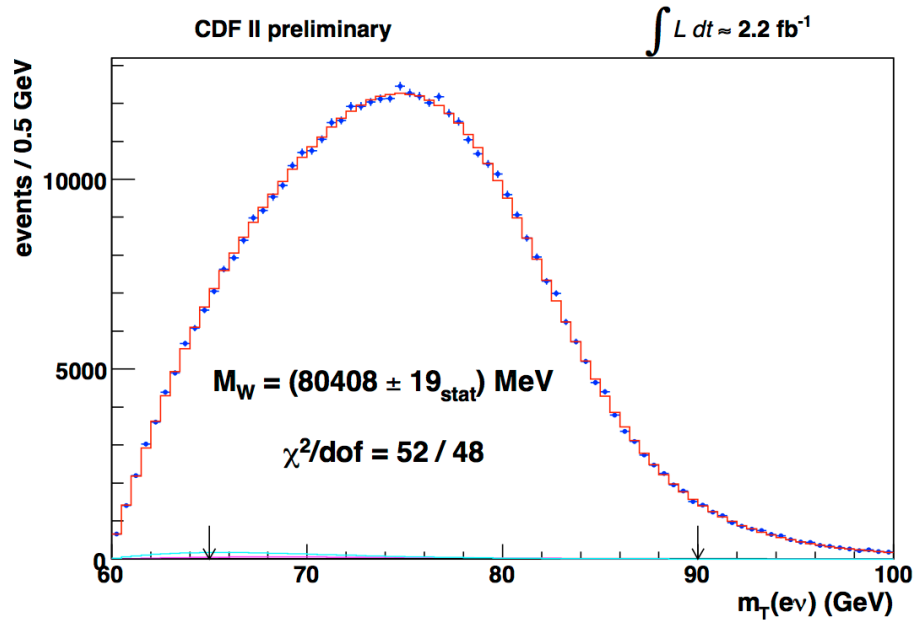
$M_T \sim 2p_T^\ell + u_{\parallel}$
 direct bias on M_W
 if mis-modelled



- ▶ Good agreement between W data and simulation.
- ▶ Residual recoil modelling systematic **~ 6 MeV**



Results



Kinematic Distribution	Electron (MeV)	Muon (MeV)	$P(\chi^2)$ (stat + syst)
Transverse Mass	80408 ± 19	80379 ± 16	28%
Lepton Transverse Momentum	80393 ± 21	80348 ± 18	13%
Neutrino p_T	80431 ± 25	80406 ± 22	49%
$P(\chi^2)$ (stat + syst)	49%	12%	



Systematic Uncertainties

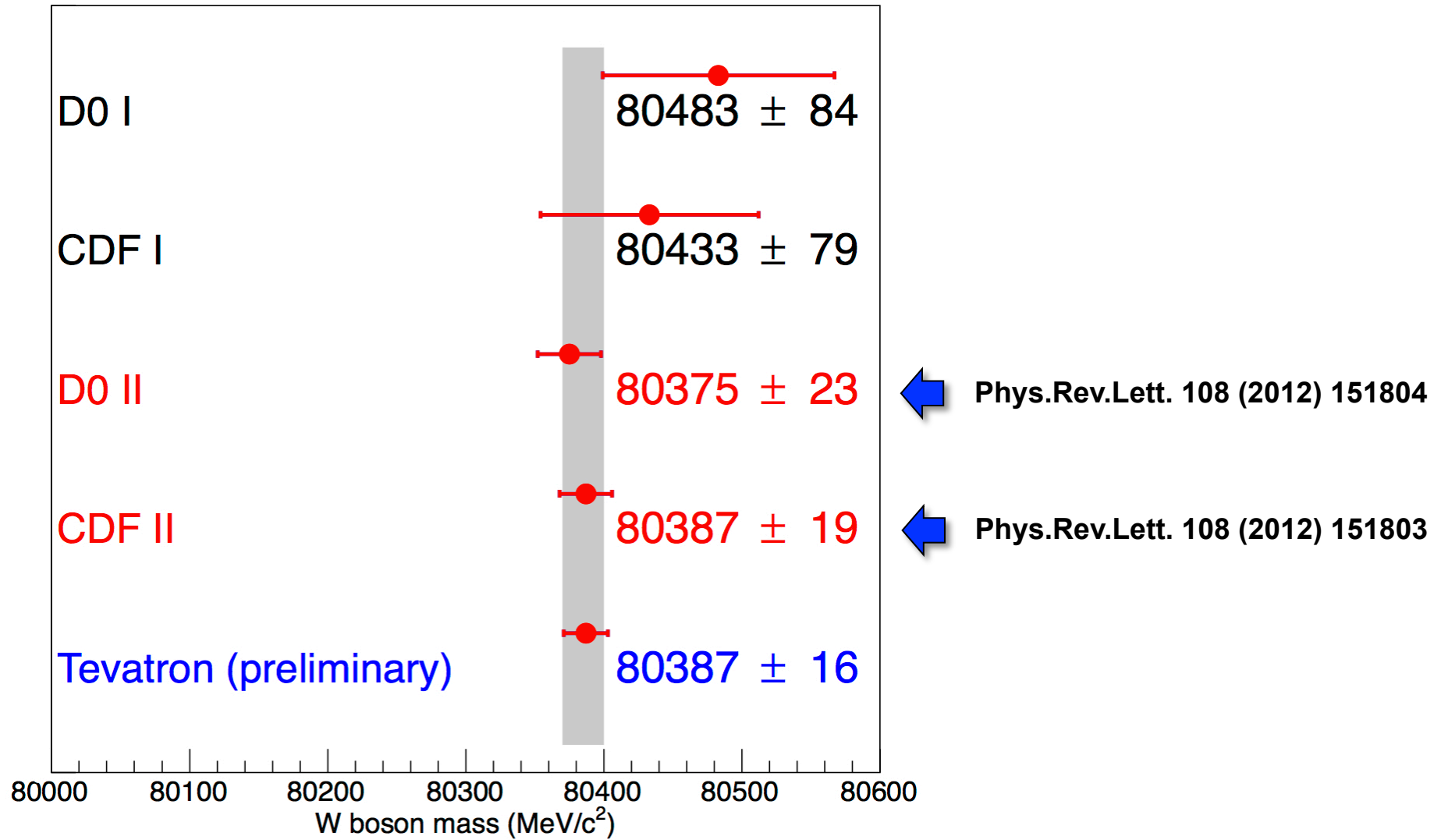


- All 6 fits are combined taking into account correlations : $P(\chi^2) = 25\%$

Source	Uncertainty (MeV)	
Lepton Energy Scale	7	← Tom, Ilija
Lepton Energy Resolution	2	
Recoil Energy Scale	4	← Sarah
Recoil Energy Resolution	4	← Sarah
Recoil Corrections	2	
Backgrounds	3	
$p_T(W)$ Model	5	← Dan
PDFs	10	← Dan
QED Radiation	4	← Ilija
Total Systematic	15	
Statistical	12	
Total Uncertainty	19	

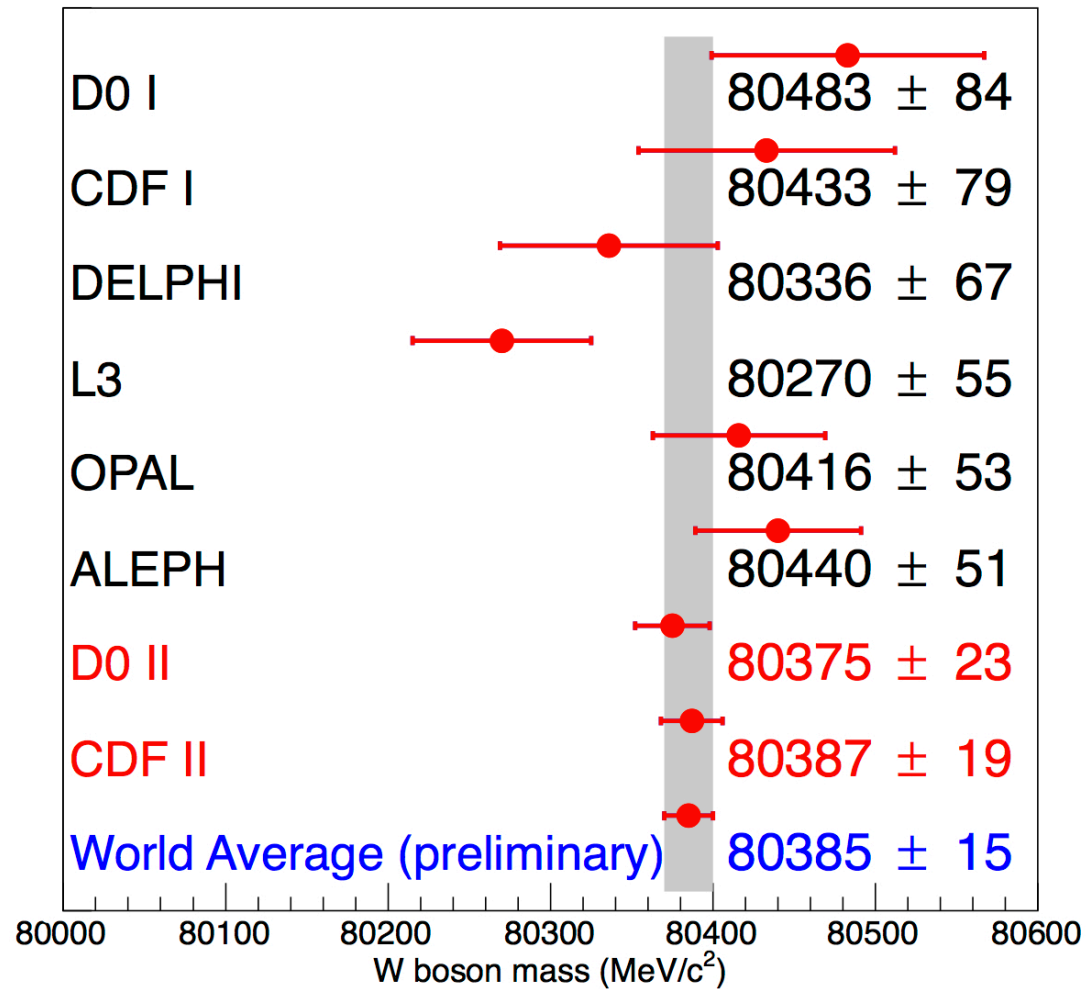


New Tevatron Average





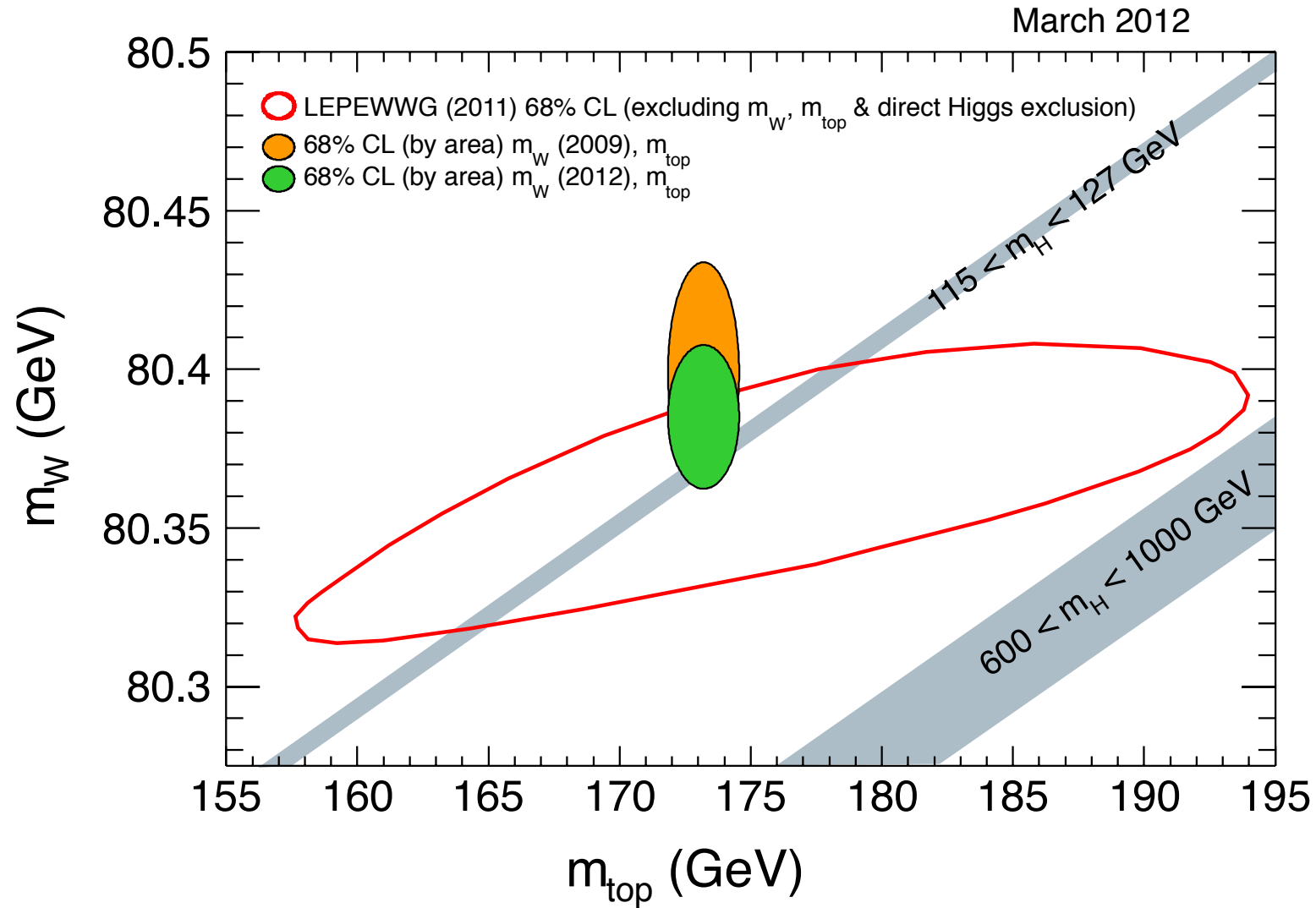
New World Average



- ▶ Previous World Average (2009) : $M_W = 80399 \pm 23 \text{ MeV}$
- ▶ Error reduced by $\frac{1}{3}$

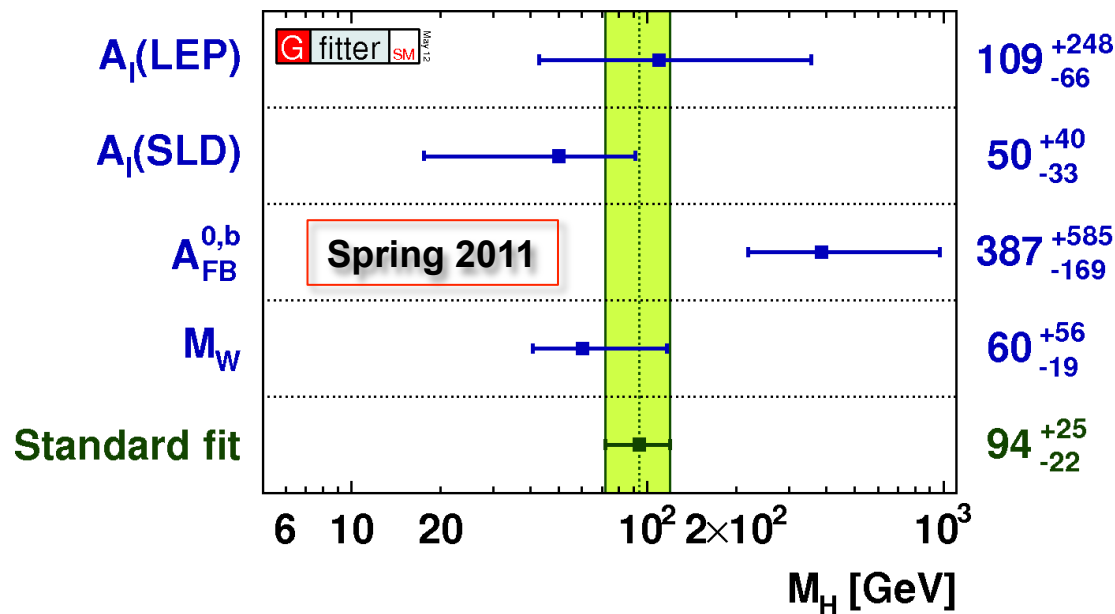
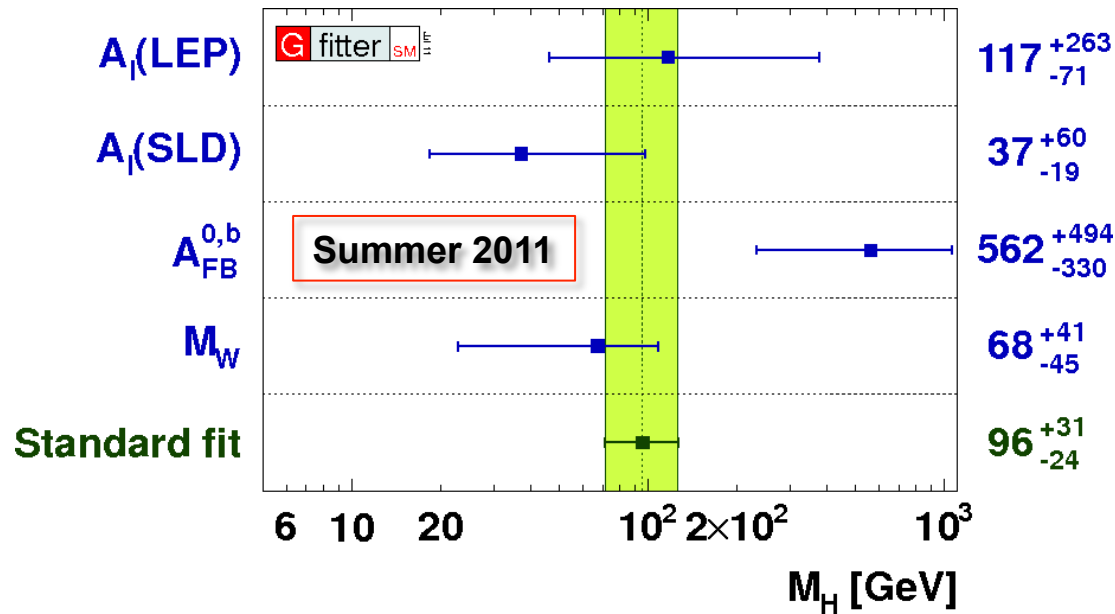


Consequences of the New M_W Measurement

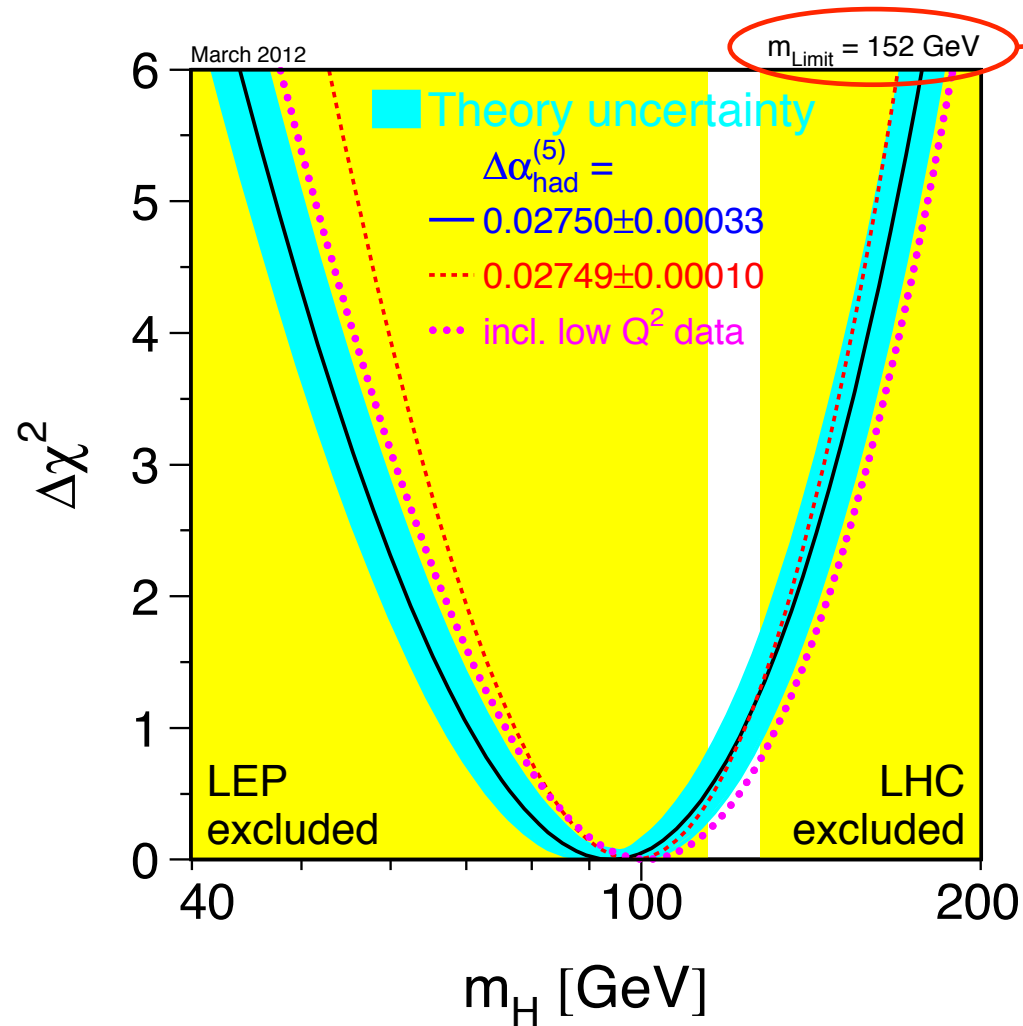




Consequences of the New M_W Measurement



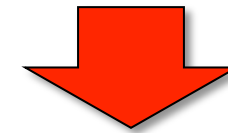
- ▶ Small decrease in central Higgs value.
- ▶ Tighter constraint on m_H



from 161 GeV

$$M_W = 80385 \pm 15 \text{ MeV}$$

$$M_{\text{top}} = 173.2 \pm 0.9 \text{ GeV}$$



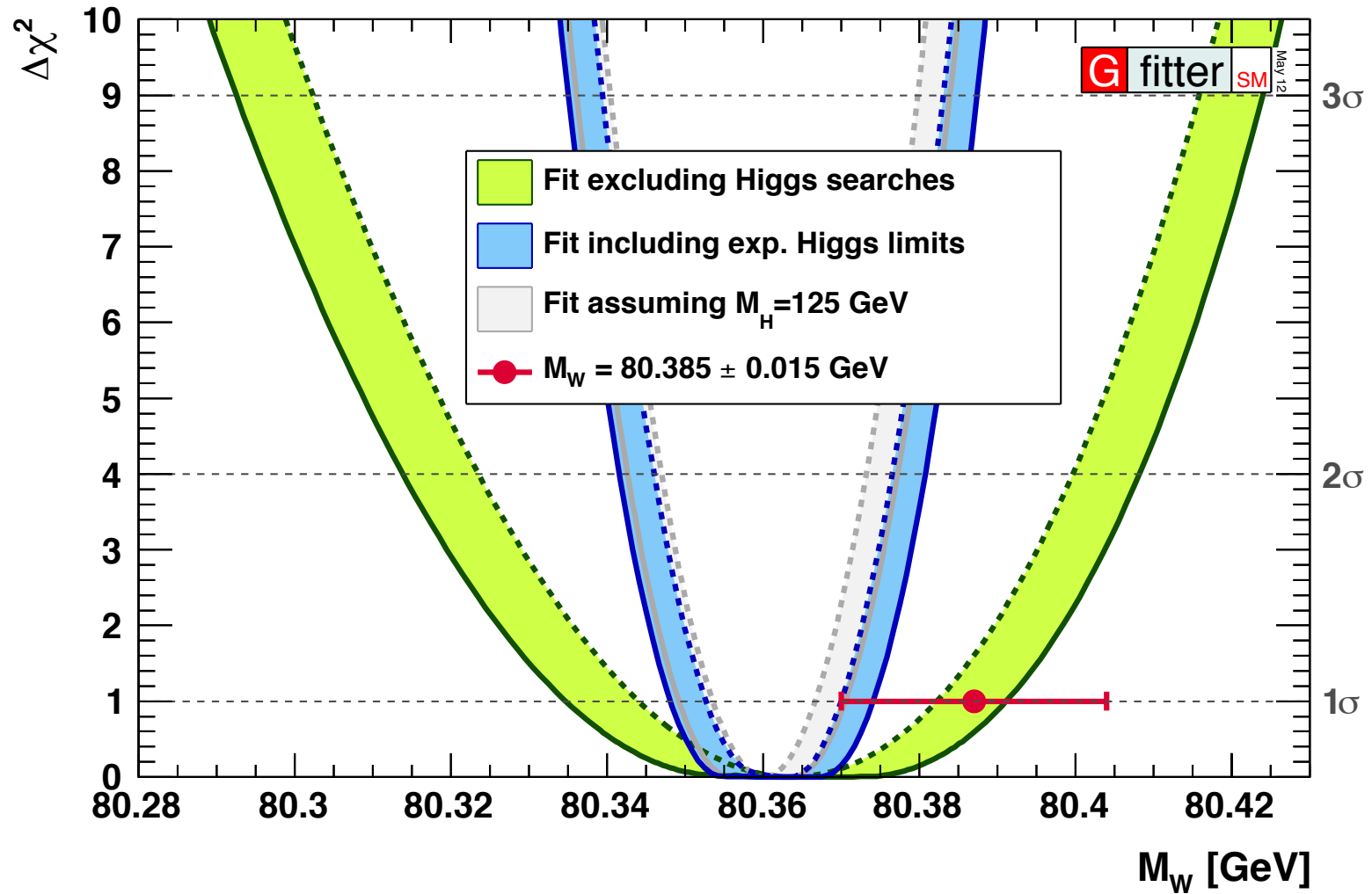
$$M_H = 94^{+29}_{-24} \text{ GeV}$$

$$M_H < 152 \text{ GeV} @ 95\% \text{ C.L.}$$

(LEPEWWG/Zfitter)



Consequences of the New M_W Measurement

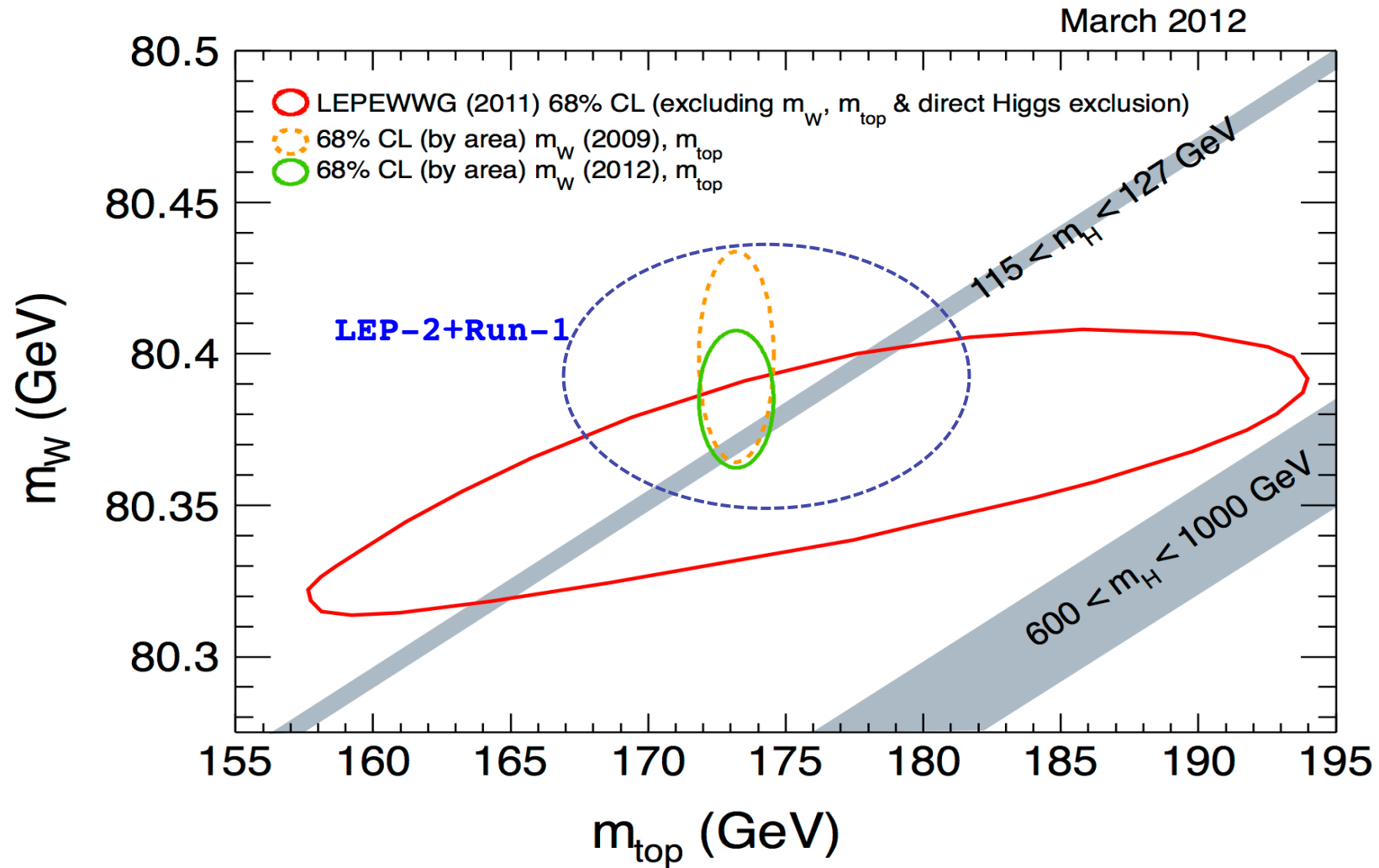




Impact of Run 2



- Impact of Run 2 precision measurements of m_W and m_{top} :

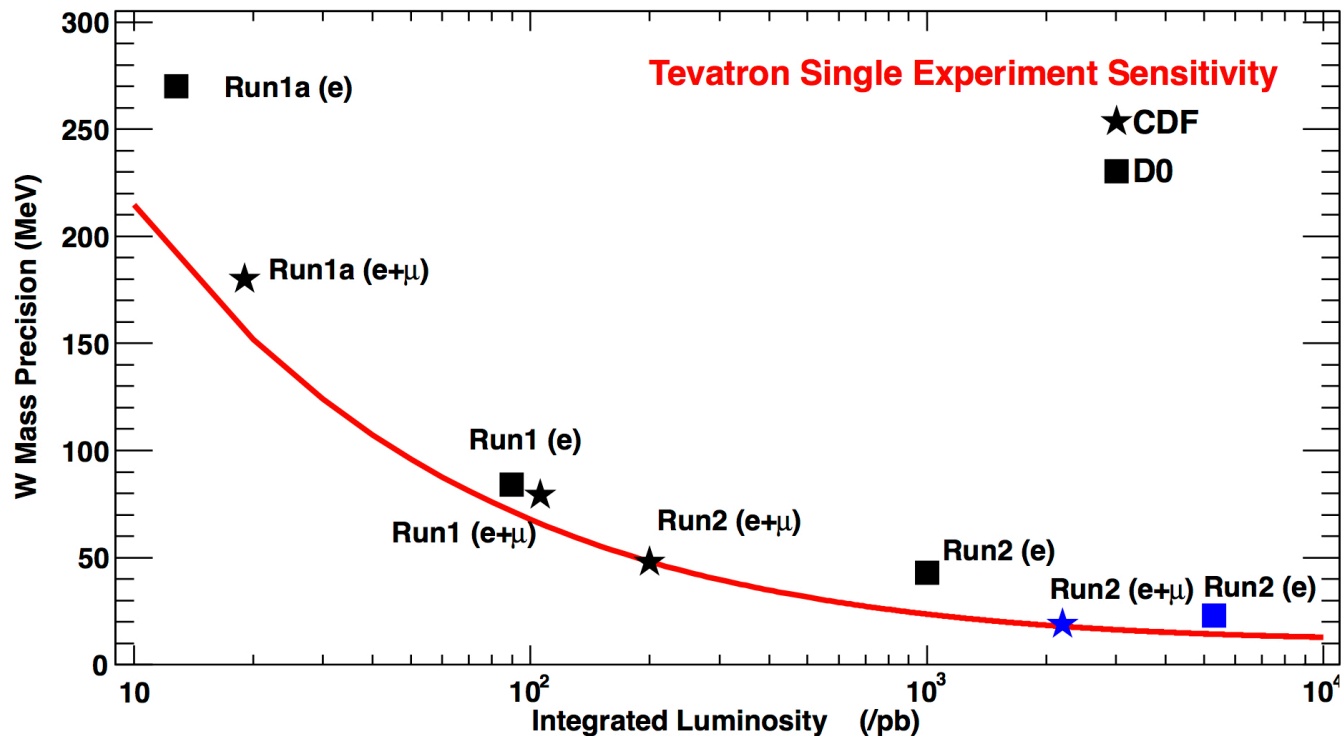




Outlook



- The W mass measurement can be further improved – for CDF only $\frac{1}{4}$ of the final dataset has been analysed. By how much ?



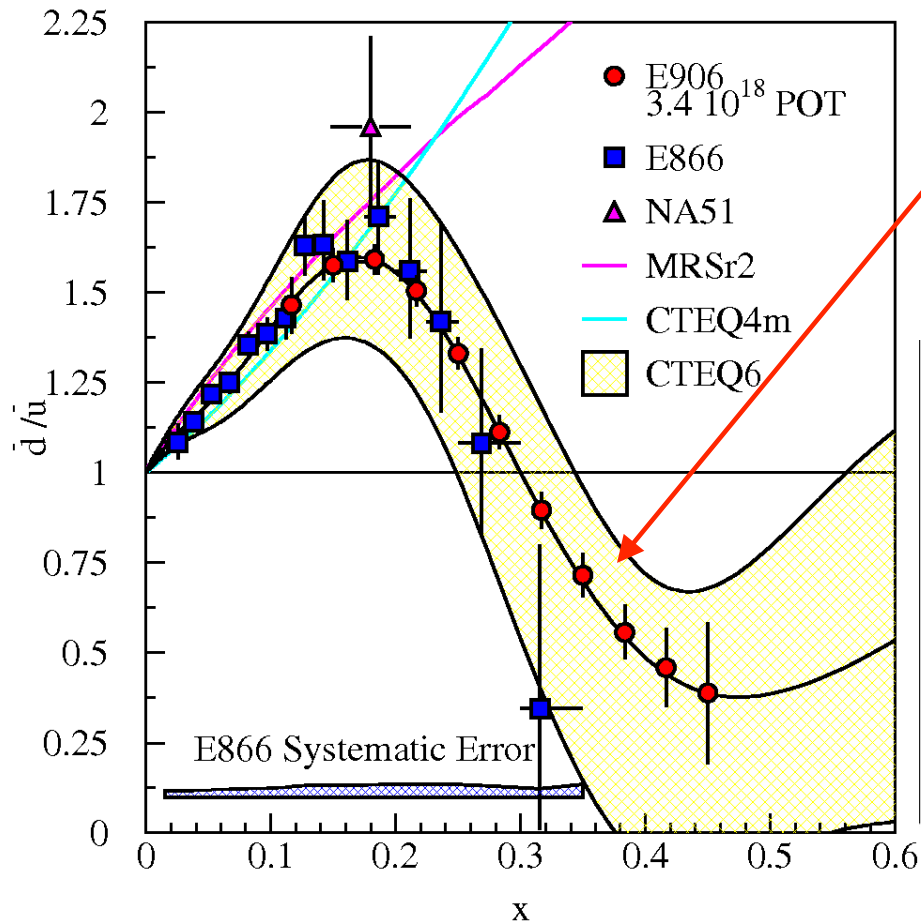
Run 2 Physics Workshop, 1999 \rightarrow 40 MeV with 2 fb^{-1}

Report of the Working Group on Precision Measurements

Conveners: Raymond Brock^a, Jens Erler^b, Young-Kee Kim^c, and William Marciano^d

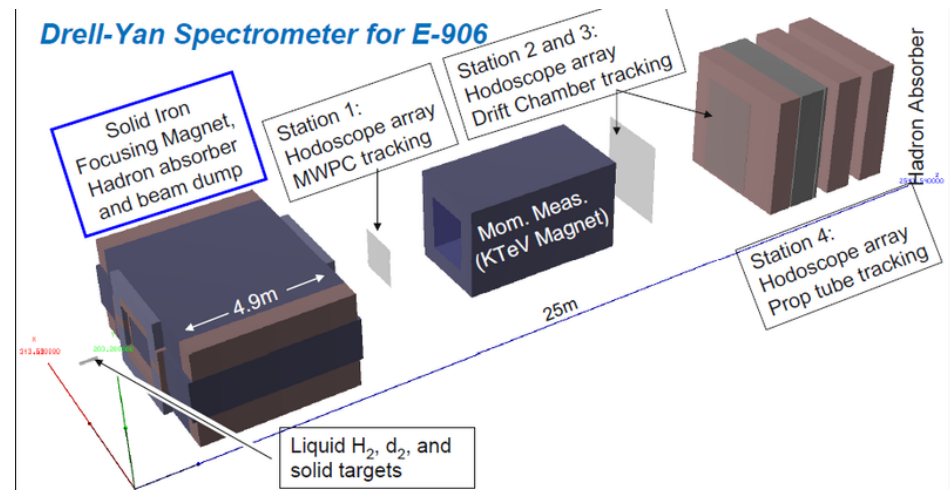
Working Group Members: William Ashmanskas^e, Ulrich Baur^f, John Ellison^g, Mark Lancaster^h, Larry Nodulmanⁱ, John Rha^j, David Waters^k, John Womersley^l

- Model systematics are becoming the limiting factor.
- New techniques or inputs required to reduce the PDF uncertainty on M_W .



- Precision expected from “SeaQuest”
 $pp \rightarrow \mu^+ \mu^- + X$
- LHCb/ATLAS/CMS ?

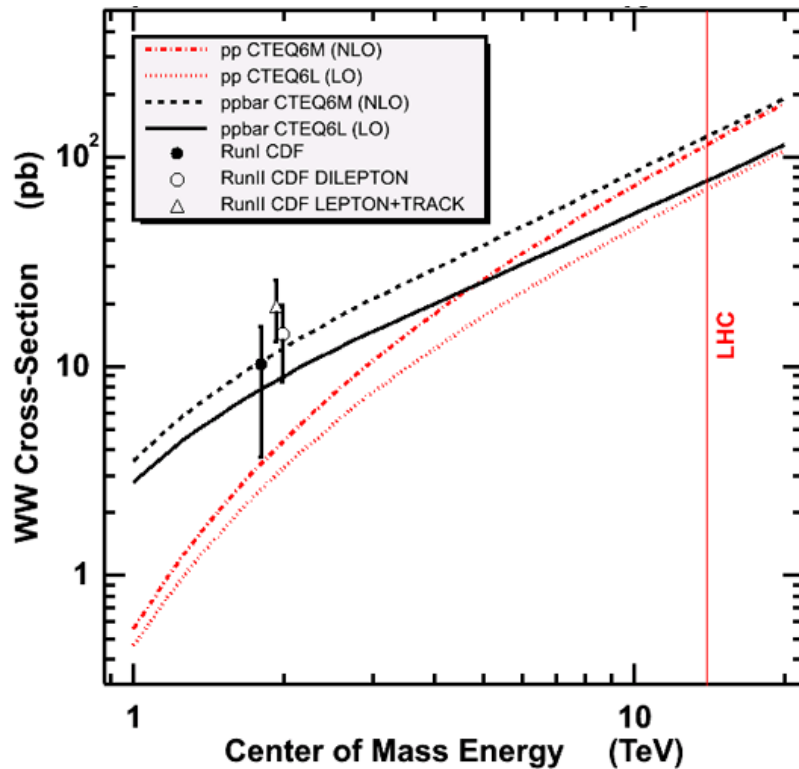
Drell-Yan Spectrometer for E-906





$\sigma(WW)$ (2004)

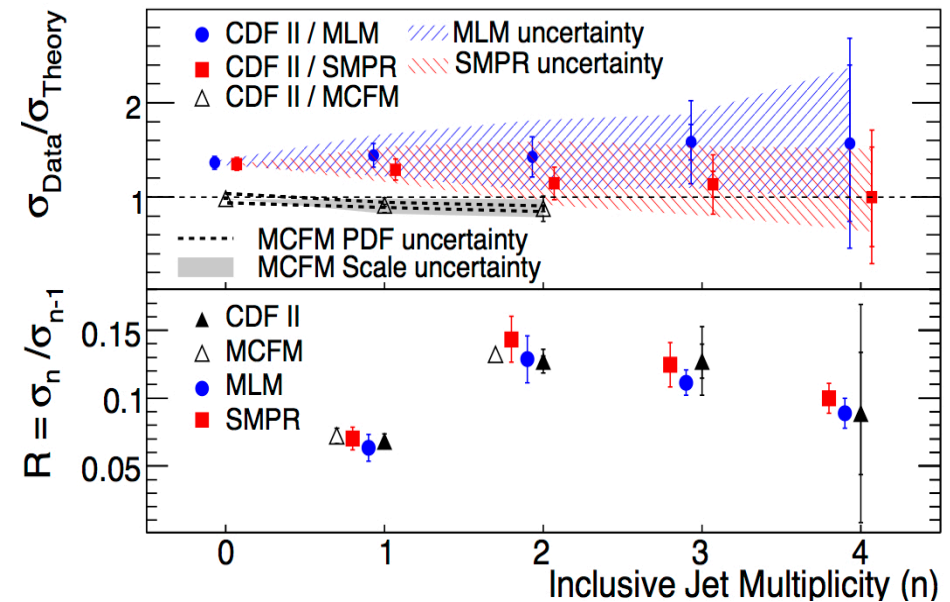
- ▶ First significant hadron collider measurement.
- ▶ Led on to using WW as a Higgs search channel.



$\sigma(W+jets)$ (2008)

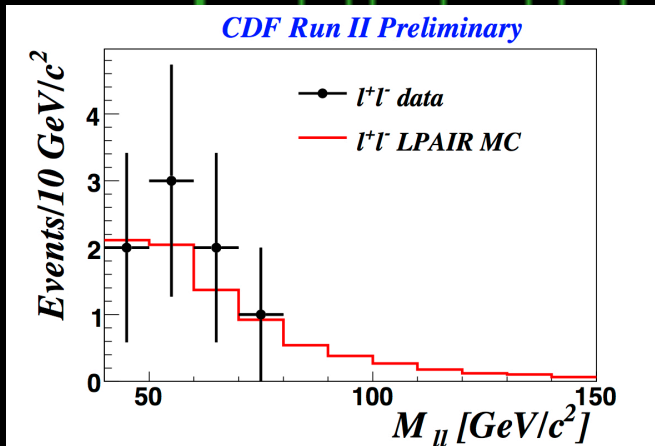
- ▶ Total and differential cross-section measurements.
- ▶ An early test of “Parton Shower Matching” schemes.

- ▶ New experimental methods developed.





Exclusive Z Production

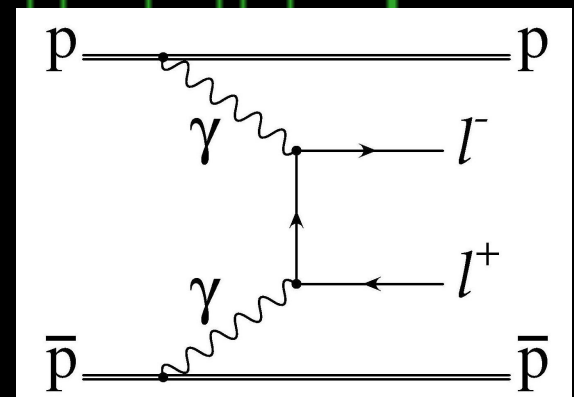
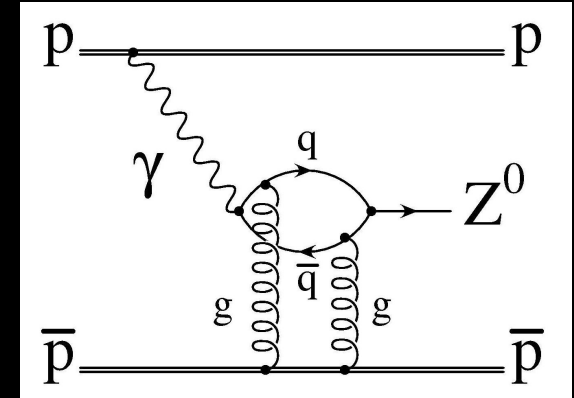
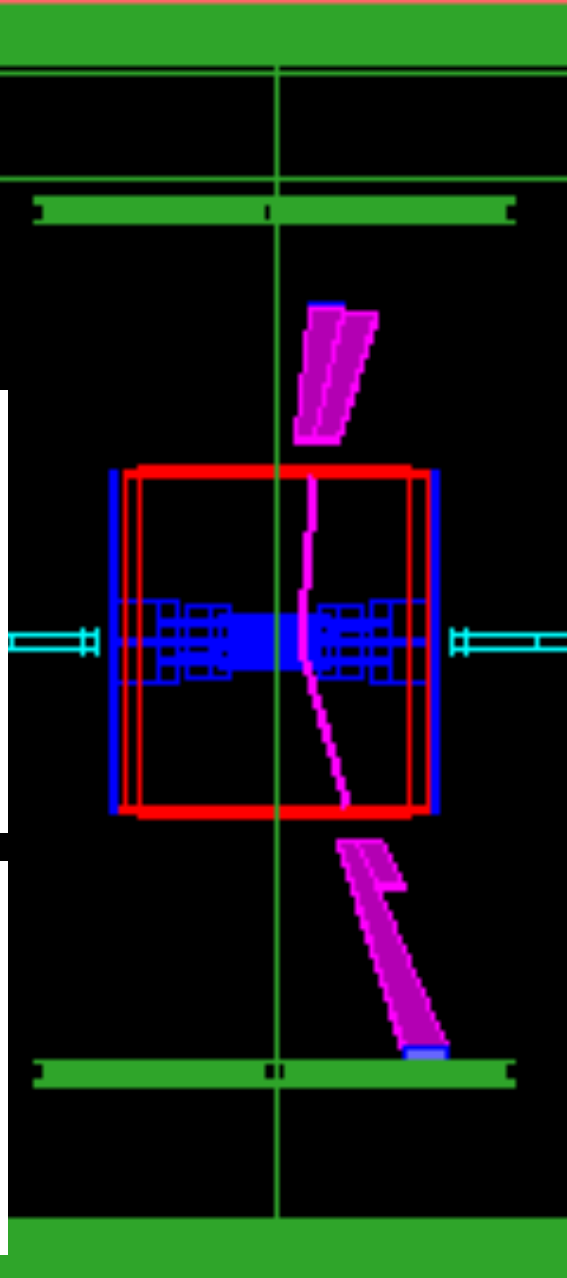


$$\sigma(p\bar{p} \rightarrow p\bar{p} l^+l^-) = 0.24^{+0.13}_{-0.10} \text{ pb}$$

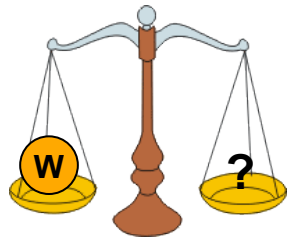
$[M_{ll} > 40 \text{ GeV}/c^2; |\eta_l| < 4]$

$$\sigma(p\bar{p} \rightarrow p\bar{p} Z^0) < 0.96 \text{ pb}$$

[@ 95% C.L.]



- Our involvement in CDF is almost over. Mark continues to oversee final Standard Model measurements.
- UCL involvement has been wide and varied, but precision electroweak measurements are a major legacy of CDF :



$$M_W = 80387 \pm 19 \text{ MeV}$$



$$\Gamma_W = 2032 \pm 73 \text{ MeV}$$



The End

