High-precision predictions for V+jet production

Jonas M. Lindert



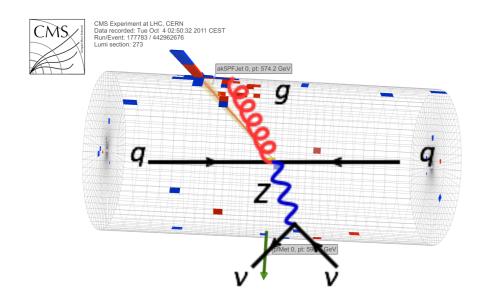


work in collaboration with:

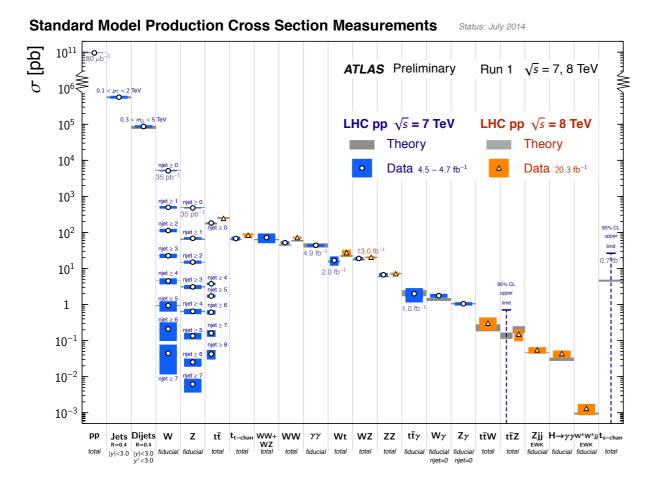
R. Boughezal, A. Denner, S. Dittmaier, A. Huss, A. Gehrmann-De Ridder, T. Gehrmann, N. Glover, S. Kallweit, P. Maierhöfer, M. L. Mangano, T.A. Morgan, A. Mück, M. Schönherr, F. Petriello, S. Pozzorini, G. P. Salam

UCL HEP Seminars UCL, London, 21.04.2017

V + multijet production

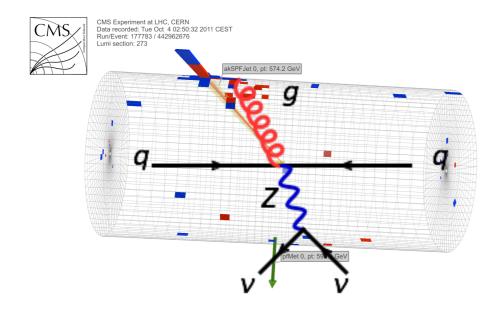


- ▶ Dominant backgrounds for monojet **DM searches**
- ▶ Important/dominant backgrounds for various BSM searches (lepton + missing E_T + ets)
- Dominant backgrounds for top physics
- Dominant backgrounds for Higgs physics, e.g.VH(→bb), H→WW



- Large cross-sections and clean leptonic signatures
- **V+jets**: Precision QCD at LHC
- Playground to probe different aspects of higher-order calculations (LO+PS, NLO+PS, NLO-Merging, NLO EW,...)
- Probe and constrain PDFs

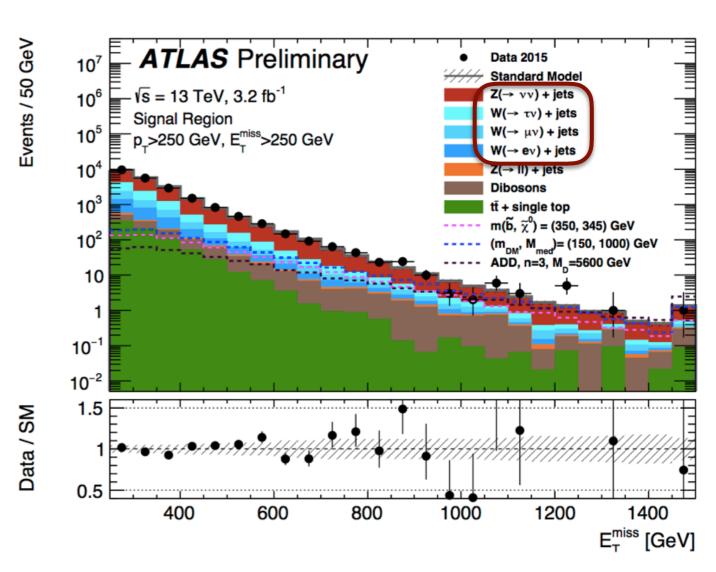
V+jets backgrounds in monojet/MET + jets searches



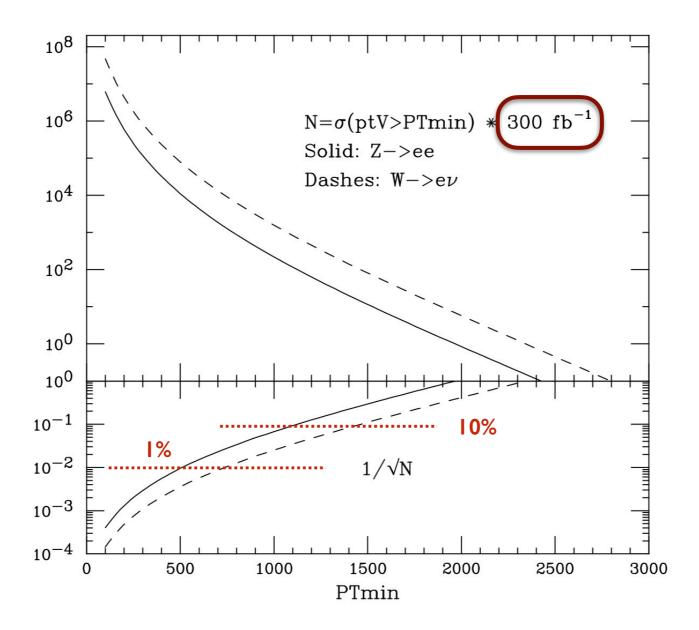
irreducible backgrounds:

$$pp \rightarrow Z(\rightarrow v\overline{v}) + jets \implies MET + jets$$

$$pp \rightarrow W(\rightarrow lv) + jets \implies MET + jets$$
 (lepton lost)

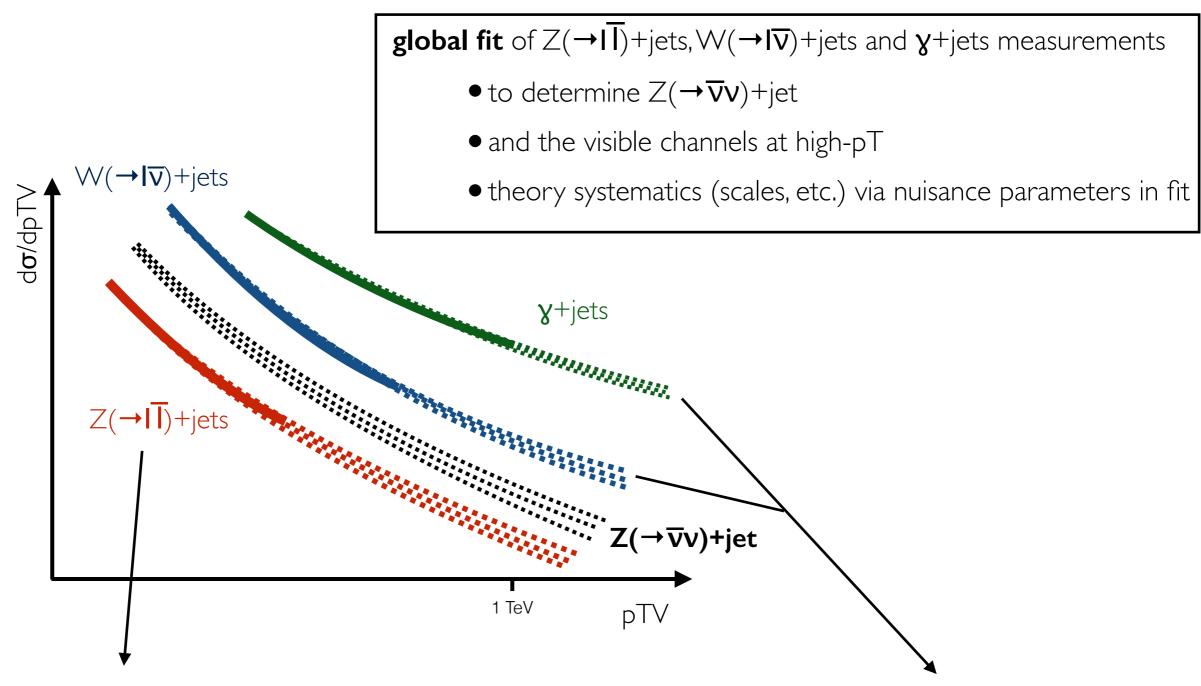


Target precision



- for 500 GeV < pTV < 1000 GeV: background statistics will be at 1% level
- understanding of V+jets backgrounds at this level increases sensitivity in DM searches
- this level of precision is theoretically possible @ NNLO QCD + NNLO EW
- requires solid understanding of uncertainties!

Determine V+jets backgrounds



- hardly any systematics (just QED dressing)
- very precise at low pT
- but: limited statistics at large pT

- fairly large data samples at large pT
- systematics from transfer factors

Goal of the ongoing study

[to be published soon, already available to ATLAS & CMS]

Combination of state-of-the-art predictions: (N)NLO QCD+(N)NLO EW
in order to match (future) experimental sensitivities
(1-10% accuracy in the few hundred GeV-TeV range)

$$\frac{\mathrm{d}}{\mathrm{d}x}\frac{\mathrm{d}}{\mathrm{d}\vec{y}}\sigma^{(V)}(\vec{\varepsilon}_{\mathrm{MC}},\vec{\varepsilon}_{\mathrm{TH}}) := \frac{\mathrm{d}}{\mathrm{d}x}\frac{\mathrm{d}}{\mathrm{d}\vec{y}}\sigma^{(V)}_{\mathrm{MC}}(\vec{\varepsilon}_{\mathrm{MC}}) \left[\frac{\frac{\mathrm{d}}{\mathrm{d}x}\sigma^{(V)}_{\mathrm{TH}}(\vec{\varepsilon}_{\mathrm{TH}})}{\frac{\mathrm{d}}{\mathrm{d}x}\sigma^{(V)}_{\mathrm{MC}}(\vec{\varepsilon}_{\mathrm{MC}})} \right]$$

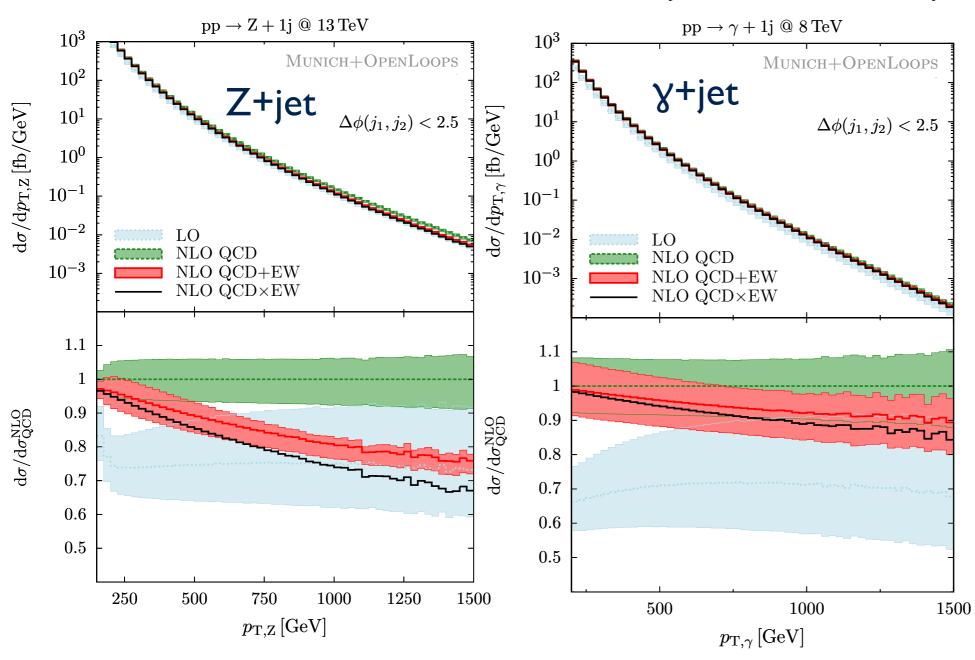
one-dimensional reweighting of MC samples in $x=p_{\mathrm{T}}^{(V)}$

with
$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{TH}}^{(V)} = \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{mix}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\Delta\sigma_{\mathrm{EW}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\gamma-\mathrm{ind}}^{(V)}.$$

- Robust uncertainty estimates including
 - I. Pure QCD uncertainties
 - 2. Pure EW uncertainties
 - 3. Mixed QCD-EW uncertainties
 - 4. PDF, γ -induced uncertainties

- Prescription for **correlation** of these uncertainties
 - within a process (between low-pT and high-pT)
 - across processes

Prelude: Z+jet vs. γ + 1 jet



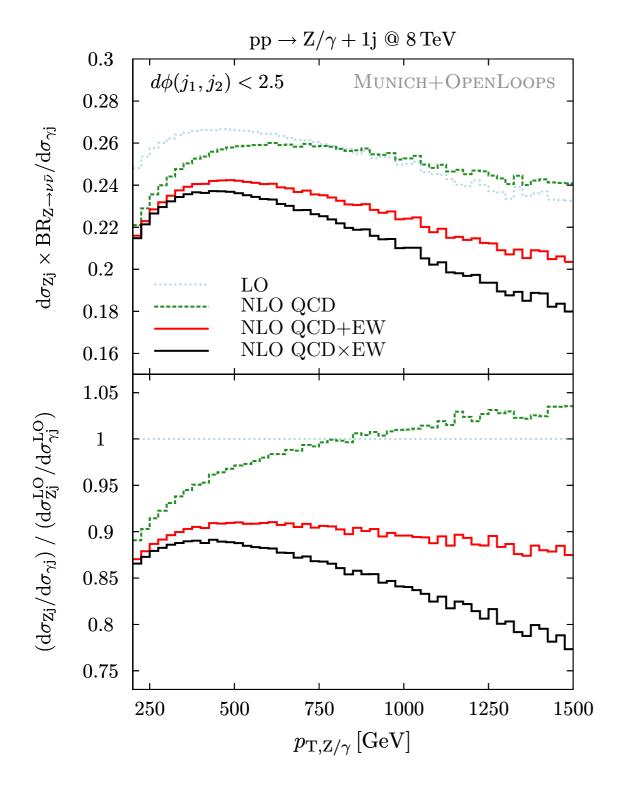
QCD corrections

- mostly moderate and stable QCD corrections
- (almost) identical QCD corrections in the tail, sizeable differences for small pT

EW corrections

- ▶ correction in pT(Z) > correction in pT(y)
- \blacktriangleright -20/-8% for Z/ $\!\gamma$ at 1 TeV
- ▶ EW corrections > QCD uncertainties for p_{T,Z} > 350 GeV

Prelude: \mathbb{Z}/\mathbf{y} pT-ratio



Overall

mild dependence on the boson pT

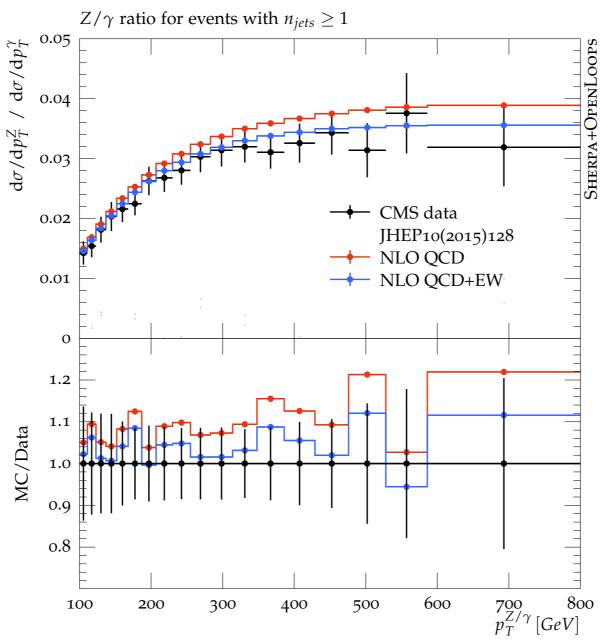
QCD corrections

- ▶ 10-15% below 250 GeV
- > ≤ 5% above 350 GeV

EW corrections

- sizeable difference in EW corrections results in 10-15% corrections at several hundred GeV
- ~5% difference between NLO QCD+EW and NLO QCDxEW

Prelude: compare against \mathbb{Z}/γ -data [JHEP10(2015)128]



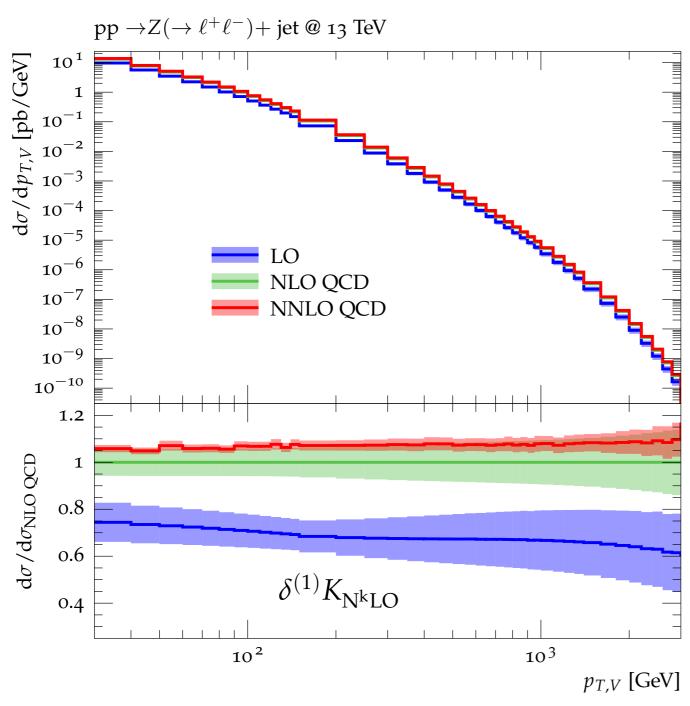
[Ciulli, Kallweit, JML, Pozzorini, Schönherr for **LH'15**]

▶ remarkable agreement with data at @ NLO QCD+EW!

I. pure QCD uncertainties

QCD effects

$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{QCD}}^{(V)} = \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LO\,QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NLO\,QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NNLO\,QCD}}^{(V)}$$



NNLO from [A. Huss, A. Gehrmann-De Ridder, T. Gehrmann, N. Glove, T.A. Morgan]

$$\mu_0 = \frac{1}{2} \left(\sqrt{p_{\mathrm{T},\ell^+\ell^-}^2 + m_{\ell^+\ell^-}^2} + \sum_{i \in \{q,g,\gamma\}} |p_{\mathrm{T},i}| \right)$$

this is a 'good' scale for V+jets

- at large pTV: HT'/2 ≈ pTV
- modest higher-order corrections
- sufficient convergence

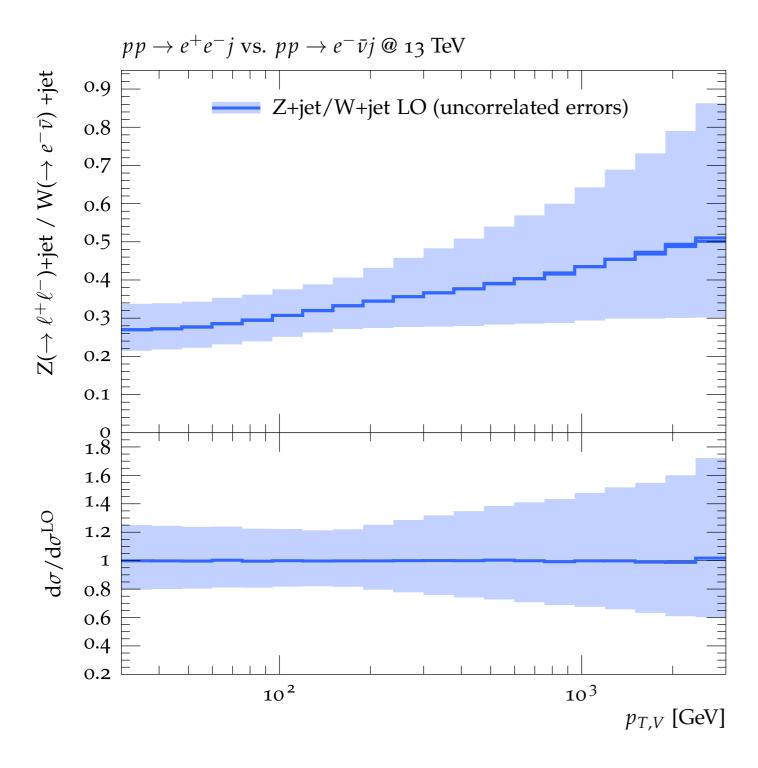
scale uncertainties due to 7-pt variations

$$\mu_{\rm R,F}=\xi_{\rm R,F}\mu_0$$

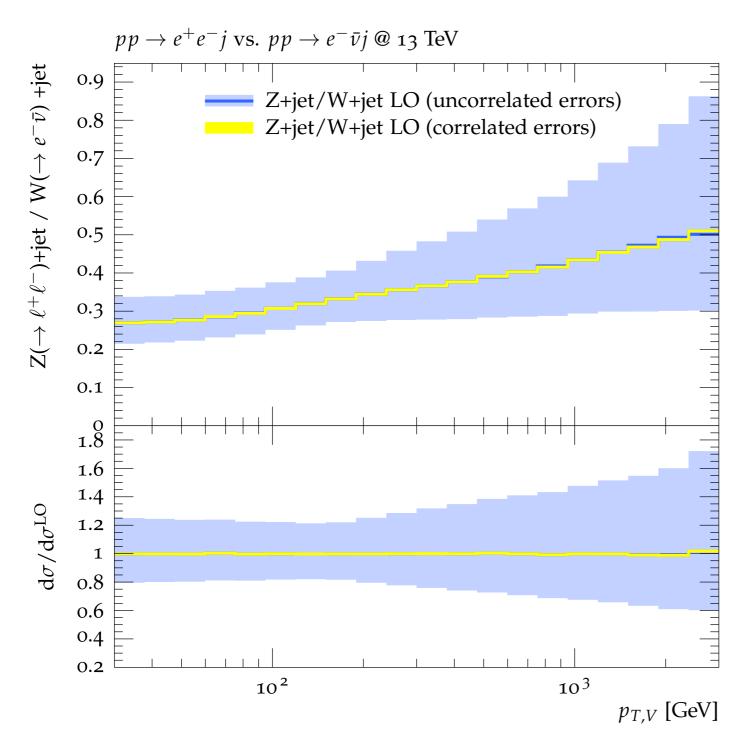
$$(\xi_{\rm R},\xi_{\rm F})=(2,2),\,(2,1),\,(1,2),\,(1,1),\,(1,0.5),\,(0.5,1),(0.5,0.5)$$
 yields
$$\Omega(20\%)\ \text{uncertainties at LO}$$

O(20%) uncertainties at LO O(10%) uncertainties at NLO O(5%) uncertainties at NNLO

with minor shape variations



consider Z+jet / W+jet $p_{T,V}$ -ratio @ LO uncorrelated treatment yields O(40%) uncertainties

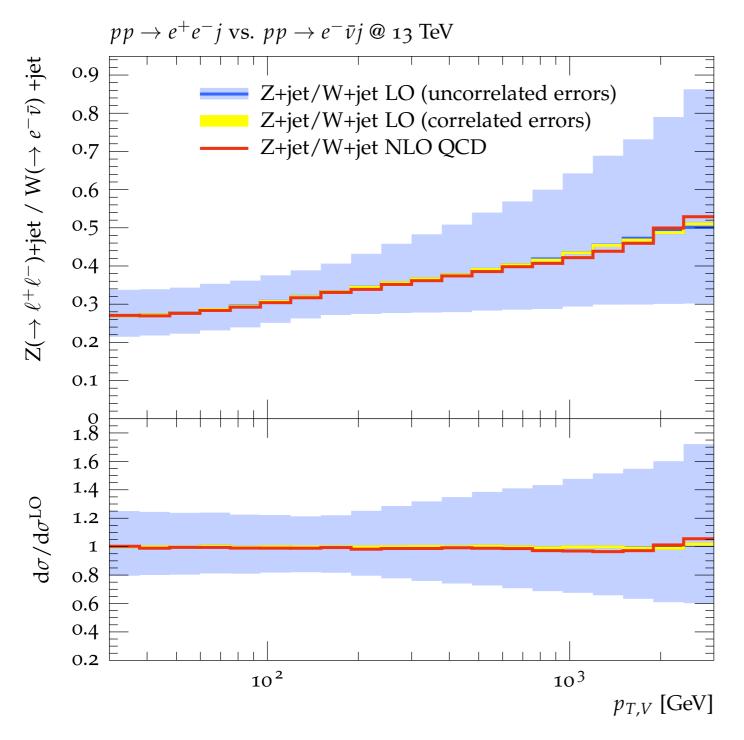


consider Z+jet / W+jet p_{T,V}-ratio @ LO

uncorrelated treatment yields O(40%) uncertainties

correlated treatment yields tiny O(<~ 1%) uncertainties

check against NLO QCD!



consider Z+jet / W+jet p_{T,V}-ratio @ LO

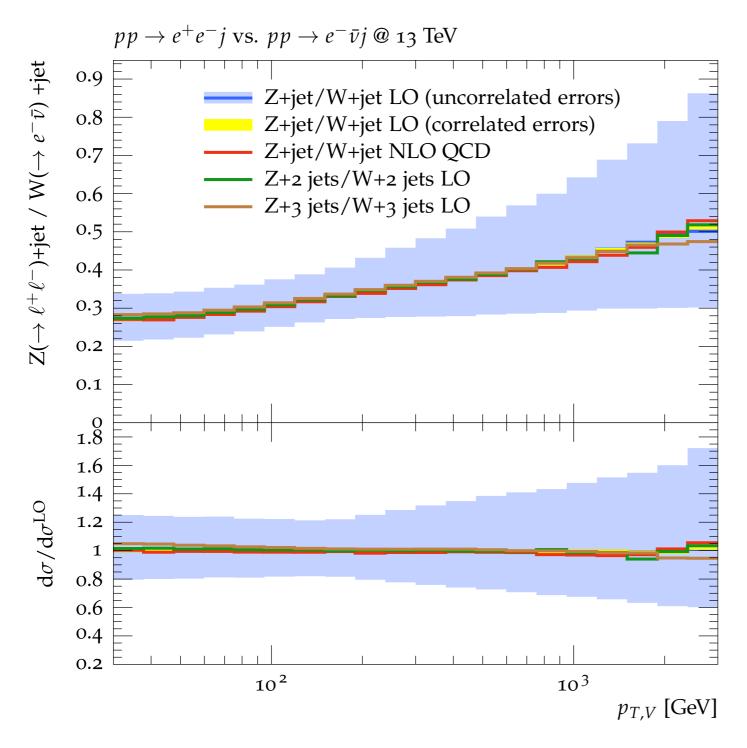
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correlated treatment yields tiny O(<~ 1%) uncertainties

check against NLO QCD!

NLO QCD corrections remarkably flat in Z+jet / W+jet ratio!

→ supports correlated treatment of uncertainties!



consider Z+jet / W+jet p_{T,V}-ratio @ LO

uncorrelated treatment yields O(40%) uncertainties

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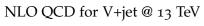
NLO QCD corrections remarkably flat in Z+jet / W+jet ratio!

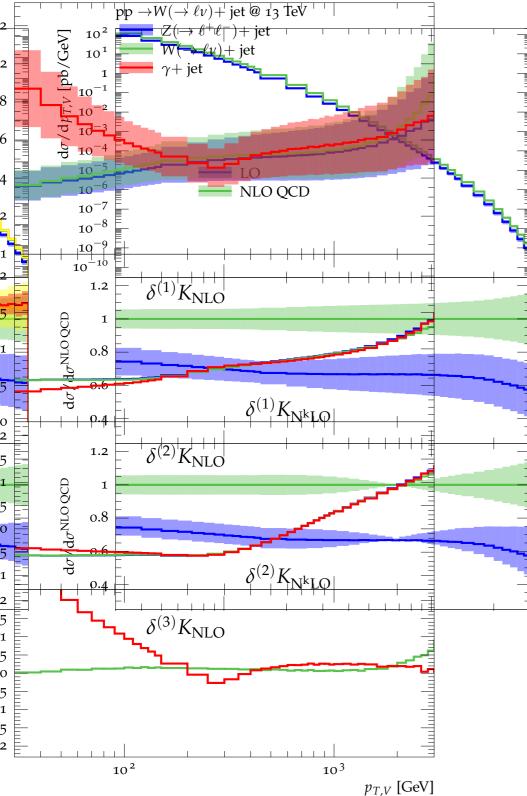
→ supports correlated treatment of uncertainties!

Also holds for higher jet-multiplicities

→ indication of correlation also in
higher-order corrections beyond NLO!

QCD uncertainties





$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{N}^{k}\mathrm{LO\,QCD}}^{(V)}(\vec{\varepsilon}_{\mathrm{QCD}}) = \begin{bmatrix} K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) + \sum_{i=1}^{3} \varepsilon_{\mathrm{QCD},i} \, \delta^{(i)} K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) \\ \times \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LO\,QCD}}^{(V)}(\vec{\mu}_{0}). \end{bmatrix}$$

$$\epsilon_{\rm QCD,i}^{(Z)} = \epsilon_{\rm QCD,i}^{(W^{\pm})} = \epsilon_{\rm QCD,i}^{(\gamma)} = \epsilon_{\rm QCD,i}$$

- correlated across processes
- correlated across pT bins

nuisance parameters:

interpreted as $I\sigma$ Gaussian

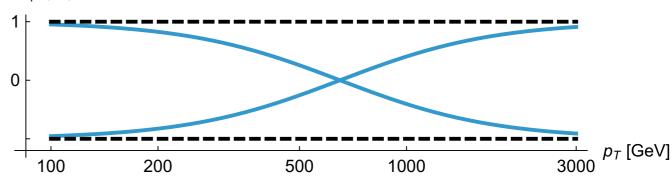
$$\bullet \quad \delta^{(1)}K_{N^{k}LO}^{V} = \frac{1}{2} \left[K_{N^{k}LO}^{V,\max} - K_{N^{k}LO}^{V,\min} \right]$$

symmetrized scale uncertainty

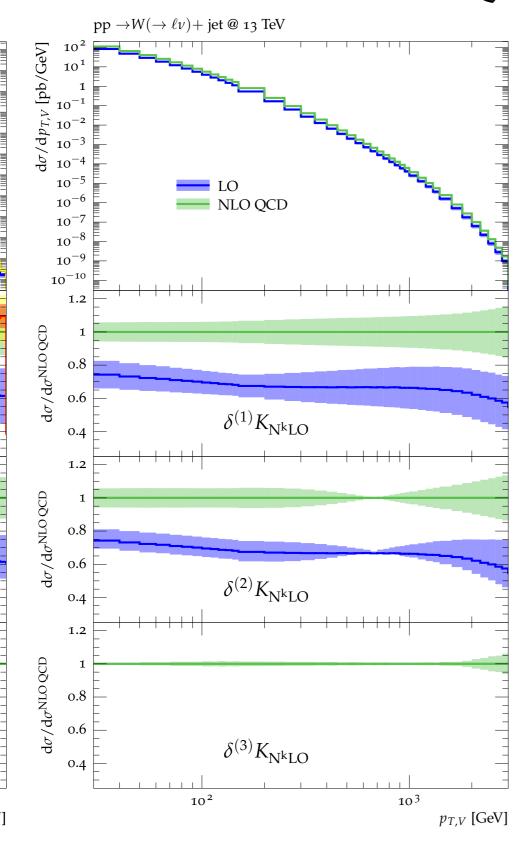
•
$$\delta^{(2)}K_{N^{k}LO}^{V} = \frac{p_{T}^{2} - 650 \text{ GeV}}{p_{T}^{2} + 650 \text{ GeV}} \delta^{(1)}K_{N^{k}LO}^{V}$$

yields max shape distortion within scale variation band

$\pm \omega_{\text{shape}}(p_T)$



QCD uncertainties



$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{N}^{k}\mathrm{LO\,QCD}}^{(V)}(\vec{\varepsilon}_{\mathrm{QCD}}) = \begin{bmatrix} K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) + \sum_{i=1}^{3} \varepsilon_{\mathrm{QCD},i} \, \delta^{(i)} K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) \\ \times \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LO\,QCD}}^{(V)}(\vec{\mu}_{0}). \end{bmatrix}$$

$$\epsilon_{\rm QCD,i}^{(Z)} = \epsilon_{\rm QCD,i}^{(W^{\pm})} = \epsilon_{\rm QCD,i}^{(\gamma)} = \epsilon_{\rm QCD,i}$$

- correlated across processes
- correlated across pT bins

nuisance parameters:

interpreted as $I\sigma$ Gaussian

$$\bullet \quad \delta^{(1)}K_{\mathrm{N^kLO}}^{V} = \frac{1}{2} \left[K_{\mathrm{N^kLO}}^{V,\mathrm{max}} - K_{\mathrm{N^kLO}}^{V,\mathrm{min}} \right]$$

symmetrized scale uncertainty

•
$$\delta^{(2)}K_{N^{k}LO}^{V} = \frac{p_{T}^{2} - 650 \text{ GeV}}{p_{T}^{2} + 650 \text{ GeV}} \delta^{(1)}K_{N^{k}LO}^{V}$$

yields max shape distortion within scale variation band

$$\bullet \quad \delta^{(3)} K_{N^{k}LO}^{V} = \frac{K_{N^{k}LO}^{V}}{K_{N^{k-1}LO}^{V}} - \frac{K_{N^{k}LO}^{Z}}{K_{N^{k-1}LO}^{Z}}$$

Difference of (N)NLO corrections as process correlation uncertainty

Caveat: χ +jet

Note: this modelling of process correlations assumes close similarity of QCD effects between different V+jets processes

$$\left| \frac{\sigma_{\rm NLO}^{(V)}}{\sigma_{\rm LO}^{(V)}} - \frac{\sigma_{\rm NLO}^{(Z)}}{\sigma_{\rm LO}^{(Z)}} \right| \ll \left| \frac{\sigma_{\rm NLO}^{(Z)}}{\sigma_{\rm LO}^{(Z)}} \right|$$

- apart from PDF effects it is the case for W+jets vs. Z+jets
- at pT > 200 GeV it is also the case for χ +jets vs. Z+jets.

Different logarithmic effects from fragmentation

W/Z+jet: masscut-off $MV_j \ge MV$

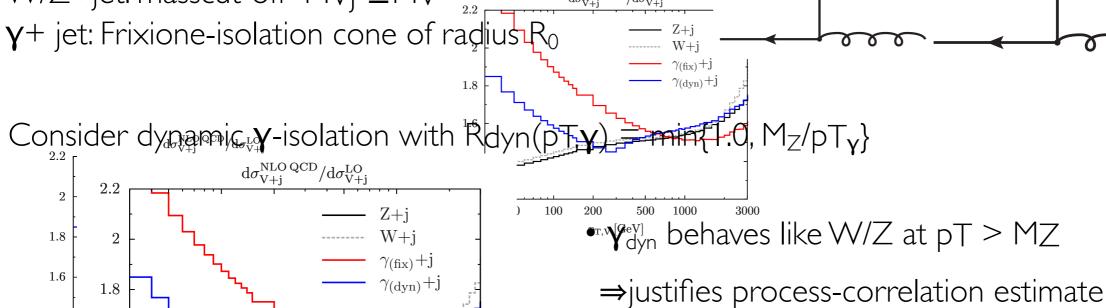
200

 $p_{\mathrm{T,V}}\left[\mathrm{GeV}\right]$

500

1000

3000



ullet remnant part $oldsymbol{\gamma}_{\text{fix}} - oldsymbol{\gamma}_{\text{dyn}}$ uncorrelated (uncertainty through extra reweighting and MC)

50

100

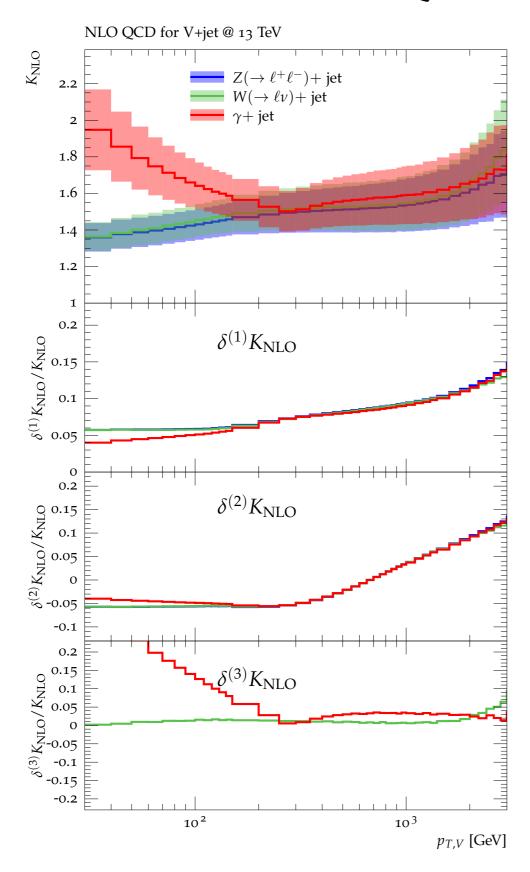
1.4

1.6

1.4

1.2

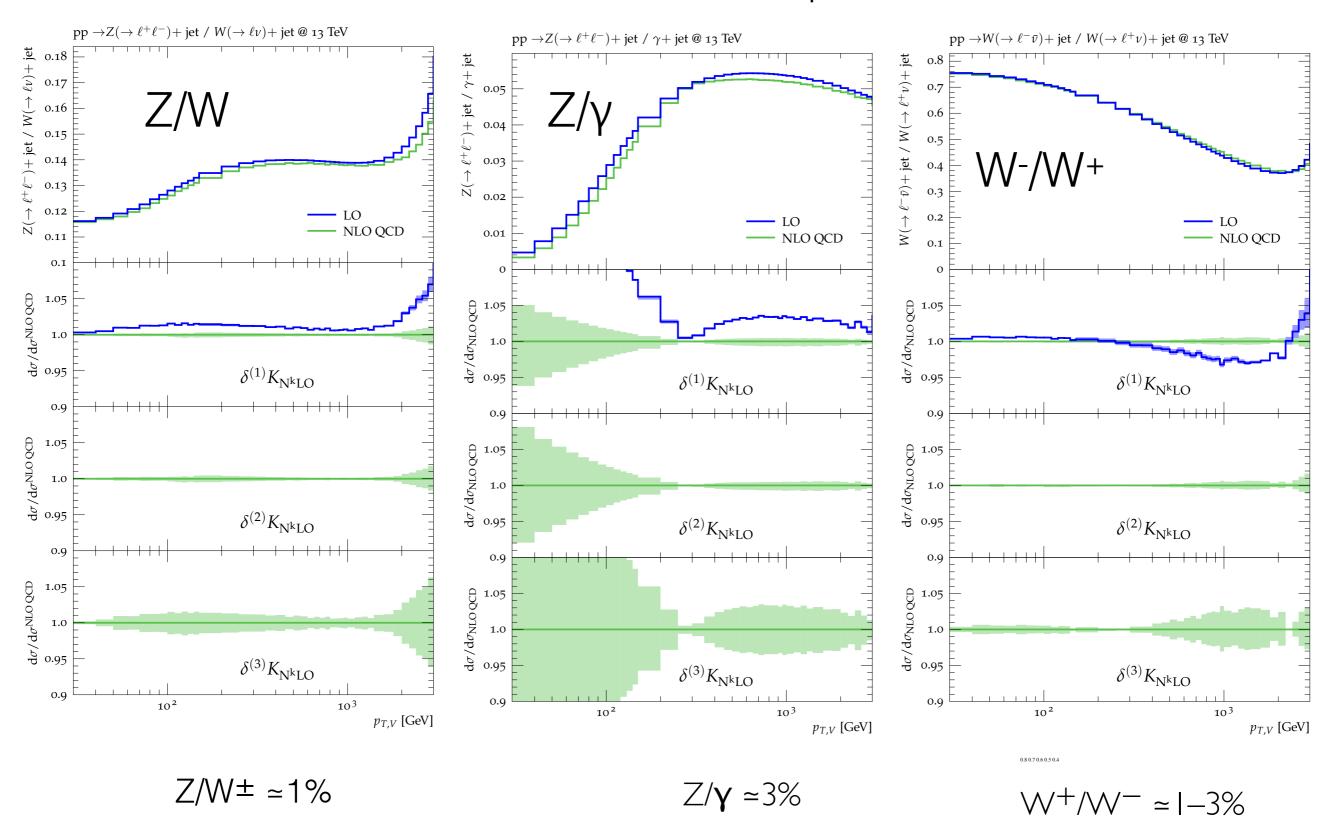
QCD uncertainties



NLO QCD corrections and uncertainties

- almost identical for W/Z/ γ for pTV > 200 GeV
- sizeable γ +jet fragmentation for pTV > 200 GeV

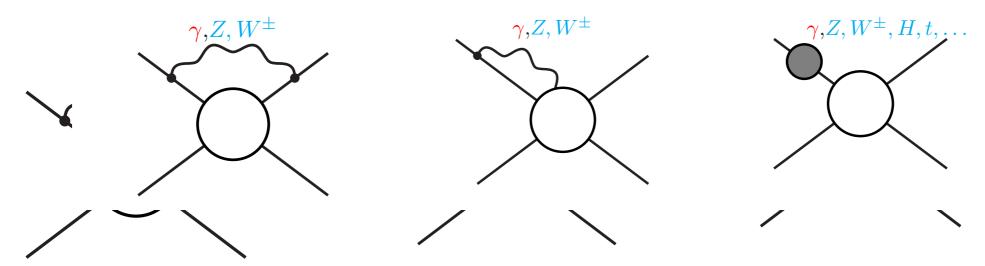
QCD uncertainties in pT-ratios



2. pure EW effects uncertainties

Virtual EW Sudakov logarithms

Originate from soft/collinear virtual EW bosons coupling to on-shell legs



Universality and factorisation similar as in QCD

[Denner, Pozzorini; '01]

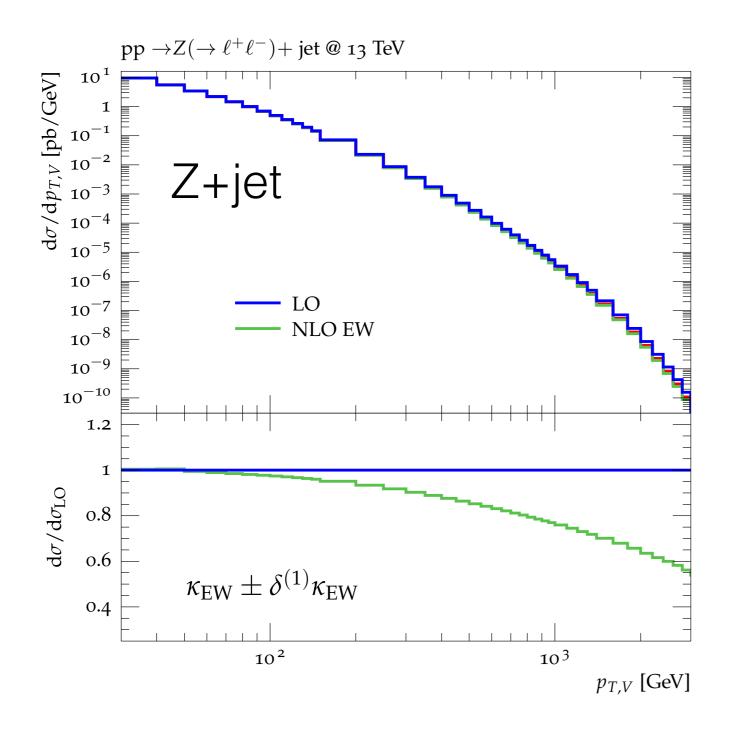
$$\delta \mathcal{M}_{\mathrm{LL+NLL}}^{\mathrm{1-loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^{n} \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^{\pm}} I^{a}(k) I^{\bar{a}}(l) \ln^{2} \left(\frac{\hat{s}_{kl}}{M_{W}^{2}} \right) + \gamma^{\mathrm{ew}}(k) \ln \left(\frac{\hat{s}}{M_{W}^{2}} \right) \right\} \mathcal{M}_{0}$$

- process-independent, simple structure
- typical size at $\sqrt{\hat{s}} = 1, 5, 10 \, \text{TeV}$:

$$\delta_{\rm LL} \sim -\frac{\alpha}{\pi s_W^2} \log^2 \frac{\hat{s}}{M_W^2} \simeq -28, -76, -104\%,$$

$$\delta_{\rm NLL} \sim +\frac{3\alpha}{\pi s_W^4} \log \frac{\hat{s}}{M_W^2} \simeq +16, +28, +32\%$$

- → large (negative) corrections at high energies (pT, MET, HT, Minv)
- → sizeable cancellations between leading and subleading terms possible

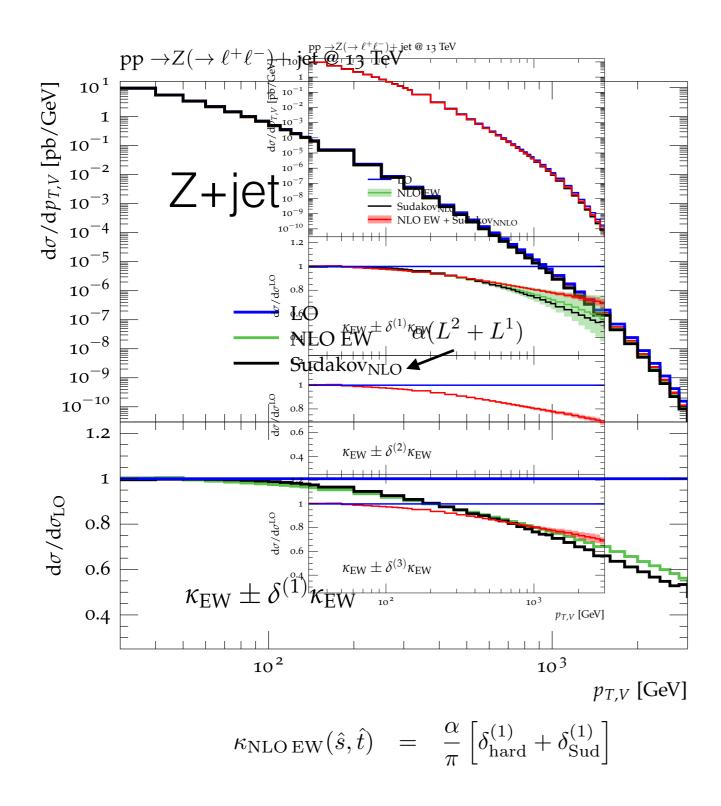


EW corrections become sizeable at large $p_{T,V}$

Origin: virtual EW Sudakov logarithms

Note: real EW Sudakov logarithms included as separate VV(+jets) backgrounds

How to estimate corresponding pure EW uncertainties of relative $\mathcal{O}(\alpha^2)$?

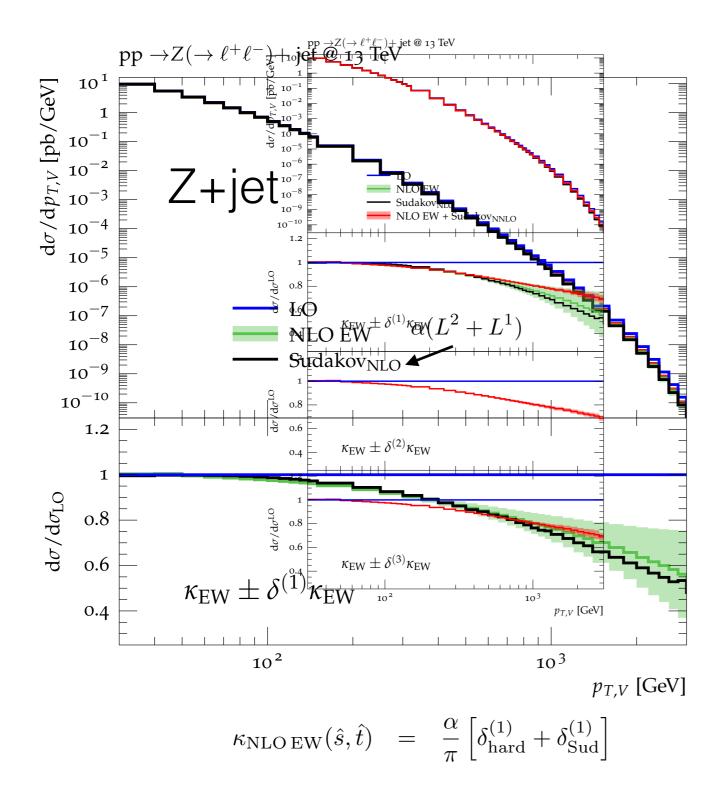


Large EW corrections dominated by Sudakov logs



Uncertainty estimate of NLO EW from naive exponentiation x 2:

$$\delta^{(1)} \kappa_{\rm EW} \simeq \frac{2}{k!} \left(\kappa_{\rm NLO,EW} \right)^k$$

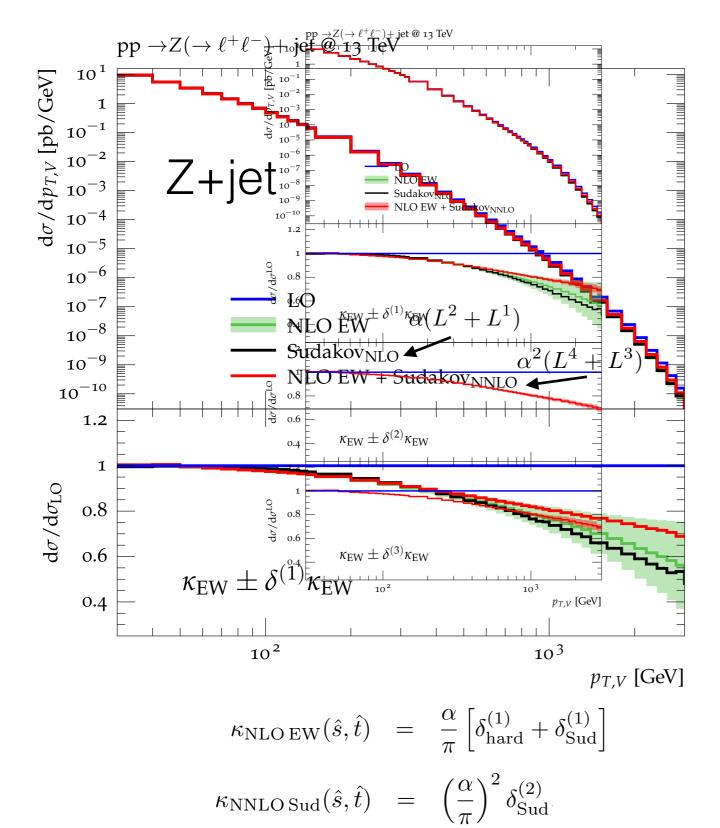


Large EW corrections dominated by Sudakov logs



Uncertainty estimate of NLO EW from naive exponentiation x 2:

$$\delta^{(1)} \kappa_{\rm EW} \simeq \frac{2}{k!} \left(\kappa_{\rm NLO,EW} \right)^k$$



Large EW corrections dominated by Sudakov logs

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Uncertainty estimate of NLO EW

from naive exponentiation \times 2:

$$\delta^{(1)} \kappa_{\text{EW}} \simeq \frac{2}{k!} \left(\kappa_{\text{NLO,EW}} \right)^{k}$$

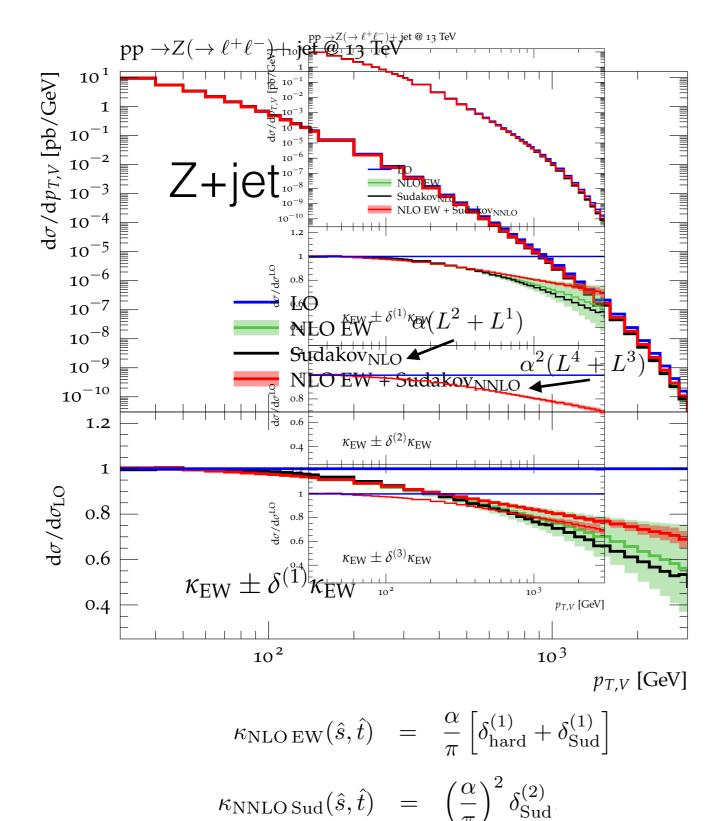
NNLO/LO - 1

NLO/LO - 1

NLO/LO - 1

NNLO/LO - 1

check against two-loop Sudakov of Sudakov of



Large EW corrections dominated by Sudakov logs



Uncertainty estimate of NLO EW from naive exponentiation x 2:

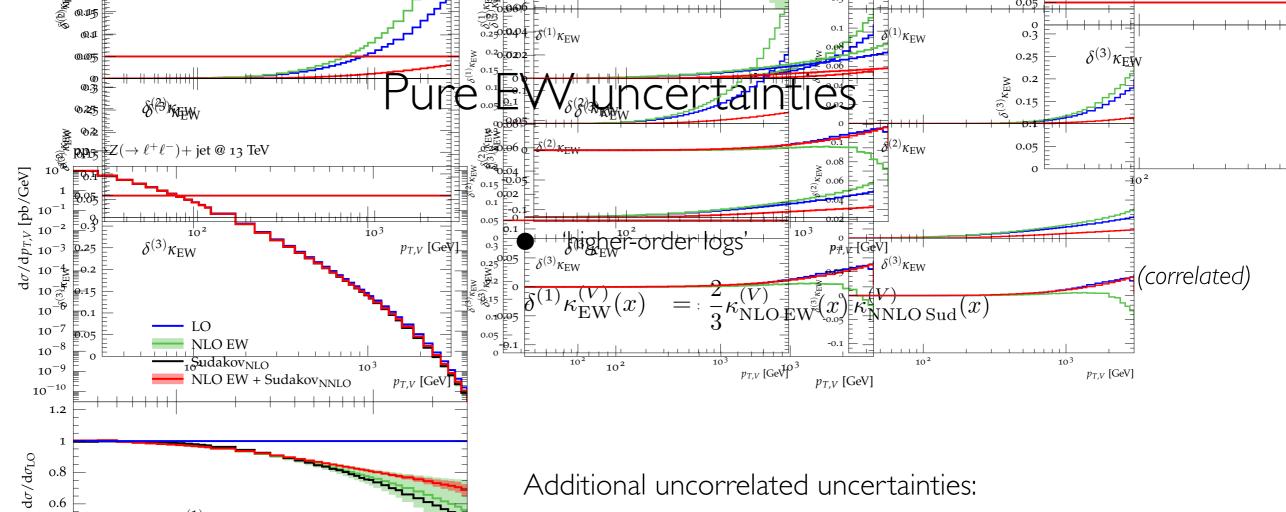
$$\delta^{(1)} \kappa_{\rm EW} \simeq \frac{2}{k!} \Big(\kappa_{\rm NLO,EW} \Big)^k$$

check against two-loop Sudakov logs [Kühn, Kulesza, Pozzorini, Schulze; 05-07]



Uncertainty estimate of NNLO EW:

$$\delta^{(1)} \kappa_{\text{EW}}^{(V)}(x) = \frac{2}{3} \kappa_{\text{NLO EW}}^{(V)}(x) \kappa_{\text{NNLO Sud}}^{(V)}(x)$$



Additional uncorrelated uncertainties:

'hard non-log NNLO effects l'

$$\delta^{(2)} \kappa_{\text{EW}}^{(V)}(x) = 0.05 \, \kappa_{\text{NLO EW}}^{(V)}(x)$$

(uncorrelated)

$$\Leftrightarrow \delta_{\text{hard}}^{(2)} \leq \frac{0.05\pi}{\alpha} \delta_{\text{hard}}^{(1)} \simeq 20 \delta_{\text{hard}}^{(1)}$$

'hard non-log NNLO effects II'

$$\delta^{(3)} \kappa_{\text{EW}}^{(V)}(x) = \kappa_{\text{NNLO Sud}}^{(V)}(x) - \frac{1}{2} [\kappa_{\text{NLO EW}}^{(V)}(x)]^2$$

(uncorrelated)

estimate of typical size of $\left[\delta_{\mathrm{hard}}^{(1)}\right]^2$ or $\delta_{\mathrm{hard}}^{(1)} \times \delta_{\mathrm{Sud}}^{(1)}$.

 $\kappa_{\rm EW} \pm \delta^{(1)} \kappa_{\rm EW}$

 $\kappa_{\rm EW} \pm \delta^{(2)} \kappa_{\rm EW}$

 $\kappa_{\rm EW} \pm \delta^{(3)} \kappa_{\rm EW}$

103

 $p_{T,V}$ [GeV]

0.4

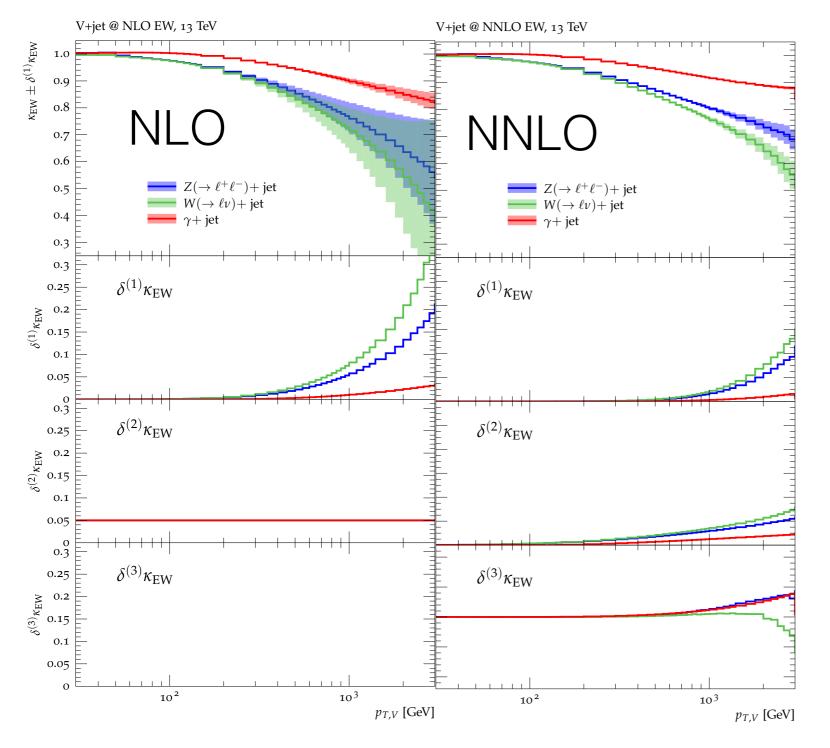
0.8

 $d\sigma/d\sigma^{LO}$

 ${\rm d}\sigma/{\rm d}\sigma^{\rm LO}$

0.6

0.4



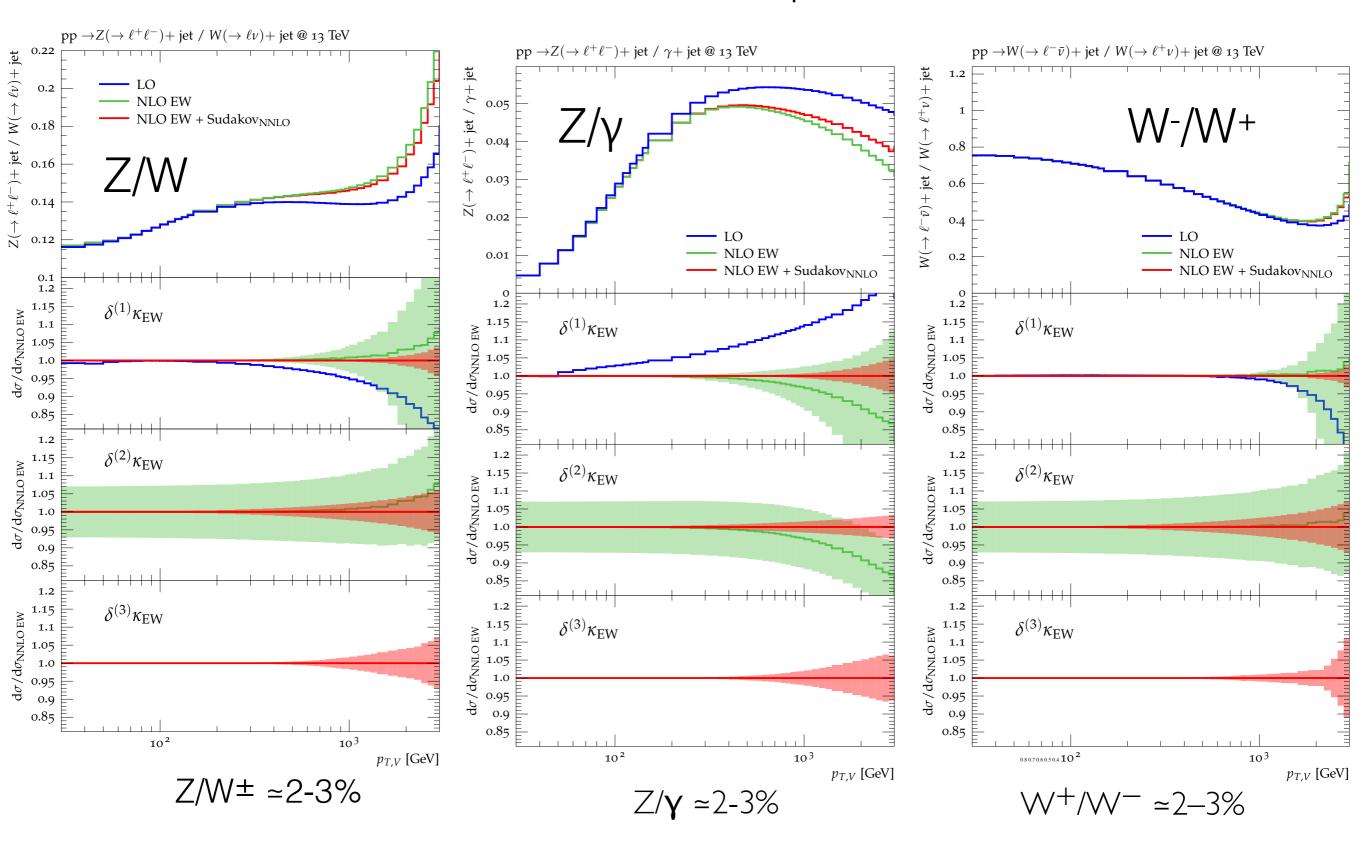
NNLO EW corrections at I TeV

- -10% for γ +jets
- -20% for Z+jet
- -25% for W+jet

Pure EW uncertainties

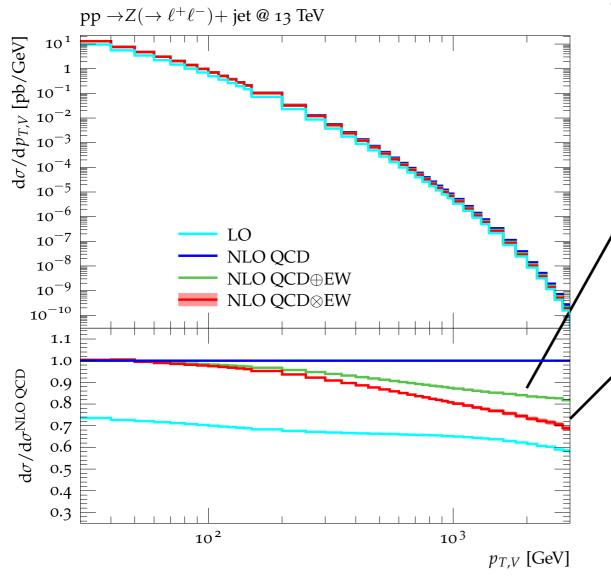
- tiny at low pT and only I-2% at I TeV
- thanks to NNLO Sudakov logs (up to ~ 5%)

EW uncertainties in pT-ratios



3. mixed QCD-EW uncertainties

Mixed QCD-EW uncertainties



Given QCD and EW corrections are sizeable, also mixed QCD-EW uncertainties of relative $\mathcal{O}(\alpha\alpha_s)$ have to be considered.

Additive combination

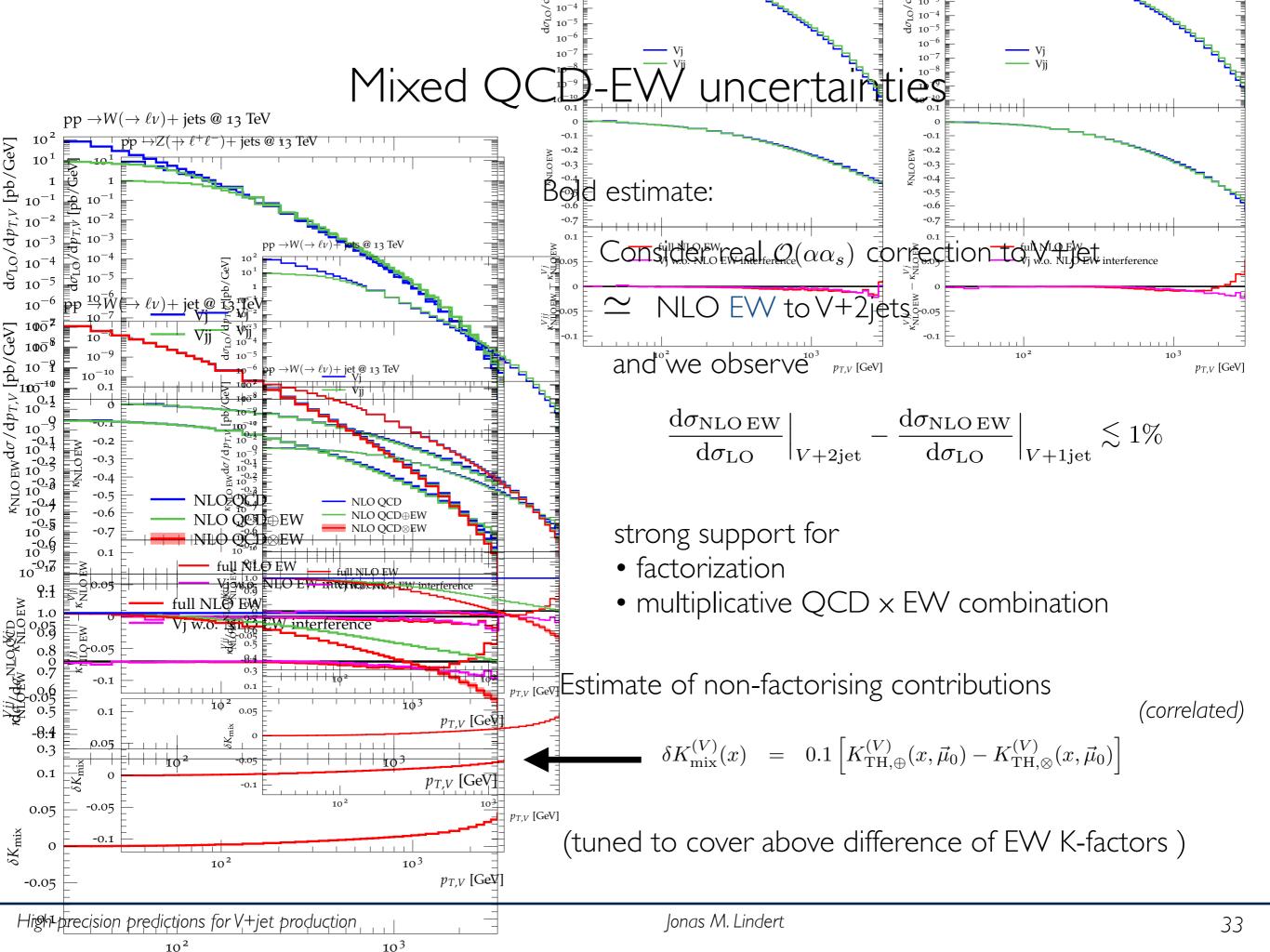
$$\sigma_{\mathrm{QCD}+\mathrm{EW}}^{\mathrm{NLO}} = \sigma^{\mathrm{LO}} + \delta\sigma_{\mathrm{QCD}}^{\mathrm{NLO}} + \delta\sigma_{\mathrm{QCD}}^{\mathrm{NLO}} + \delta\sigma_{\mathrm{EW}}^{\mathrm{NLO}} + \delta\sigma_{\mathrm{EW}}^{\mathrm{NLO}} + \delta\sigma_{\mathrm{QCD}}^{\mathrm{NLO}} + \delta\sigma_{\mathrm$$

Difference between these two approaches indicates size of missing mixed EW-QCD corrections.

$$K_{\rm QCD\otimes EW}-K_{\rm QCD\oplus EW}\sim 10\%$$
 at 1 TeV

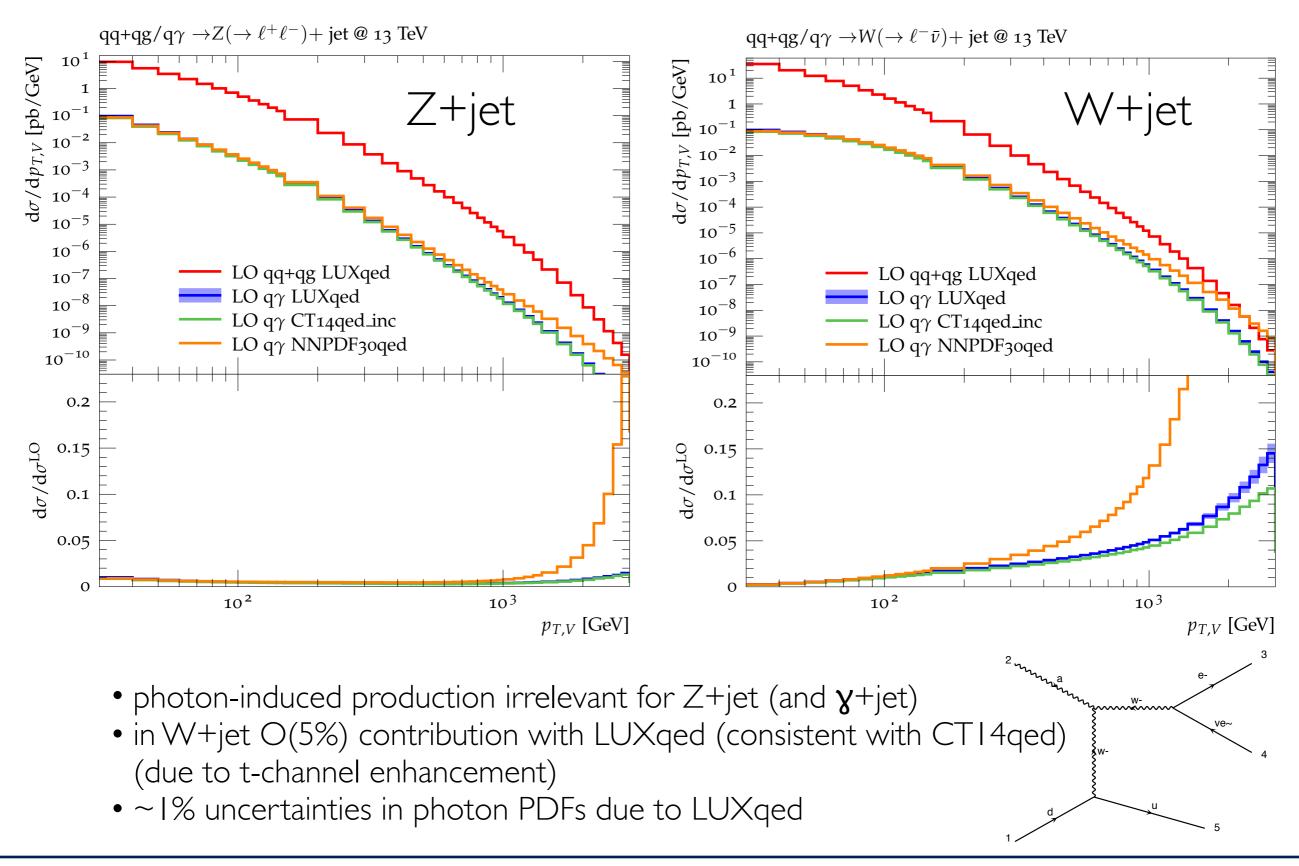
Too conservative!?

For dominant Sudakov EW logarithms factorization should be exact!

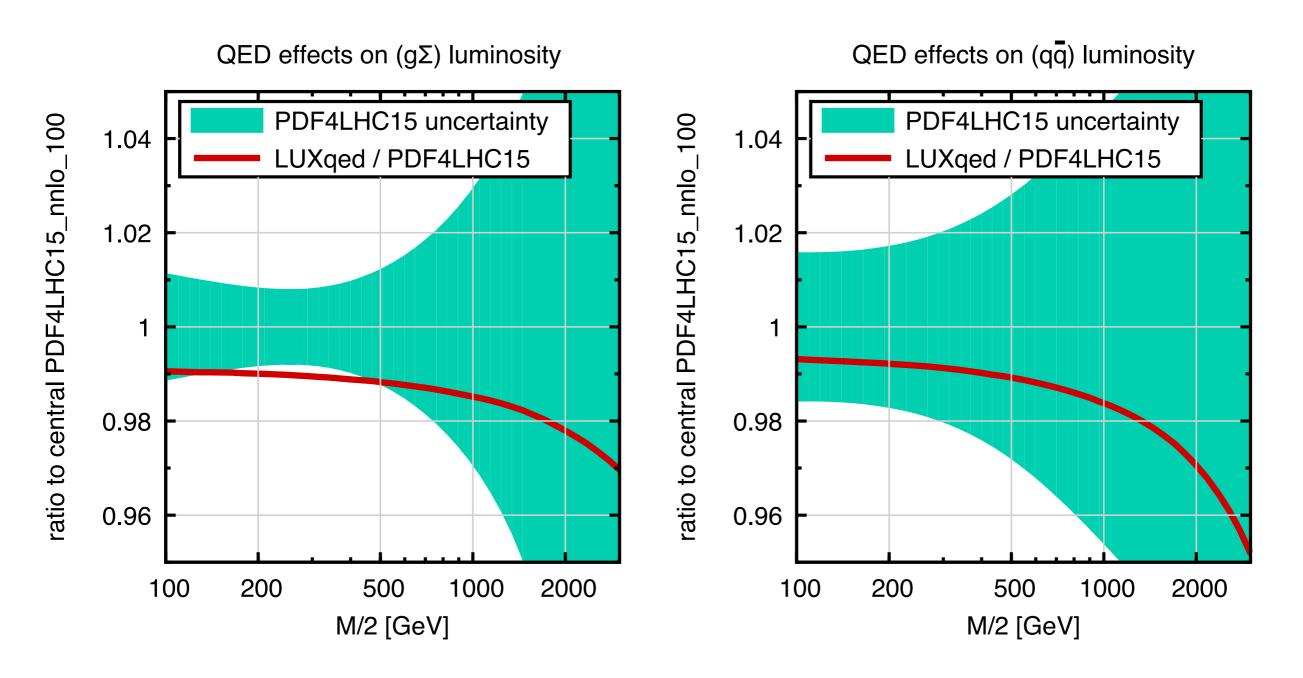


4. Other issues (PDFs, y-induced)

Photon-induced production



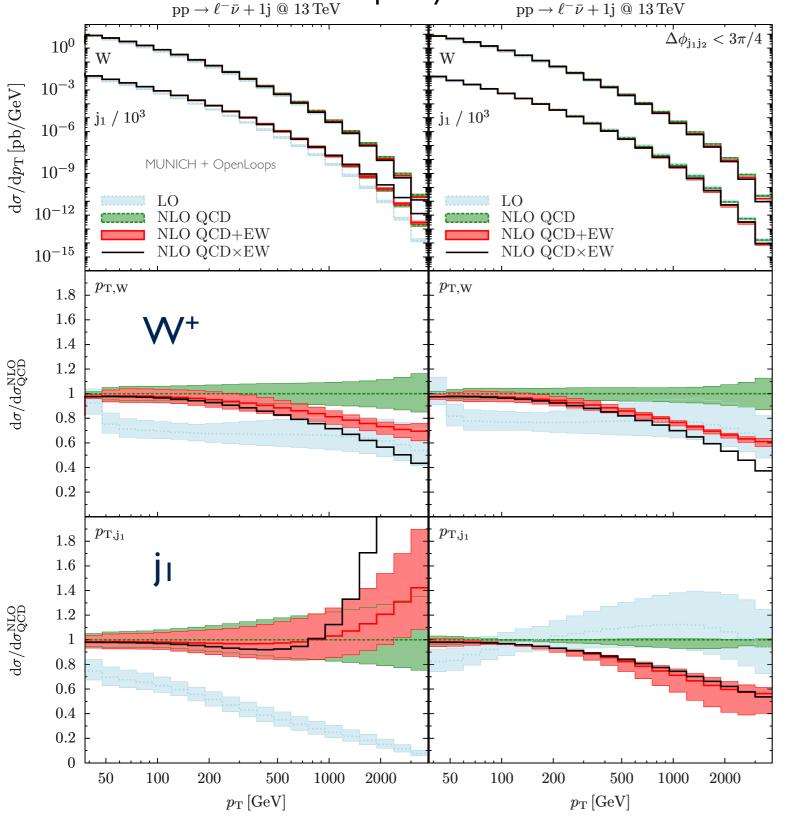
PDFs



- small percent-level QED effects on qg/qq luminosities (included via LUXqed)
- 1.5-5% PDF uncertainties

Exclusive V+jets

Interplay between QCD and EW $_{\text{pp} \rightarrow \ell^-\bar{\nu}+1j \ @ \ 13 \, \text{TeV}}$

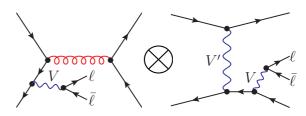


p⊤ of jet

- "giant QCD K-factors" in the tail [Rubin, Salam, Sapeta '10]
- dominated by dijet configurations
- ▶ positive 10-50% EW corrections from quark bremsstrahlung

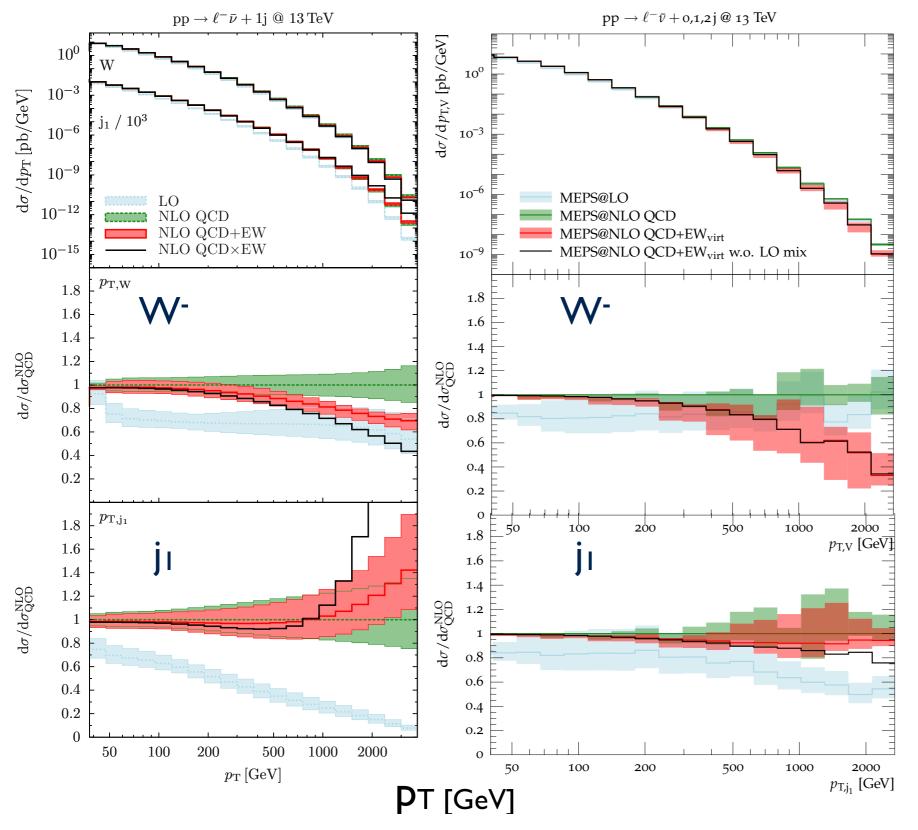
soft W/Z

00000000



- ⇒ pathologic with large uncertainties!
- ⇒ exclusive jet observables require merging W+1 jet with W+2 jets at NLO QCD+EW!

MEPS@NLO QCD+EWvirt



- ▶ Stable NLO QCD+EW predictions in all of the phase-space...
- …including Parton-Shower effects.
- ▶ Can directly be used by the experimental collaborations
- ▶ p_{T,V} : MEPS@NLO QCD+EW in agreement with QCDxEW (fixed-order)
 - ★again: support for factorization!!
- ▶ p_{T,j1}: compensation between negative Sudakov and LO mix

Conclusions

- ▶ monojet / MET+jets searches soon limited by V+jets background systematics
- ▶ MC reweighting allows to promote V + jet to NNLO QCD+(N)NLO EW:
 - inclusion of EW corrections crucial due to large Sudakov logs
- ▶ Perturbative systematics in pTV under control at the level of I-10% up to the TeV

Outlook

- ▶ percent precision requires scrutiny of many subtleties and close TH/EXP interplay
- ▶ Experimental closure tests in control regions
- ▶ Applicability to other more exclusive observables / process classes

Illuminating standard candles at the LHC - V+jets

25-26 April 2017 0 Search... Imperial College London Europe/London timezone Overview This informal, brainstorming workshop held in conjunction with the IPPP (Institute for Particle Physics Phenomenology at Durham) will focus on the Standard Model Timetable measurements of vector boson + jets processes that we can perform in Run 2 of the LHC Contribution List to enhance our understanding of the high transverse momentum phase space and constrain higher order QCD and electroweak corrections. My Conference My Contributions Registration **Starts** 25 Apr 2017 10:00 Imperial College London Blackett building, room 539 **Ends** 26 Apr 2017 14:00 Participant List Europe/London https://workspace.imperial.ac.uk/campusinfo/p Sarah Malik 2 Materials Bjoern Penning Jonas Lindert There are no materials yet. Info on booking accommodation around the South Kensington area: http://www.imperial.ac.uk/visitors-accommodation/local-hotels/ How to get to the South Kensington Campus: https://www.imperial.ac.uk/visit/campuses/southkensington/ Registration See details > You have registered for this event.

https://indico.cern.ch/event/624982

BACKUP

Putting everything together

$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{TH}}^{(V)}(\vec{\mu}) = K_{\mathrm{TH}}^{(V)}(x,\vec{\mu}) \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LOQCD}}^{(V)}(\vec{\mu}_0) + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\gamma-\mathrm{ind.}}^{(V)}(x,\vec{\mu})$$

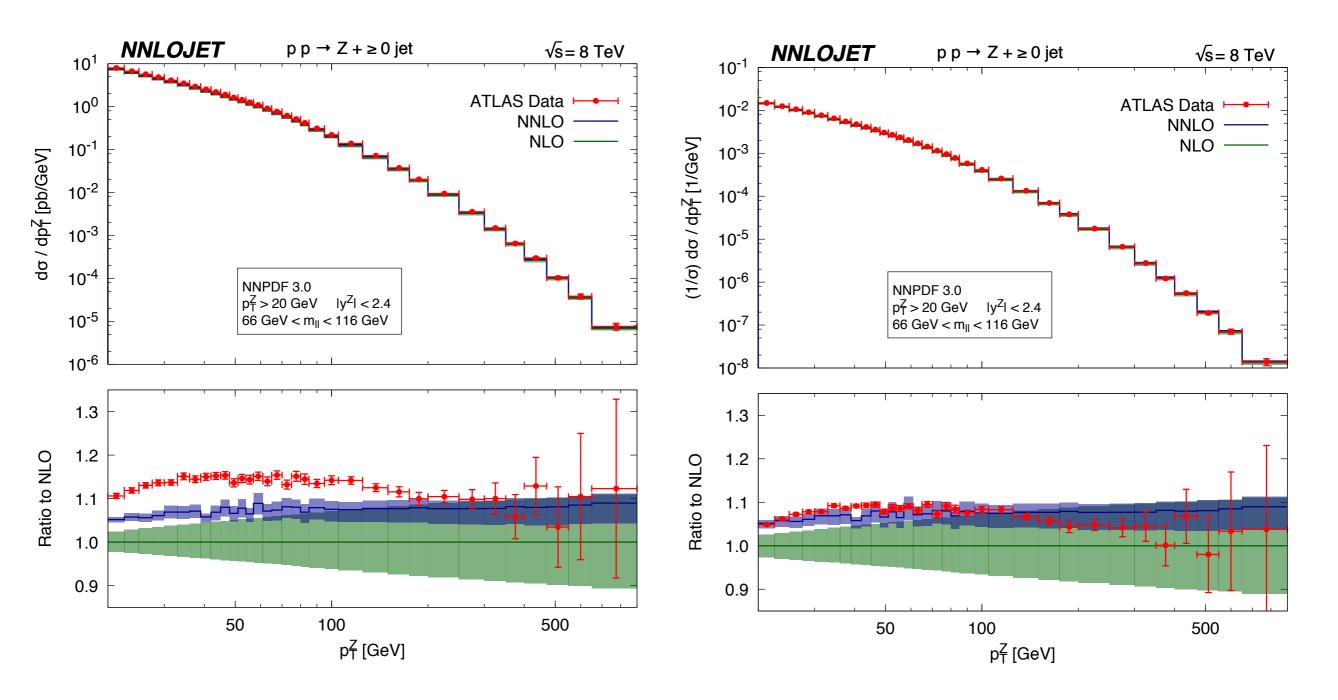
$$\begin{split} K_{\mathrm{TH}}^{(V)}(x,\vec{\varepsilon}_{\mathrm{QCD}},\vec{\varepsilon}_{\mathrm{EW}},\varepsilon_{\mathrm{mix}}) &= K_{\mathrm{TH},\otimes}^{(V)}(x,\vec{\varepsilon}_{\mathrm{QCD}},\vec{\varepsilon}_{\mathrm{EW}}) + \varepsilon_{\mathrm{mix}}\,\delta K_{\mathrm{mix}}^{(V)}(x), \\ &= \left[K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) + \sum_{i=1}^{3} \varepsilon_{\mathrm{QCD},i}\,\delta^{(i)}K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x)\right] \\ &\times \left[1 + \kappa_{\mathrm{EW}}^{(V)}(x) + \sum_{i=1}^{3} \varepsilon_{\mathrm{EW},i}^{(V)}\,\delta^{(i)}\kappa_{\mathrm{EW}}^{(V)}(x)\right] + \varepsilon_{\mathrm{mix}}\,\delta K_{\mathrm{mix}}^{(V)}(x), \end{split}$$

$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{QCD}}^{(V)} = \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LO\,QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NLO\,QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NNLO\,QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NNLO\,QCD}}^{(V)}$$

$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{EW}}^{(V)} = \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NLO\,EW}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{Sudakov\,NNLO\,EW}}^{(V)}$$

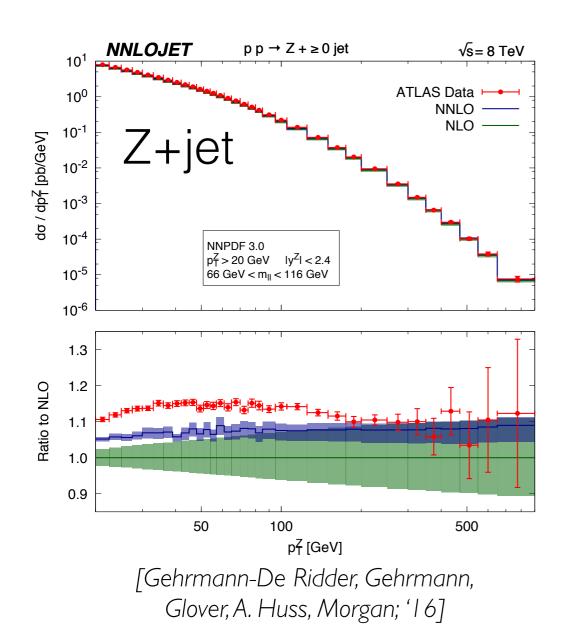
with nuisance parameters $\vec{\varepsilon}_{TH} = (\vec{\varepsilon}_{QCD}, \hat{\varepsilon}, \vec{\varepsilon}_{EW}, \varepsilon_{\gamma})$

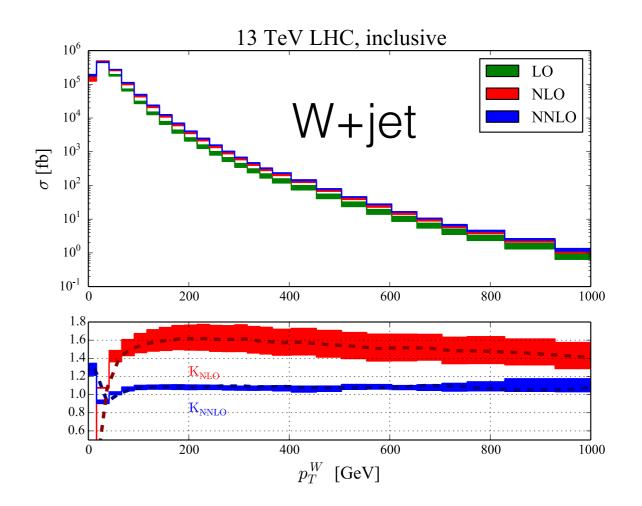
NNLO for Z+jet



[Gehrmann-De Ridder, Gehrmann, Glover, A. Huss, Morgan; 'I 6]

NNLO for W/Z+jet

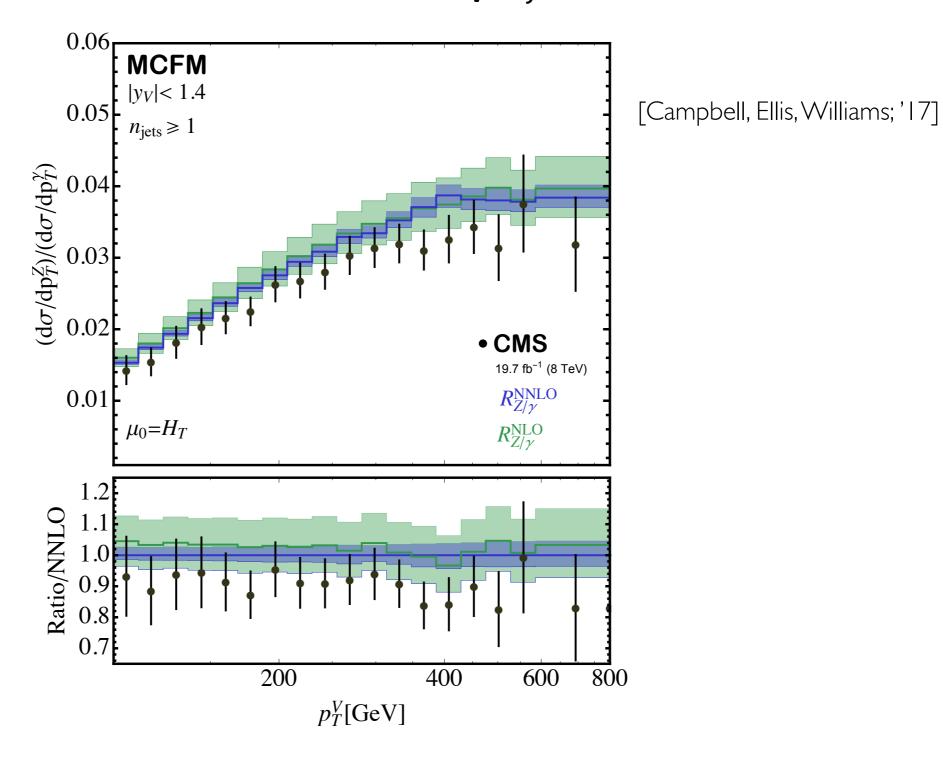




[Boughezal, Liu, Petriello; 'I 6]

- unprecedented reduction of scale uncertainties at NNLO: $O(\sim 5\%)$
- we can now check the correlation of the uncertainties going from NLO to NNLO

NNLO for Z/γ +jet



NNLO/NLO ~ 1 for large pT!

Combination of NLO QCD and EW & Setup

Two alternatives:

$$\sigma_{\text{QCD}+\text{EW}}^{\text{NLO}} = \sigma^{\text{LO}} + \delta\sigma_{\text{QCD}}^{\text{NLO}} + \delta\sigma_{\text{EW}}^{\text{NLO}}$$

$$\sigma_{\text{QCD}\times\text{EW}}^{\text{NLO}} = \sigma_{\text{QCD}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right) = \sigma_{\text{EW}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{QCD}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right)$$

Difference between the two approaches indicates uncertainties due to missing two-loop EW-QCD corrections of $\mathcal{O}(\alpha\alpha_s)$

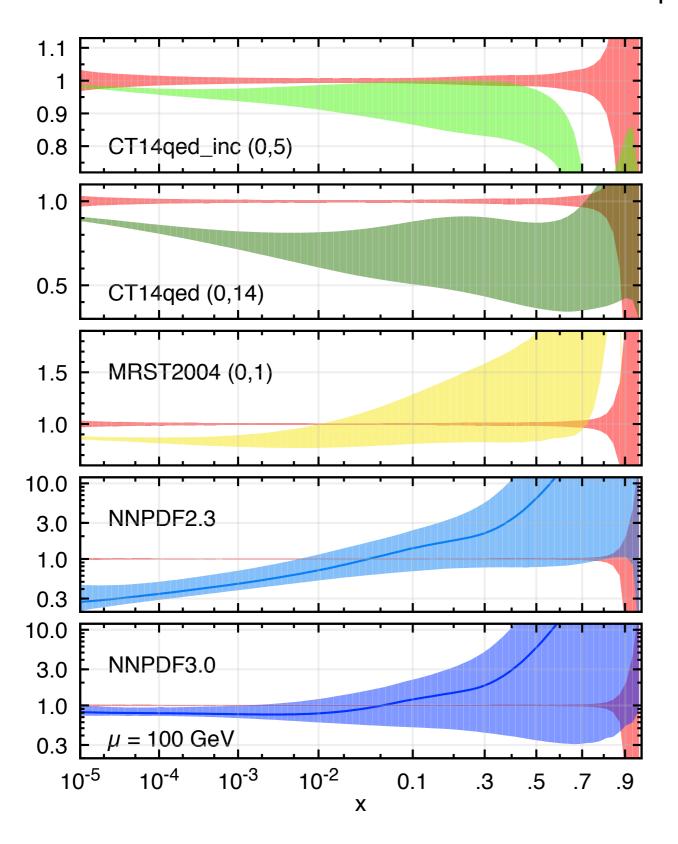
Relative corrections w.r.t. NLO QCD:

$$\frac{\sigma_{\rm QCD+EW}^{\rm NLO}}{\sigma_{\rm QCD}^{\rm NLO}} = \left(1 + \frac{\delta\sigma_{\rm EW}^{\rm NLO}}{\sigma_{\rm QCD}^{\rm NLO}}\right) \qquad \text{suppressed by large NLO QCD corrections}$$

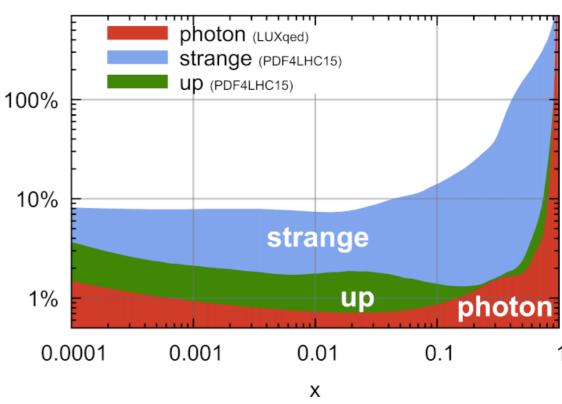
$$\frac{\sigma_{\rm QCD\times EW}^{\rm NLO}}{\sigma_{\rm QCD}^{\rm NLO}} = \left(1 + \frac{\delta\sigma_{\rm EW}^{\rm NLO}}{\sigma_{\rm LO}^{\rm NLO}}\right) \qquad \text{``usual'' NLO EW w.r.t. LO}$$

$$ho = \frac{\sqrt{2}}{\pi} G_{\mu} M_{\mathrm{W}}^2 \left(1 - \frac{M_{\mathrm{W}}^2}{M_{\mathrm{Z}}^2} \right)$$
 in G_{μ} -scheme with $G_{\mu} = 1.16637 \times 10^{-5} \; \mathrm{GeV}^{-2}$

LUXqed



PDF uncertainties (Q = 100 GeV)



[Manohar, Nason, Salam, Zanderighi, '16]

